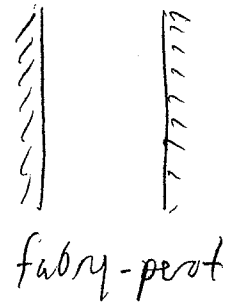


resonators



$$\frac{da}{dt} = (j\omega_0 - \frac{1}{\tau}) a$$

ω_0 = oscillation freq.

τ = lifetime

energy $\propto |a|^2$

$$\frac{d|a|^2}{dt} = 2|a| \frac{d|a|}{dt} = \frac{2}{\tau} |a|^2 \text{ rate of power dissipation}$$

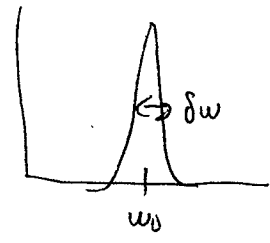
quality factor Q given by $\frac{\text{energy}}{\text{power lost/cycle}}$

$$Q = \frac{|a|^2 \omega_0}{\frac{2}{\tau} |a|^2} = \frac{\tau \omega_0}{2} \quad \omega_0 \tau / 2$$

in freq. domain

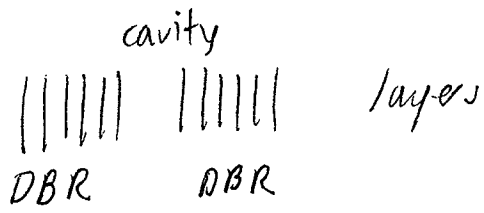
$$Q = \omega_0 / \delta\omega_{1/2}$$

~~$$j\omega a = j\omega_0 a - \frac{a}{\tau}$$~~

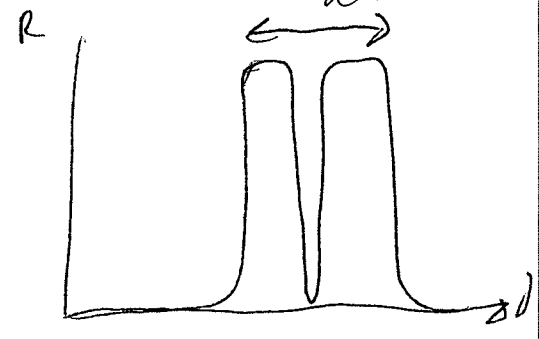
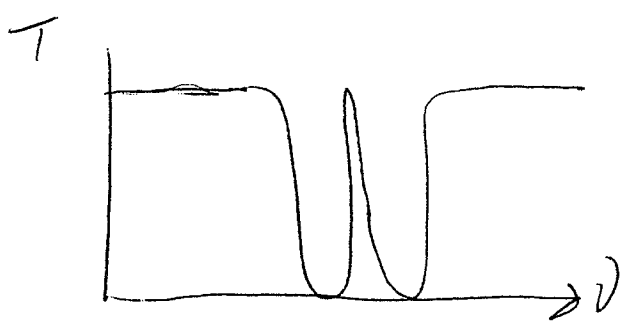
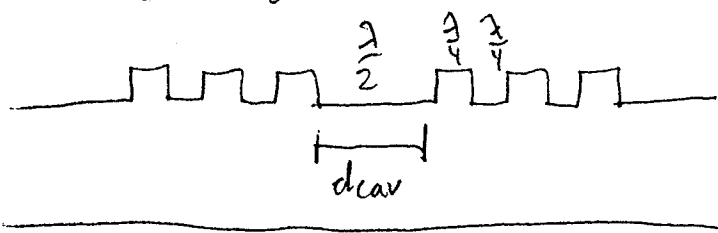


1-D cavity resonators

Fabry-Pérot.



wave guide grating



$$T(\lambda) = \frac{1}{1 + \frac{4R_{DBR}^2}{(1-R_{DBR}^2)} \sin^2 \left| \frac{\pi n_H d_{cav}}{\lambda} - \frac{\pi n_H d_{cav}}{\lambda_0} \right|}$$

λ_0 = design wavelength n_H = cavity effective index

$$Q = \frac{4\pi R_{DBR}}{1-R_{DBR}^2}$$

- homework - 1) direct phase vs. direct ampl. med. MSI (Intel 4/13)
- 2) model Intel via beamprop.
 - 4) calc. qual. factor of r.f., simple method
 - 3) x fe function of $\frac{Q}{\omega}$