

Rail voltages = ±10 V

- The above circuit operates in linear mode. Derive a symbolic expression for  $v_o$ . The expression must contain not more than the parameters  $i_{s1}$ ,  $i_{s2}$ ,  $R_1$ ,  $R_2$ , and  $R_3$ .
- If  $i_{s1} = 0 \mu\text{A}$ , find the value of  $R_3$  that will yield an output voltage of  $v_o = 1 \text{ V}$  when  $i_{s2} = 10 \mu\text{A}$ .
- Derive a symbolic expression for  $v_o$  in terms of common mode and differential input currents:

$$i_{\Sigma} \equiv \frac{i_{s1} + i_{s2}}{2} \quad \text{and} \quad i_{\Delta} \equiv \frac{i_{s1} - i_{s2}}{2}$$

The expression must contain not more than the parameters  $i_{\Sigma}$ ,  $i_{\Delta}$ ,  $R_1$ ,  $R_2$ , and  $R_3$ . Write the expression as  $i_{\Sigma}$  times a term plus  $i_{\Delta}$  times a term. Hint: start by writing  $i_{s1}$  and  $i_{s2}$  in terms of  $i_{\Sigma}$  and  $i_{\Delta}$ :

$$i_{s1} \equiv i_{\Sigma} + i_{\Delta} \quad \text{and} \quad i_{s2} \equiv i_{\Sigma} - i_{\Delta}$$

$R_{in} = \frac{V_x}{i_{s2}}$

- If  $i_{\Delta} = 0$  and  $R_1 = R_2$ , write a formula for the current flowing from left to right in  $R_3$  as a function of not more (and possibly less) than the following terms:  $i_{\Sigma}$ ,  $R_1$ ,  $R_2$ , and  $R_3$ .

---

sol'n: a) First, we find  $v_p$  (voltage at + input):

$$v_p = i_{s2} R_2$$

Second, we find the current flowing toward the - input from the left, using  $v_n$  (voltage at - input) =  $v_p$ :

$$i_l = i_{s1} - \frac{v_n}{R_1} = i_{s1} - \frac{i_{s2} R_2}{R_1}$$

Third, we find the current flowing in the feedback resistor,  $R_3$ , from left to right:

$$i_r = \frac{v_n - v_o}{R_3} = \frac{i_{s2} R_2 - v_o}{R_3}$$

Fourth, we set  $i_r = i_l$  and solve for  $v_o$ :

$$i_{s1} - \frac{i_{s2} R_2}{R_1} = \frac{i_{s2} R_2 - v_o}{R_3}$$

or 
$$v_o = -i_{s1} R_3 + i_{s2} R_2 \left(1 + \frac{R_3}{R_1}\right)$$

b) 
$$1V = 10\mu A \cdot 2k\Omega \left(1 + \frac{R_3}{2k\Omega}\right) = 20mV \left(1 + \frac{R_3}{2k\Omega}\right)$$

$$\therefore 1 + \frac{R_3}{2k\Omega} = 50 \quad \text{or} \quad \frac{R_3}{2k\Omega} = 49$$

or 
$$R_3 = 98 k\Omega$$

---


$$c) \quad v_o = -(i_\Sigma + i_\Delta) R_3 + (i_\Sigma - i_\Delta) R_2 \left(1 + \frac{R_3}{R_1}\right)$$

or

$$v_o = i_\Sigma \left( R_2 + \frac{R_2 R_3}{R_1} - R_3 \right) - i_\Delta \left( R_2 + \frac{R_2 R_3}{R_1} + R_3 \right)$$

d) For  $i_\Delta = 0$  and  $R_1 = R_2$ , we have

$$v_o = i_\Sigma \left( R_2 + \frac{R_2 R_3}{R_1} - R_3 \right)$$

or  $v_o = i_\Sigma R_2$

Then  $i_{R3} = \frac{v_n - v_o}{R_3} = \frac{v_n - i_\Sigma R_2}{R_3}$

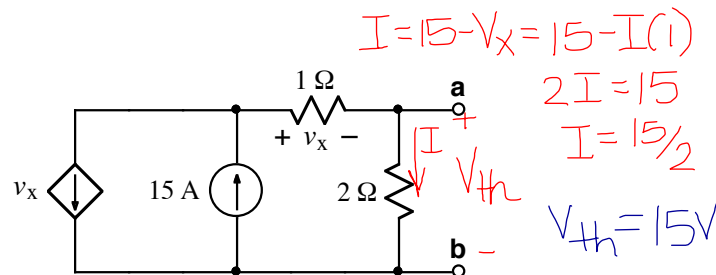
But  $v_n = v_p = i_{s2} R_2 = \frac{i_{s1} + i_{s2}}{2} R_2$

(since  $i_{s1} = i_{s2}$ )  $= i_\Sigma R_2$

Then  $i_{R3} = \frac{i_\Sigma R_2 - i_\Sigma R_2}{R_3} = 0 \text{ A}$

Note: When  $i_{s1} = i_{s2}$ , the current in  $R_1$  and  $R_2$  is the same (since  $v_n = v_p$ ), so there is no current left over to flow in  $R_3$ .

