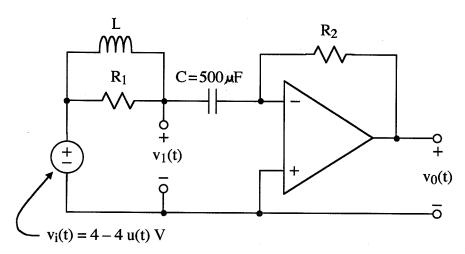
Ex:

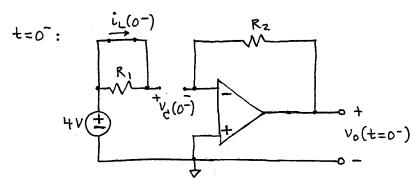


Find a symbolic expression for  $V_0(s)$  in terms of not more than  $R_1$ ,  $R_2$ , L, C, and constants.

Soln: To find the Laplace transformed circuit elements, we first find initial conditions for L and C:  $i_L(o^-)$  and  $v_C(o^-)$ .

For a long time before t=0,  $v_i(t)=4V$ .

For this DC input, the circuit will reach an equilibrium with constant currents and voltages. Thus, derivatives  $di_L/dt$  and  $dv_C/dt$  equal zero. This, in turn, means  $v_L=0$  and  $i_C=0$ . So L= wire and C= open.



The op-amp has negative feedback that acts to keep  $V_- \doteq V_+$ . Thus, we have OV at the inputs of the op-amp.

If we consider a voltage passing through the 4V source, L=wire, C=open, and across the op-amp inputs=OV drop, we have

$$V_{c}(0^{-}) = 4V.$$

Since C = open, we also have

$$i_L(o^-) = oA.$$

Now we Laplace transform the input voltage to obtain a model for the 5-domain.

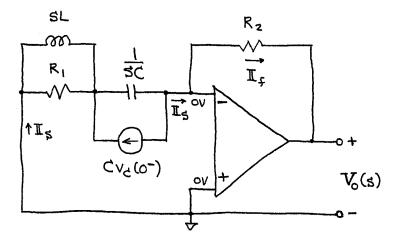
Thus,  $V_i(s) = ov$  which is wire.

Using a parallel current source for initial conditions on the L, we have 0/5 = 0A = 0 pen. Thus, we may leave out this source.

Using a series voltage source for initial conditions on C, we would have 4v/s. Since we have a virtual reference at v\_, however, C is effectively in parallel with R, and C.

Thus, we use a parallel current source for initial conditions on C. The value of the current source is  $Cv_c(o^-) = C \cdot 4V$ . The direction of current is chosen to place charge instantly on C that will yield 4V at time  $O^+$  across C. (Note that, in the time-domain,  $C \cdot 4V$  corresponds to  $C \cdot 4V \cdot 8(t)$ .)

## 5-domain model:



To solve this op-amp circuit, we observe that  $V_{+} = OV$  and  $V_{-} = V_{+} = OV$ .

Since no current flows into the op-amp, we also have  $\mathbb{I}_S$  flowing toward the - in put from the left is the same as current  $\mathbb{I}_S$  flowing in  $R_Z$ . We write equations for  $\mathbb{I}_S$  and  $\mathbb{I}_S$  using  $V_- = 0V$ . Then we set  $\mathbb{I}_S = \mathbb{I}_S$  and solve for  $V_0(S)$ .

We observe that Is is the current flowing in R, and \$L, and we use a current divider egh.

$$I_{s} = -cv_{c}(o^{-}) \frac{1/sc}{1/sc} + R_{1}||_{sL}$$

$$= -cv_{c}(o^{-}) \frac{1}{1+sc} \cdot R_{1}||_{sL}$$

$$= -cv_{c}(o^{-}) \frac{1+R_{1}/sL}{1+R_{1}+sR_{1}c}$$

$$= -cv_{c}(o^{-}) \frac{sL+R_{1}}{sL+R_{1}+s^{2}R_{1}Lc}$$

$$I_{s} = -cv_{c}(o^{-}) \frac{sL+R_{1}}{sL+R_{1}+s^{2}R_{1}Lc}$$

$$I_{s} = -cv_{c}(o^{-}) \frac{1}{sL+R_{1}+s^{2}R_{1}Lc}$$

$$I_{s} = -cv_{c}(o^{-}) \frac{1}{R_{1}c} \cdot \frac{s+R_{1}/L}{s^{2}+L_{1}s+L_{1}}$$
or 
$$I_{s} = -\frac{4v}{R_{1}c} \cdot \frac{s+R_{1}/L}{s^{2}+L_{1}s+L_{1}}$$

For If, we have

$$\mathbb{I}_{f} = \frac{ov - V_{o}(s)}{R_{2}} = -\frac{V_{o}(s)}{R_{2}}$$

Equating Is and If and solving for  $V_o(s)$  yields

$$V_o(s) = -R_2 \mathbb{I}_s$$

$$V_o(s) = 4V \cdot \frac{R_z}{R_1} \cdot \frac{s + R_1/L}{s^2 + \frac{1}{R_1C}} + \frac{1}{LC}$$