## ECE 2210 / 00 Capacitor Lecture Notes

Now that we have voltages and currents which can be functions of time, it's time to introduce the capacitor and the inductor.

Electrical equivalent:


$$
C=\varepsilon \cdot \frac{A}{d}=\frac{Q}{V}=\frac{d q}{d v}
$$

$$
\mathcal{V}^{\mathrm{i}} \mathrm{C} \begin{aligned}
& \text { flow is like } \\
& \text { current }
\end{aligned}
$$

Units: $\quad$ farad $=\frac{\text { coul }}{\text { volt }}=\frac{\mathrm{amp} \cdot \mathrm{sec}}{\mathrm{volt}}$
$\mu \mathrm{F}=1 \cdot 10^{-6} \cdot$ farad
Fluid Model:
A. Stolp 2/17/03

$$
\mathrm{pF}=1 \cdot 10^{-12} \cdot \text { farad }
$$

For drawings of capacitors and info about tolerances, see Ch. 3 of textbook.

Basic equations
you should know:

$$
\begin{aligned}
\mathrm{C} & =\frac{\mathrm{Q}}{\mathrm{~V}} \\
\mathrm{i}_{\mathrm{C}} & =\mathrm{C} \cdot \frac{\mathrm{~d}}{\mathrm{dt}} \mathrm{v}_{\mathrm{V}} \mathrm{C}
\end{aligned}
$$

$$
\begin{aligned}
& { }^{\mathrm{v}_{\mathrm{C}}}=\frac{1}{\mathrm{C}} \cdot \int_{-\infty}^{\mathrm{t}} \mathrm{i}_{\mathrm{C}}^{\mathrm{dt}} \\
& \text { Or... } \quad{ }^{\mathrm{v}_{\mathrm{C}}}=\frac{1}{\mathrm{C}} \cdot \int_{0}^{\mathrm{t}}{ }^{\mathrm{i}} \mathrm{C}^{\mathrm{dt}+\mathrm{v}_{\mathrm{C}}(0)} \\
& \text { Or... initial voltage } \\
& \\
&
\end{aligned}
$$

Energy stored in electric field: $\mathrm{W}_{\mathrm{C}}=\frac{1}{2} \cdot \mathrm{C} \cdot \mathrm{V}_{\mathrm{C}}{ }^{2}$
Capacitor voltage cannot change instantaneously
parallel:

$$
\begin{gathered}
\mathrm{C}_{\mathrm{eq}}=\mathrm{C}_{1}+\mathrm{C}_{2}+\mathrm{C}_{3}+\ldots \\
\mathrm{c}_{1}+\mathrm{c}_{2}+ \\
\hline 1
\end{gathered}
$$

Capacitors are the only "backwards" components.
series: $\quad C_{e q}=\frac{1}{\frac{1}{\mathrm{C}_{1}}+\frac{1}{\mathrm{C}_{2}}+\frac{1}{\mathrm{C}_{3}}+\ldots}$


Sinusoids

## Steady-state or Final conditions

If a circuit has been connected for "a long time", then it has reached a steady state condition. that means the currents and voltages are no longer changing.
$\frac{\mathrm{d}}{\mathrm{dt}} \mathrm{v} \mathrm{C}=0 \quad{ }^{\mathrm{i}} \mathrm{C}=\mathrm{C} \cdot \frac{\mathrm{d}}{\mathrm{dt}} \mathrm{v} \mathrm{C}=0$

no current means it looks like an open

$$
\begin{aligned}
& { }^{\mathrm{i}} \mathrm{C}^{(\mathrm{t})}=\mathrm{I}_{\mathrm{p}} \cdot \cos (\omega \cdot \mathrm{t}) \\
& \left.{ }^{\mathrm{v}} \mathrm{C}^{(\mathrm{t}}\right)=\frac{1}{\mathrm{C}} \cdot \int \quad{ }_{\mathrm{i}}^{\mathrm{C}} \mathrm{dt} \quad=\frac{1}{\mathrm{C}} \cdot \frac{1}{\omega} \cdot \mathrm{I}_{\mathrm{p}} \cdot \sin (\omega \cdot \mathrm{t})=\frac{1}{\mathrm{C}} \cdot \frac{1}{\omega} \cdot \mathrm{I}_{\mathrm{p}} \cdot \cos (\omega \cdot \mathrm{t}-90 \cdot \mathrm{deg}) \\
& \text { indefinite integral }
\end{aligned}
$$

> Voltage "lags" current, makes sense, current has to flow in first to charge capacitor.