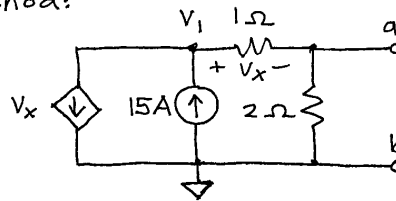
Ex:



- Find the Thevenin equivalent of the above circuit relative to terminals **a** and **b**.
- If we attach  $R_L$  to terminals **a** and **b**, find the value of  $R_L$  that will absorb maximum power.
- Calculate the value of that maximum power absorbed by  $R_L$ .

sol'n: a)  $V_{Th} = V_{a,b}$  with nothing connected across  $a,b$

One approach is to use the node-voltage method:



Using the voltage-divider formula, we relate  $v_x$  to  $v_1$ :

$$v_x = v_1 \cdot \frac{1\Omega}{1\Omega + 2\Omega} = \frac{v_1}{3}$$

Node  $v_1$  eq'n:

$$\frac{v_1}{3} - 15A + \frac{v_1}{1\Omega + 2\Omega} = 0A$$

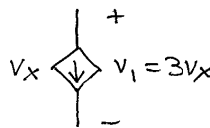
$$\text{or } \frac{2V_1}{3\Omega} = 15A$$

$$\text{or } V_1 = \frac{3\Omega \cdot 15A}{2} = 22.5V$$

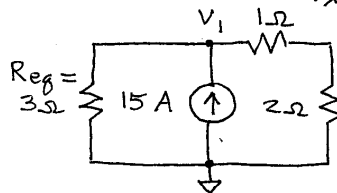
To find  $V_{Th}$ , we again use a voltage-divider formula:

$$V_{Th} = V_1 \cdot \frac{2\Omega}{1\Omega + 2\Omega} = 22.5V \cdot \frac{2}{3} = 15V$$

Note: Another approach is to replace the dependent source with a resistor. To do so, we write the voltage across the dependent source in terms of dependent variable  $V_x$ . From an eq'n above, we have  $V_1 = 3V_x$ .



$$R_{eq} = \frac{V}{i} = \frac{3V_x}{V_x} = 3\Omega$$



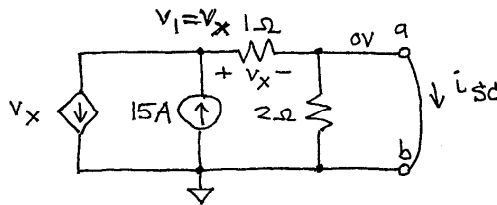
$$V_1 = 15A \cdot 3\Omega \parallel 3\Omega = 22.5V$$

Note:  $R_{eq}$  changes with  $R$  across  $a, b$ .

One way to find  $R_{Th}$  is to use

$$R_{Th} = \frac{V_{Th}}{i_{sc}}$$

where  $i_{sc} \equiv$  short circuit from **a** to **b**



We may ignore the  $2\Omega$  resistor that is shorted out.

Node  $v_1$  eq'n: (Note that  $v_x = v_1$ .)

$$v_1 - 15A + \frac{v_1}{1.5} = 0A$$

or

$$\frac{2v_1}{1.5} = 15A$$

or

$$v_1 = 15A \cdot \frac{1.5}{2} = 7.5V$$

$$\text{Our current is } i_{sc} = \frac{v_1}{1.5} = \frac{7.5V}{1.5} = 7.5A.$$

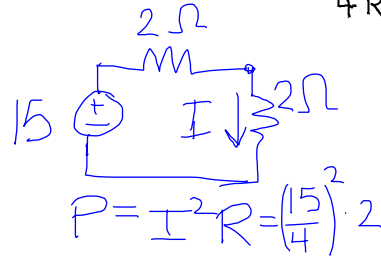
$$R_{Th} = \frac{V_{Th}}{i_{sc}} = \frac{15V}{7.5A} = 2\Omega$$

Note: we could replace the dependent source with  $R_{eq} = \frac{V}{i} = \frac{v_x}{v_x} = 1.5\Omega$  for  $i_{sc}$ .

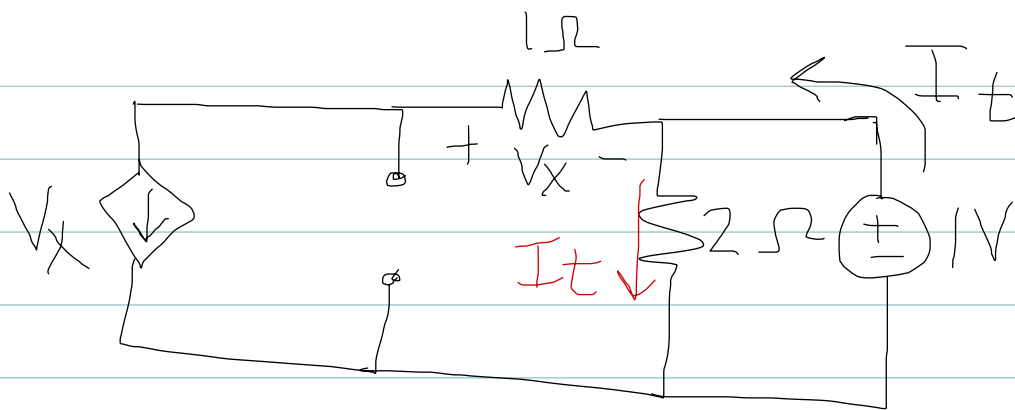
---

b)  $R_L = R_{Th} = 2\Omega$  for max pwr xfer

c)  $P_{max} = \frac{V_{Th}^2}{4R_{Th}} = \frac{15^2}{4 \cdot 2\Omega} = 28.125 \text{ W}$



