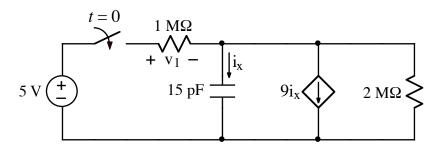
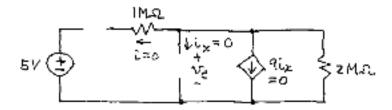
U

Ex:



After being open for a long time, the switch closes at t = 0. Find  $v_1(t)$  for t > 0.

soln:  $t=0^{-}$  model: (to find  $v_{c}(o^{-})$ ) C=open circuit

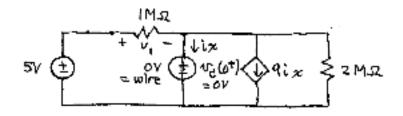


The total current flowing cut of top node eguals zero, and there is no current flowing in the IMD, the C, and the dependent source. It follows that the current in the 2MD is CA. By Ohm's law, the voltage drop across the 2MD is O·2MD = CV. This is also the voltage across the C.

$$v_c(o^-) = 0V$$
and
$$v_c(o^+) = v_c(o^-) = 0V$$

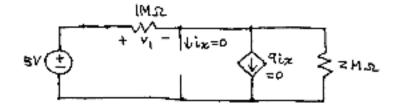
We use this value of  $v_{\sigma}(t=c^{+})$  as a voltage source in the  $t=c^{+}$  model to find  $v_{\tau}(c^{+})$ .

t=c+ model:



From a voltage loop on the left side, we have  $v_1(0^+) = 5V$ . Note: the components to the right of C are in parallel with the circuitry on the left and directly across the same voltage source, (namely oV).

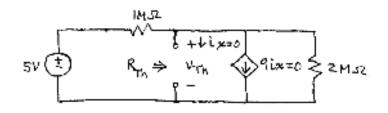
 $t \rightarrow \infty$  model: (to find  $V_1(t \rightarrow \infty)$ ) C=open circ



The dependent are is off and effectively disappears. This leaves a voltage divider:

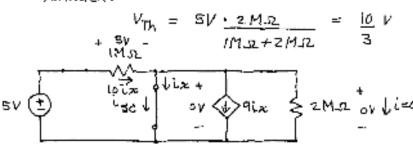
$$V_1(\pm \rightarrow \infty) = 5V \cdot 1M\Omega = 5V$$

Finally, we have  $T = R_{Th} C$  where  $R_{Th}$  is the Therenin equivalent resistance seen looking into the terminals where C is connected.



Because there is a dependent source, we find  $R_{Th}$  from  $R_{Th} = \frac{V_{Th}}{i_{SA}}$ .

 $V_{\text{Th}}$ , as always, equals the voltage across the output terminals when nothing is connected across them. Since  $i_x=0$  and  $9i_x=0$ ,  $v_{\text{Th}}$  is given by a voltage divider formula:



If we short out the output terminals, we have OV across the 2MD resistor.

Thus, there is no current in the 2MD R.

A current summation for the top node reveals that the current in the IMSI must be  $10i_{\times}$ . From a V-loop on the left side, we also have 5V across the IMSI R. Thus, the current in the IMSI R is  $5V/IMSI = 5\mu A$ . Thus, we have

From the schematic diagram, we see that  $i_{SC} = i_{A} = 0.5 \text{ MA}.$ 

$$R_{Th} = \frac{V_{Th}}{\tilde{L}_{SC}} = \frac{10}{3} V = \frac{20}{3} M\Omega$$

$$0.5 \mu A$$

Thus,  $t = R_{Th} c = \frac{20}{3} \text{ M.D. 15pF} = 100 \text{ M.S.}$ 

Using the general form of solution, we have

$$v_{\mathbf{r}}(t) = v_{\mathbf{r}}(t \to \infty) + \left[v_{\mathbf{r}}(t \to 0^{\dagger}) - v_{\mathbf{r}}(t \to \infty)\right] e^{-t/t}$$

$$- t/(\infty) = -t/(\infty)$$

$$\sqrt{1}(t) = \frac{\pi}{2} V + \left[ 5V - \frac{\pi}{2} V \right] e^{-\frac{t}{2} (\alpha A \delta)}, \quad t>0$$

or 
$$V_1(t) = \frac{5}{3}V + \frac{10}{3}Ve$$
 ,  $t > 0$ 

Note: A much simpler way to solve that this problem is to observe the Pix dependent source acts like a capacitor that is 9 times C. Since the C and 9°C are in parallel, we have an equivalent capacitance of  $10C = 10 \cdot 15 \, \text{pF} = 150 \, \text{pF}$ . The dependent source is now gone, and the soln is easier to find. The solution, of course is the same as above. Rin C is the same, but Rin = 1Ms2 | 2Ms2 and C=150 \text{pF}.

V<sub>1</sub>(0+) and V<sub>1</sub>(t+m) are the same as before.