

TOOL: At a any particular frequency, ω_s , a circuit consisting of only L's and C's is equivalent to a single L or C.

LEMMA: We may place an appropriate L or C in parallel or series with a circuit consisting of only L's and C's to create a resonance at any particular frequency, ω_s .

TOOL: Given an L in series with a C with resonant frequency ω_o , at any particular frequency, ω_s , the L and C are equivalent to:

- 1) A single C if $\omega_s < \omega_o$
- 2) A wire if $\omega_s = \omega_o$
- 3) A single L if $\omega_s > \omega_o$

TOOL: Given an L in parallel with a C with resonant frequency ω_o , at any particular frequency, ω_s , the L and C are equivalent to:

- 1) A single L if $\omega_s < \omega_o$
- 2) An open circuit if $\omega_s = \omega_o$
- 3) A single C if $\omega_s > \omega_o$

COMMENT: A circuit consisting of only L's and C's looks like a single L or C at one frequency, ω_s , because all the impedances are purely imaginary. Thus, the impedance of the entire circuit, z_{tot} , is purely imaginary.

If z_{tot} is positive imaginary, then $z_{tot} = j\omega_s L$ for some L.

If z_{tot} is negative imaginary, then $z_{tot} = -j/(\omega_s C)$ for some C.

TOOL: Summary of LC behavior:

LC	$\omega = 0$	$\omega < \omega_o$	$\omega = \omega_o$	$\omega > \omega_o$	$\omega \rightarrow \infty$
series	-- (open)	$-jX$	— (wire)	jX	-- (open)
parallel	— (wire)	jX	-- (open)	$-jX$	— (wire)