$$P = I^2 R = \left(\frac{15}{4}\right)^2 \cdot 2$$



$$V_x = -V_x (1)$$

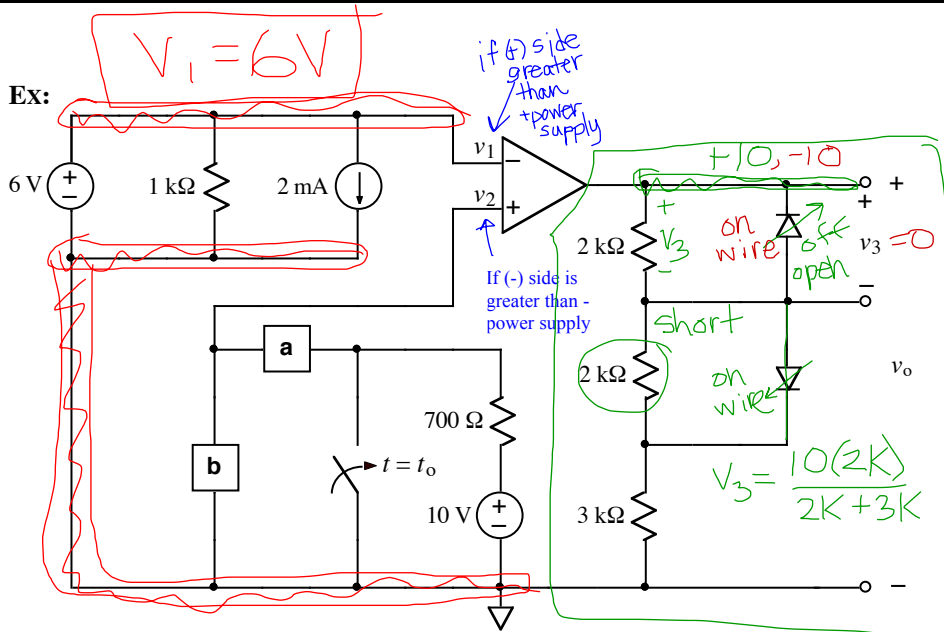
$$I_t = \frac{1}{2}$$

$$2V_x = 0$$

$$V_x = 0$$

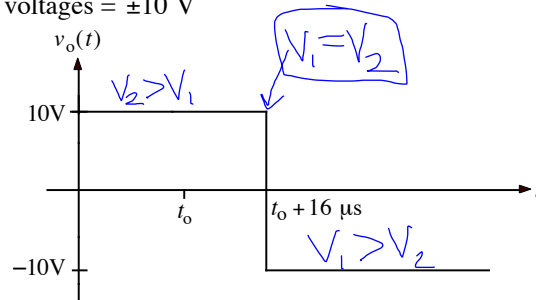
$$R_{th} = 2$$





After being open for a long time, the switch closes at time  $t = t_0$ .

Rail voltages =  $\pm 10$  V



- Choose either an  $R$  or  $L$  to go in box **a** and either an  $R$  or  $L$  to go in box **b** to produce the  $v_o(t)$  shown above. (You will need one  $R$  and one  $L$ . Use an  $R$  value of  $1.3 \text{ k}\Omega$ . Also, note that  $v_o$  stays low forever after  $t_0 + 16 \mu\text{s}$ .) Specify which element goes in each box and its value.
- Sketch  $v_1(t)$ , showing numerical values appropriately.
- Sketch  $v_2(t)$ , showing numerical values appropriately.
- Sketch  $v_3(t)$ . Show numerical values for  $t < t_0$ , for  $t_0 < t < t_0 + 16 \mu\text{s}$ , and for  $t > t_0 + 16 \mu\text{s}$ . Use the ideal model of the diode: when forward biased, its resistance is zero; when reverse biased, its resistance is infinite.

---

sol'n: a) We first find  $v_1$ , which is constant. The  $1k\Omega$  resistor and  $2mA$  source are across the  $6V$  source. Because they are across the  $6V$  source, they may be ignored.  $v_1 = 6V$  regardless of what is across the  $6V$  source.

$$v_1 = 6V$$

For boxes **a** and **b**, we observe that, if we had an  $L$  in **b**, that  $L$  will act like a wire at  $t=0^-$ . This would make  $v_2(0^-) = 0V$ . The op-amp acts like a comparator, with the output equal to  $\pm 10V$  according to the sign of  $v_2 - v_1$ . For  $v_2 = 0V$  and  $v_1 = 6V$  we would have  $v_2 - v_1 = 0 - 6V = -6V$  and  $v_o = -10V$  at  $t=0^-$ . This differs from the plot of  $v_o(t)$  given in the problem statement. Thus, **b** must contain an  $R$  rather than an  $L$ .

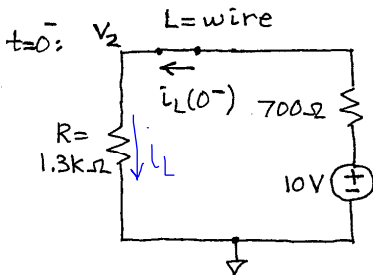
Because the output voltage,  $v_o(t)$ , changes  $16\mu s$  after the switch moves, box **a** must contain an  $L$  to give the circuit a time-varying behavior.

$$a = L$$

$$b = R \approx 1.3k \text{ (from prob statement)}$$

At  $t=0^-$ , we have the following equivalent circuit:

$a=L$   
 $b=R$



$$i_L(0^-) = \frac{10V}{1.3k\Omega + 700\Omega}$$

$$i_L(0^-) = 5\text{mA}$$

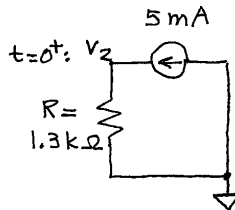
This is a voltage divider.

$$v_2(0^-) = 10V \cdot \frac{1.3k\Omega}{1.3k\Omega + 700\Omega} = 6.5V$$

We note that  $v_2(0^-) = 6.5 > v_1(0^-) = 6V$   
and  $v_2 - v_1 = 6.5 - 6V = 0.5V > 0V$  so  
 $v_o(0^-) = +10V$ , as desired.

