

Ex: Find the rectangular and polar forms of $\frac{6-j2}{4+j5}$.

Ans: $\frac{14}{41} - j\frac{38}{41}$ and $0.987e^{-j69.78^\circ}$

$$\begin{aligned}\text{SOL'N: } \frac{6-j2}{4+j5} &= \frac{6-j2}{4+j5} \frac{(4+j5)^*}{(4+j5)^*} = \frac{6-j2}{4+j5} \frac{(4-j5)}{(4-j5)} \\ &= \frac{24-10-j(30+8)}{16+25} = \frac{14}{41} - j\frac{38}{41}\end{aligned}$$

$$A = \sqrt{\left(\frac{14}{41}\right)^2 + \left(\frac{38}{41}\right)^2} = 0.987$$

$$\phi = \tan^{-1}\left(\frac{-38}{41}\right) = -69.78^\circ$$

