

**EX:** A Gilbert cell is an electronic circuit that produces an output voltage that is equal to the product of two input voltages. If the input voltages,  $X$  and  $Y$ , are independent and uniformly distributed on  $[0,3]$ , find the mean of  $Z = XY$ .

**SOL'N:** Since  $X$  and  $Y$  are independent, the mean of the product is the product of the means:

$$\mu_Z = \mu_X \mu_Y$$

The mean of a uniform distribution is its midpoint. Thus, we have the following value for our answer:

$$\mu_Z = \frac{3}{2} \cdot \frac{3}{2} = \frac{9}{4}$$