Initial  
Value

At  $t=0^+$ , we have the following equivalent circuit:



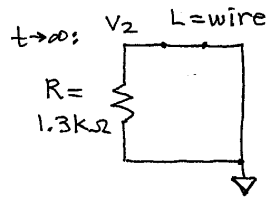
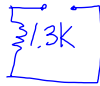
$$v_2(0^+) = 5\text{mA} \cdot 1.3k\Omega$$

$$v_2(0^+) = 6.5V \quad v_2 > v_1 \checkmark$$

At  $t=0^+$ ,  $v_2 - v_1 = 6.5V - 6V = 0.5V > 0V$   
so  $v_o(0^+) = +10V$ , as desired.

As  $t \rightarrow \infty$ , we have the following equivalent circuit:

$$V_2 = 0 + (6.5 - 0)e^{-t/\tau}$$



Since there is no power source,  
 $V_2(t \rightarrow \infty) = 0V$

$$V_1 > V_2 \checkmark$$

The time constant of the circuit is

$$\tau = \frac{L}{R_{Th}} = \frac{L}{1.3k\Omega}$$

Using the general form of solution for RL circuits, we write an expression for  $V_2(t > 0)$ :

$$V_2(t > 0) = V_2(t \rightarrow \infty) + [V_2(0^+) - V_2(t \rightarrow \infty)]e^{-t/\tau}$$

$$\text{or } V_2(t > 0) = 0V + [6.5V - 0V]e^{-t/\tau}$$

$$\text{or } V_2(t > 0) = 6.5V e^{-t/\tau}$$

The op-amp output switches from high to low when  $V_2(t) = V_1 = 6V$ , which must occur at  $t = t_0 + 16\mu s$ .

Setting  $t_0 = 0$ , we solve for  $L$  in  $V_1 = V_2$  at  $t = 16\mu s$ .

$$6V = 6.5V e^{-16\mu s / \tau}$$

$$\text{or } \ln(6/6.5) = -16\mu s / \tau$$

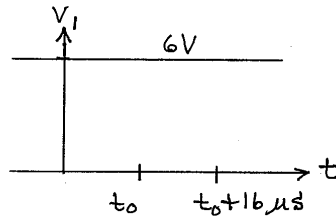
$$\text{or } \tau = \frac{-16 \mu\text{s}}{\ln(6/6.5)} \doteq 200 \mu\text{s}$$

$$L = \tau \cdot R_{Th} = 200 \mu\text{s} \cdot 1.3 \text{ k}\Omega = 260 \text{ mH}$$

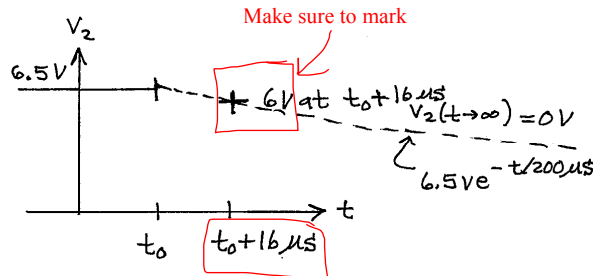
$$R = 1.3 \text{ k}\Omega$$

$$L = 260 \text{ mH}$$

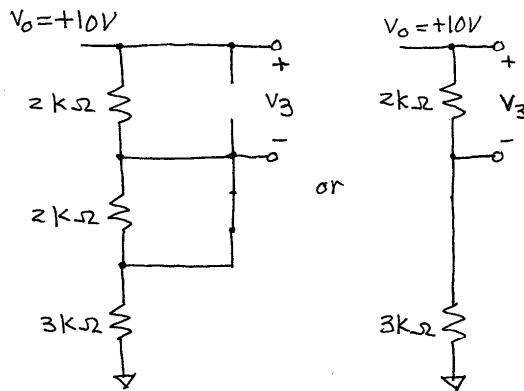
b) From above,  $v_1(t) = 6V$  at all times



c) From above,  $v_2(0^-) = 6.5V$  and  $v_2(t > 0) = 6.5 e^{-t/200 \mu\text{s}}$  V  
 Also,  $v_2(t = 16 \mu\text{s}) = v_1 = 6V$



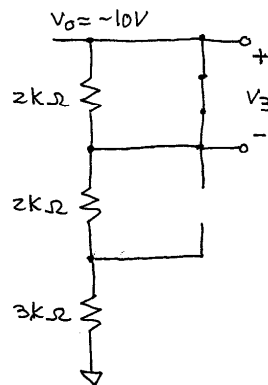
d) When  $V_0 = +10V$ , the equivalent circuit on the right side is as follows:



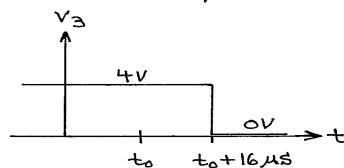
We have a voltage divider:  $V_3 = \frac{10V \cdot 2k\Omega}{2k\Omega + 3k\Omega}$

