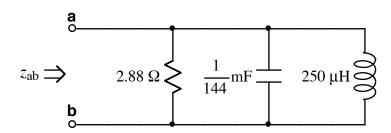
U

Ex:



Find a frequency, ω , that causes z_{ab} to have a phase angle of -45° , (i.e., imaginary part is the negative of the real part). Hint: use admittance, (the reciprocal of impedance).

sol'n: For single components in parallel, using admittance = 1/2 is helpful.

$$\frac{1}{z_{ab}} = \frac{1}{z_{R}} + \frac{1}{z_{d}} + \frac{1}{z_{d}}$$

Here, we have
$$\geq_{c} = \frac{1}{j\omega c} = -\frac{j}{\omega c}$$

$$= \frac{-j}{\omega \cdot 1} = -\frac{j}{\omega}$$
144m

If $\angle Z_{ab} = -45^\circ$, then $Z_{ab} = k(1-j)$ where k is a positive real number.

Then
$$\frac{1}{z_{ib}} = \frac{1}{k(1-j)} \approx \frac{1+j}{k(1-j)(1+j)} = \frac{1+j}{2k}$$
.

Thus,
$$\angle \frac{1}{2ab} = 45^{\circ}$$
 and $Re\left[\frac{1}{2ab}\right] = Im\left[\frac{1}{2ab}\right]$.

We observe that the values of 1 and 1 are pure imaginary 2 21

and constitute the entire imaginary part of 1 : 2ab

$$Im \left[\frac{1}{2ab} \right] = Im \left[\frac{1}{2a} + \frac{1}{2a} \right]$$

$$= Im \left[j\omega c + \frac{1}{j\omega L} \right]$$

$$= Im \left[j\omega c - \frac{j}{\omega L} \right]$$

$$= \omega c - \frac{1}{ab}$$

$$= \omega c + \frac{1}{ab}$$

Note: Im [] had a <u>real</u> value. Im [a+jb] = b rather than jb.

The real part of \mathbb{Z}_{ab} consists entirely of \mathbb{L} :

$$Re\left[\frac{1}{e_{q}}\right] = Re\left[\frac{1}{R}\right] = \frac{1}{R}$$

Now we solve $Re\left[\frac{1}{2ab}\right] = Im\left[\frac{1}{2ab}\right]$ or $\frac{1}{R} = \omega C + \frac{1}{\omega L}$.

or
$$\frac{1}{RC}\omega = \omega^2 - \frac{1}{LC}$$

or $\omega^2 - \frac{1}{RC}\omega - \frac{1}{LC} = 0$

or $\omega = \frac{1}{2RC} \pm \sqrt{\frac{1}{2RC}^2 + \frac{1}{LC}}$

Note: since w>0, we use only +1-1.

$$\omega = \frac{1}{2RC} + \sqrt{\left(\frac{1}{2RC}\right)^2 + \frac{1}{LC}}$$

Now we calculate values.

$$\frac{1}{2RC} = \frac{1}{2(z.88)} \frac{1m}{1m} s = \frac{1k \cdot 1k}{2(z.88k)} s$$

$$\frac{1}{2RC} = \frac{1M}{40s} = 25k/s$$

$$\frac{1}{2RC} = \frac{1}{40s} = 25k/s$$

$$\frac{1}{40s} = \frac{1}{40s} = \frac{1}{4$$

Using values, we have the following:

$$\omega = 25 k/s + \sqrt{(25k/s)^2 + (24k/s)^2}$$