



**Ex:** Find the simplest Sum-Of-Products (SOP) form for the following Boolean expression.

$$A\bar{B} + C \oplus (\bar{A} + B)$$

**SOL'N:** We write the X-OR as an OR of two AND's.

$$A\bar{B} + \bar{C}(\bar{A} + B) + C(\overline{\bar{A} + B})$$

We apply De Morgan's theorem to the last term.

$$A\bar{B} + \bar{C}\bar{A} + \bar{C}B + CAB$$

The first term makes the last term redundant.

$$A\bar{B} + \bar{C}\bar{A} + \bar{C}B$$

Put letters in alphabetical order in each term:

$$\bar{A}\bar{B} + \bar{A}\bar{C} + \bar{B}\bar{C}$$

Now we use the rule that  $A = AB + A\bar{B}$ , etc.

$$\bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + \bar{A}B\bar{C} + \bar{A}BC + A\bar{B}\bar{C} + A\bar{B}C$$

Now we put the terms in order and eliminate duplicates.

$$\bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + \bar{A}B\bar{C} + \bar{A}BC + A\bar{B}\bar{C}$$

Now we use  $A = AB + A\bar{B}$ , etc., in reverse.

$$\bar{C} + A\bar{B}$$

An alternative is to use a truth table:

A	B	C	$A\bar{B}$	$\bar{A} + B$	$C \oplus (\bar{A} + B)$	$A\bar{B} + C \oplus (\bar{A} + B)$
0	0	0	0	1	1	1
0	0	1	0	1	0	0
0	1	0	0	1	1	1
0	1	1	0	1	0	0
1	0	0	1	0	0	1
1	0	1	1	0	1	1
1	1	0	0	1	1	1
1	1	1	0	1	0	0

From the truth table, we see that our previous answer is optimal.

$$\bar{C} + A\bar{B}$$