$$V_3 = 4V$$

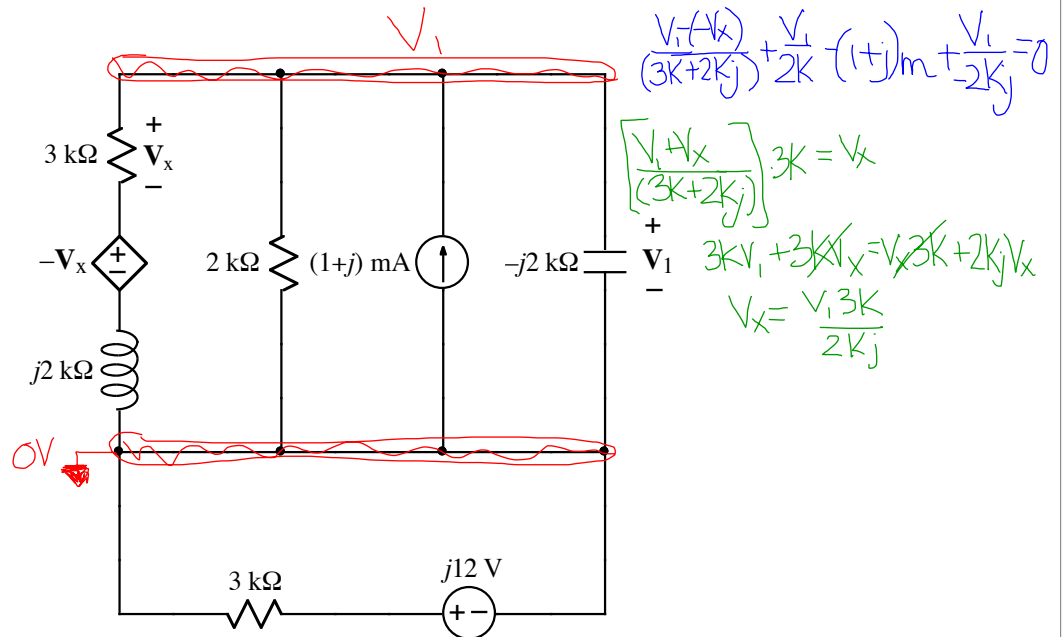
When  $V_0 = -10V$ , the equivalent circuit on the right side is as follows:



Since we have a short across  $V_3$ ,  $V_3 = 0V$ .



Ex:

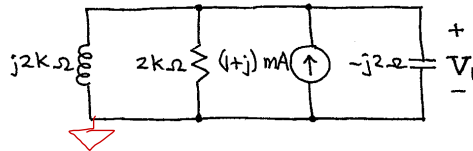


- A frequency-domain circuit is shown above. Write the value of phasor voltage  $V_1$  in rectangular form.
- Given  $\omega = 500$  rad/s, write a numerical time-domain expression for  $v_1(t)$ , the inverse phasor of  $V_1$ .

sol'n: a) The dependent-source voltage cancels out the voltage across the  $3k\Omega$  resistor, yielding the equivalent of a wire, (i.e.  $0V$ ).

We may also ignore the bottom part of the circuit, which is shorted out by the middle wire.

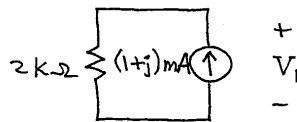
Thus far, we have the following circuit:



Now we observe that the  $j2k\Omega$  and  $-j2k\Omega$  in parallel are equivalent to an open circuit:

$$j2k\Omega \parallel -j2k\Omega = j2k\Omega \cdot \frac{1}{-1} = \frac{j2k\Omega \cdot -1}{0} = \infty\Omega$$

Thus, the L and C disappear:



Now we use Ohm's Law:

$$V_1 = (1+j) \text{ mA} \cdot 2k\Omega = 2+j2 \text{ V}$$

- b) In polar form,  $V_1 = 2\sqrt{2} \angle 45^\circ \text{ V}$   
 In the time domain, we have

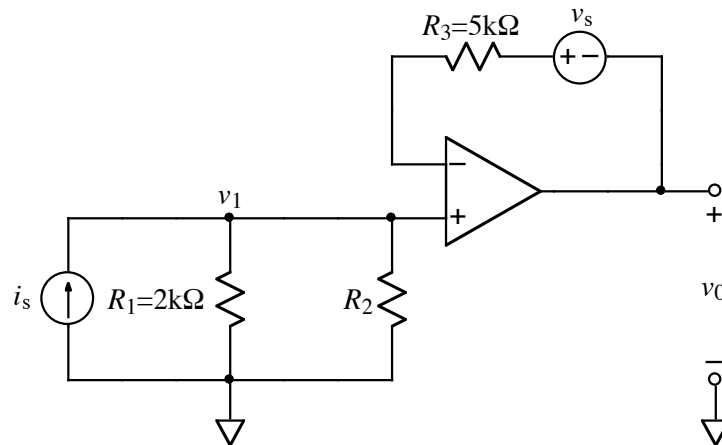
$$V_1(t) = 2\sqrt{2} \cos(500t + 45^\circ) \text{ V}$$

Note: We could also directly take the inverse phasor of  $2+j2\text{V}$ :

$$V_1(t) = 2\cos(500t) - 2\sin(500t) \text{ V}$$



Ex:



Rail voltage =  $\pm 9$  V

- The above circuit operates in linear mode. Derive a symbolic expression for  $v_o$ . The expression must contain not more than the parameters  $i_s$ ,  $v_s$ ,  $R_1$ ,  $R_2$ , and  $R_3$ .
- If  $v_s = 0$  V, find the value of  $R_2$  that will yield an output voltage of  $v_o = 1$  V when  $i_s = 1$  mA.
- Using the value of  $R_2$  from part (a), find the value of  $v_s$  that will yield  $v_o = 1$  V when  $i_s = 0$  A.
- Using the value of  $R_2$  from part (a), calculate the input resistance,  $R_{in} = v_1/i_s$ , seen by the  $i_s$  source.

sol'n: a) First, we find the voltage,  $v_1$ , at the + input of the op-amp.

$$v_1 = i_s \cdot R_1 \parallel R_2$$

Second, we assume the voltage,  $v_n$ , at the - input of the op-amp =  $v_1$

---

$$V_n = i_s \cdot R_1 \parallel R_2$$

Third, we find the value of  $V_o$  that yields the above value of  $V_n$ .

Since no current flows into the op-amp inputs, no current flows in  $R_3$ , and  $R_3$  has no voltage drop.

$$\therefore V_o = V_n - V_s$$

$$\text{or } V_o = i_s \cdot R_1 \parallel R_2 - V_s$$

- b) Given  $V_s = 0V$  and  $i_s = 1mA$  we are to find the value of  $R_2$  that yields  $V_o = 1V$ .

