

Ex:



For the circuit shown, write three independent equations for the three mesh currents  $i_1$ ,  $i_2$ , and  $i_3$ . The quantity  $v_x$  must not appear in the equations.

**SOL'N:** We first define the variable for the dependent source in terms of mesh currents:

 $v_{\rm x}=(i_1-i_2)R_1$ 

Since the dependent current source is on the outside edge of the circuit,  $i_1$  is equal to  $\alpha v_x$  (but in the opposite direction).

$$i_1 = -\alpha(i_1 - i_2)R_1$$

For  $i_2$  and  $i_3$ , we have a super-mesh. Thus, we take a voltage loop around the outside of the  $i_2$  and  $i_3$  loops. We also write an equation for the  $i_s$  source in terms of  $i_2$  and  $i_3$ .

$$-i_{3}R_{3} - i_{2}R_{1} + i_{1}R_{1} - i_{2}R_{2} - i_{3}R_{4} = 0 V$$
  
$$i_{s} = i_{3} - i_{2}$$