Using the expression in (a) for  $V_o$  we have

$$1V = 1mA \cdot 2k\Omega \parallel R_2 - 0V$$

$$\text{or } 2k\Omega \parallel R_2 = 1k\Omega$$

$$\text{or } R_2 = 2k\Omega$$

- c) We have  $1V = 0A \cdot \cancel{2k\Omega} \parallel 2k\Omega - V_s$

$$\text{or } V_s = -1V$$

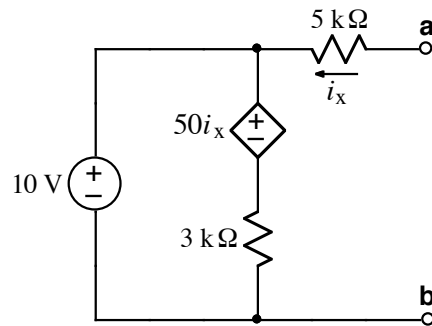
---

d) From part (a), we have the following:

$$v_1 = i_s \cdot R_1 \parallel R_2$$

$$R_{in} \equiv \frac{v_1}{i_s} = R_1 \parallel R_2 = 1k\Omega$$

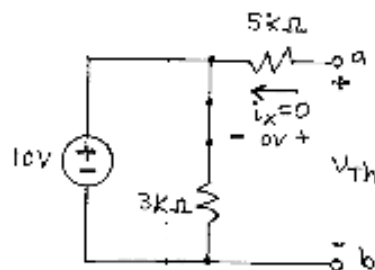
Ex:



- Find the Thevenin equivalent of the above circuit relative to terminals **a** and **b**.
- If we attach  $R_L$  to terminals **a** and **b**, find the value of  $R_L$  that will absorb maximum power.
- Calculate the value of that maximum power absorbed by  $R_L$ .

sol'n: a)  $V_{TH} = V_{a,b}$  no load

With nothing connected from **a** to **b**,  
 $i_x = 0$  and  $50i_x = 0V$  acts like a wire

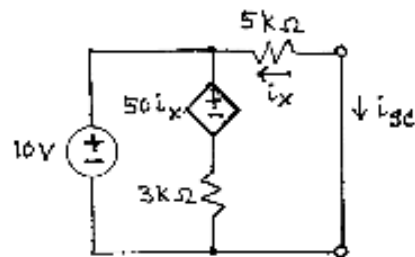


Since  $i_x = 0$ , there is no  $v$ -drop across the  $5\text{ k}\Omega$  resistor. An outer voltage loop reveals that  $V_{TH} = 10V$ .

---

Because we have a dependent source, we can find  $R_{Th}$  using the formula

$$R_{Th} = \frac{V_{Th}}{i_{sc}}$$



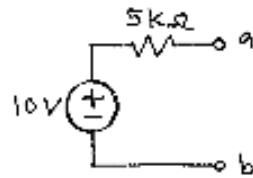
Although we have a dependent source, the 10V source between the top and bottom rails makes the  $50i_x$  and  $3k\Omega$  components irrelevant.

From an outer  $v$ -loop, we have

$$i_{sc} = \frac{10V}{5k\Omega} = 2mA$$

$$\therefore R_{Th} = \frac{V_{Th}}{i_{sc}} = \frac{10V}{2mA} = 5k\Omega$$

Note: The 10V source across the rails allows to ignore the  $50i_x$  and  $3k\Omega$ . We may remove them. Then we observe that we are left with the Thevenin equivalent circuit:  $V_{Th} = 10V$ ,  $R_{Th} = 5k\Omega$ .

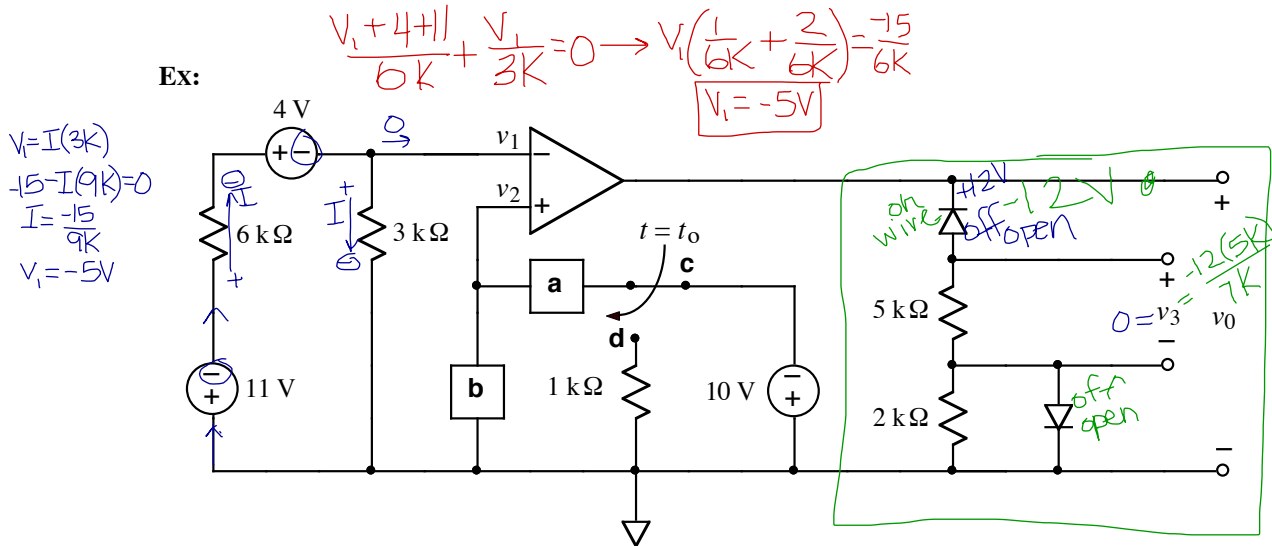


b)  $R_L = R_{Th} = 5k\Omega$  for max power transfer

c) 
$$P_{max} = \frac{V_{Th}^2}{4R_{Th}} = \frac{(10V)^2}{4 \cdot 5k\Omega} = \frac{100}{20} \text{ mW}$$

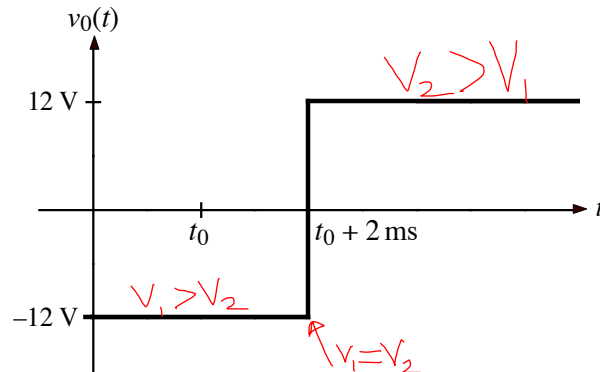
$$P_{max} = 5 \text{ mW}$$

Ex:



After being in position **c** for a long time, the switch moves from **c** to **d** at  $t = t_0$ .

Rail voltages =  $\pm 12$  V



- Choose either an  $R$  or  $C$  to go in box **a** and either an  $R$  or  $C$  to go in box **b** to produce the  $v_0(t)$  shown above. (Note that  $v_0$  stays high forever after  $t_0 + 2$  ms.) Specify which element goes in each box and its value.
- Sketch  $v_1(t)$ , showing numerical values appropriately.
- Sketch  $v_2(t)$ , showing numerical values appropriately.
- Sketch  $v_3(t)$ . Show numerical values for  $t < t_0$ , for  $t_0 < t < t_0 + 2$  ms, and for  $t_0 + 2$  ms  $< t$ . Use the ideal model of the diode: when forward biased, its resistance is zero; when reverse biased, its resistance is infinite.

---

Sol'n: a) For  $v_o$  to be low, (i.e.,  $-12V$ ), we must have  $v_2 < v_1$ .

To find  $v_1$ , we slide the  $4V$  source through the  $6k\Omega$  resistor and find that we have the equivalent of a  $-15V$  source and a voltage divider formed by the  $3k\Omega$  and  $6k\Omega$  resistors.

$$v_1 = -15V \cdot \frac{3k\Omega}{3k\Omega + 6k\Omega} = -5V$$

At  $t=0^-$ , we must have  $v_2 < -5V$ .

a=R  
b=C [ This is possible only if box **a** contains a resistor and box **b** contains a capacitor. If **a** is an R and **b** is a C, then the C will charge until  $v_2 = -10V < v_1$ .

When the switch moves from **c** to **d**, the capacitor voltage starts charging toward  $0V$ , but it will still be  $-10V$  initially. This gives the desired waveform for  $v_o(t)$ :  $v_o$  will go high when  $v_2 = v_1 = -5V$ .

Note: The reasons why other components in boxes **a** and **b** fail to yield the desired  $v_o(t)$  are as follows:



---

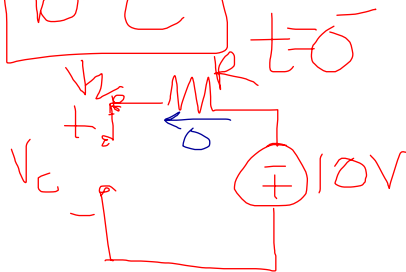
$a = R$  and  $b = R$  cannot give a waveform that changes after a delay.  $v_o$  would have to change instantly at  $t = t_0$ .

$a = C$  and  $b = R$  would result in  $C$  charging until no current flows in  $R$ . This means  $v_2 = 0V$ , or  $v_2 > v_1$ , causing  $v_o$  to be high before  $t = t_0$ .

$a = C$  and  $b = C$  would result in an arbitrary voltage at  $v_2$ . The total voltage drop across the two  $C$ 's would be  $10V$ . When the switch changes from  $c$  to  $d$ , the capacitors would charge until the total voltage drop across them was  $0V$ . The same current would flow in both  $C$ 's, causing a voltage change that would be inversely proportional to the  $C$  values. The waveform shown for  $v_o(t)$  could be produced, but there is a lack of control over the initial value of  $v_2$ . This would make the timing of the  $v_o(t)$  waveform uncertain. Thus, we reject this solution.

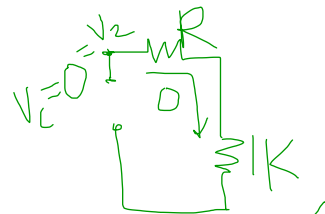
$$\boxed{a=R}$$

$$\boxed{b=C}$$



$$V_c = V_2 = -10V$$

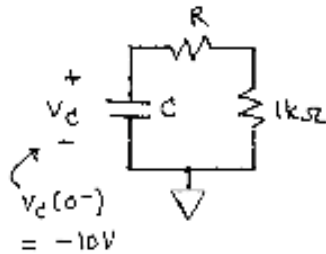
$$\checkmark V_1 = -5 > V_2 = -10V$$



$$V_2 > V_1 \checkmark$$

$\tau$  found at final

Now we find possible values for  $R$  and  $C$ . We have the following circuit model for  $t > t_0$ :



$$V_c(0^-) = -10V$$

$$V_c(t > t_0) = V_c(t \rightarrow \infty) + \left[ V_c(t_0^+) - V_c(t \rightarrow \infty) \right] e^{-t/\tau}$$

$$\begin{matrix} \parallel & \parallel & \parallel \\ 0V & -10V & 0V \end{matrix}$$

$$V_c(t > t_0) = -10 e^{-t/\tau} \quad \text{(where we take } t_0 = 0)$$

$$\text{where } \tau = (R + 1k\Omega) C$$

$$\text{We want } V_c(t = 2ms) = V_1 = -5V$$

$$\text{or } -10 e^{-2ms/\tau} = -5V$$

$$e^{-2ms/\tau} = \frac{1}{2}$$

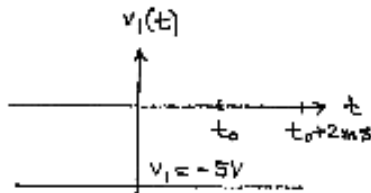
$$-2ms = \tau \ln \frac{1}{2}$$

$$\tau = \frac{2ms}{\ln 2} \doteq 2.9ms$$

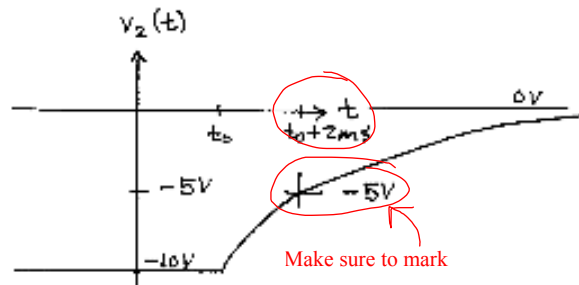
One sol'n is  $R = 1.9k\Omega$  and  $C = 1\mu F$ .

Note:  $R = 0\Omega$  is min  $R$ ,  $C = 2.9\mu F$  is max  $C$ .

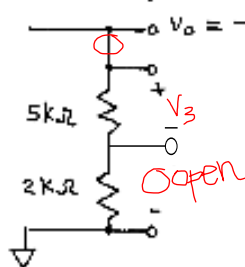
b)  $v_1(t) = -5V$  as shown earlier.



c)  $v_2 = v_c(t > 0) = -10V e^{-t/2.9ms}$  from (a)



d) When  $v_o$  is low, the top diode will act like a wire and the bottom diode will act like an open circuit.

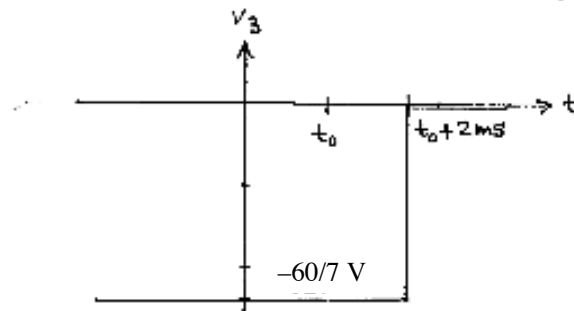


We have a voltage divider:  $v_3 = -12V \cdot \frac{5k\Omega}{2k\Omega + 5k\Omega} = -\frac{60}{7}V$ .

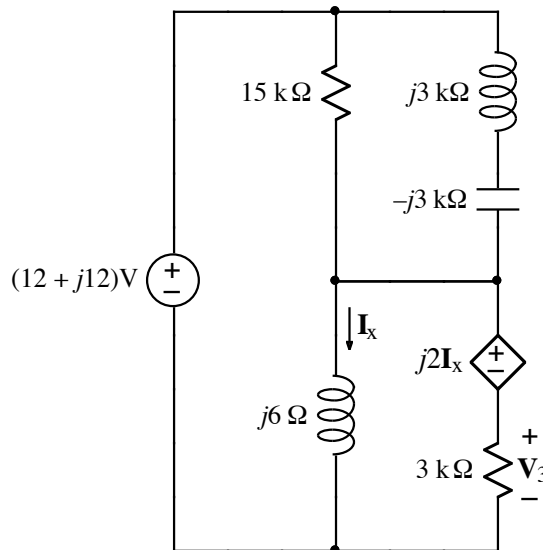
---

When  $v_o$  is high, the top diode will act like an open circuit, leaving the bottom part of the circuit disconnected from  $v_o$ , (or any other power source).

Thus  $v_3 = 0V$  when  $v_o$  is high.



Ex:



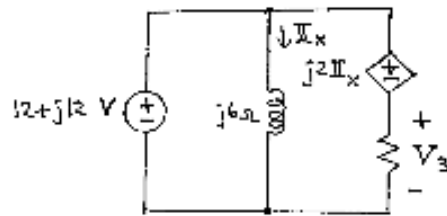
- A frequency-domain circuit is shown above. Write the value of phasor  $V_3$  in polar form.
- Given  $\omega = 37$  rad/s, write a numerical time-domain expression for  $v_3(t)$ , the inverse phasor of  $V_3$ .

sol'n: a) The  $j3k\Omega$  and  $-j3k\Omega$  sum to  $0\Omega = \text{wire}$ .

Thus, the  $15k\Omega$  is bypassed by a short and may be ignored.

It also follows that the  $12+j12$  V is directly across the  $j6\Omega$  and directly across the  $j2I_x$  source in series with the  $3k\Omega$  resistor.

Our circuit model is as follows:



By Ohm's law,  $I_x = \frac{12 + j12}{j6} = \frac{2(1+j)}{j}$  A

or  $I_x = -j2(1+j)$  A

or  $I_x = 2 - j2$  A

It follows that  $j2I_x = j2(2 - j2) = 4 + j4$  V.

From a v-loop around the outside of the circuit, we have the following:

$$V_3 = (12 + j12) - (4 + j4)$$

or  $V_3 = 8 + j8$  V

or  $V_3 = 8\sqrt{2} \angle 45^\circ$  V



b)  $v_3(t) = P^{-1} [8\sqrt{2} \angle 45^\circ \text{ V}], \quad \omega = 37 \text{ rad/s}$

$$v_3(t) = 8\sqrt{2} \cos(37t + 45^\circ) \text{ V}$$