## Example

The voltage across a $0.5 \mu \mathrm{~F}$ capacitor is shown below. Make an accurate drawing of the capacitor current. Label the $y$-axis of your graph (I've already done the time-axis).
The accuracy of your plot at $0,2,6$, and 8 ms is important, so calculate those values and plot or label them carefully. Between those points your plot must simply be the correct shape.
$\mathrm{C}:=0.5 \cdot \mu \mathrm{~F}$
$1-2 \mathrm{~ms}: \quad{ }^{\mathrm{i}} \mathrm{C}=\mathrm{C} \cdot \frac{\Delta \mathrm{V}}{\Delta \mathrm{t}}=0.5 \cdot \mu \mathrm{~F} \cdot \frac{-4 \cdot \mathrm{~V}}{2 \cdot \mathrm{~ms}}=-1 \cdot \mathrm{~mA}$
$2 \mathrm{~ms}-6 \mathrm{~ms}$ : Initial slope is zero and the final slope is positive, so the current must be a triangle that starts at zero and ends at some height.

$$
\begin{aligned}
{ }^{\Delta{ }^{\mathrm{v}}} \mathrm{C}^{(\mathrm{t})} & =\frac{1}{\mathrm{C}} \cdot \int_{0}^{\mathrm{t}}{ }^{\mathrm{i}} \mathrm{C}^{(\mathrm{t}) \mathrm{dt}} \\
8 \cdot \mathrm{~V} & =\frac{1}{\mathrm{C}} \cdot\left(\frac{4 \cdot \mathrm{~ms} \cdot \text { height }}{2}\right) \\
\text { height } & =8 \cdot \mathrm{~V} \cdot \frac{\mathrm{C} \cdot 2}{4 \cdot \mathrm{~ms}}=2 \cdot \mathrm{~mA}
\end{aligned}
$$

$6 \mathrm{~ms}-8 \mathrm{~ms}$ : Slope is zero, so the current must be zero.

## ECE 2210 / 00 Inductor Lecture Notes



Basic equations you should know:

$$
v_{L}=L \cdot \frac{d}{d t} i_{L}
$$

Energy stored in electric field: $\mathrm{W}_{\mathrm{L}}=\frac{1}{2} \cdot \mathrm{~L} \cdot \mathrm{I}_{\mathrm{L}}{ }^{2}$ Inductor current cannot change instantaneously
Units: henry $=\frac{\mathrm{volt} \cdot \mathrm{sec}}{\mathrm{amp}}$
$\mathrm{L}=\mu_{\mathrm{o}} \cdot \mathrm{N}^{2} \cdot \mathrm{~K}$

$\mu$ is the permeability of the inductor core
K is a constant which depends on the inductor geometry N is the number of turns of wire

$$
\begin{aligned}
& \mathrm{i}_{\mathrm{L}}=\frac{1}{\mathrm{~L}} \cdot \int_{-\infty}^{\mathrm{t}}{ }_{-}^{\mathrm{v}}{ }_{\mathrm{L}} \mathrm{dt} \\
& \text { Or... }{ }^{\mathrm{i}} \mathrm{~L}=\frac{1}{\mathrm{~L}} \cdot \int_{0}^{\mathrm{t}}{ }^{\mathrm{v}}{ }_{\mathrm{L}} \mathrm{dt}+\mathrm{i}_{\mathrm{L}}(0) \\
& \text { initial current }
\end{aligned}
$$

$$
\mathrm{mH}=10^{-3} \cdot \mathrm{H} \quad \mu \mathrm{H}=10^{-6} \cdot \mathrm{H}
$$

```
series:
\[
\mathrm{L}_{\mathrm{eq}}=\mathrm{L}_{1}+\mathrm{L}_{2}+\mathrm{L}_{3}+\ldots
\]
```

parallel:

$$
\begin{aligned}
\mathrm{L}_{\mathrm{eq}}= & \frac{1}{\frac{1}{\mathrm{~L}_{1}}+\frac{1}{\mathrm{~L}_{2}}+\frac{1}{\mathrm{~L}_{3}}+\ldots} \\
& =\mathrm{L}_{1} \mathrm{~L} \mathrm{~L} \mathrm{~L}_{3} \mathrm{~S} \\
& \mathrm{~L}_{4}
\end{aligned}
$$

Sinusoids $\quad{ }_{i} L^{(t)}=I_{p} \cdot \cos (\omega \cdot \mathrm{t})$
${ }^{v}{ }_{L}(t)=L \cdot \frac{d}{d t} i_{L}=L \cdot \omega \cdot\left(-I_{p} \cdot \sin (\omega \cdot t)\right) \quad=L \cdot \omega \cdot I_{p} \cdot \cos (\omega \cdot t+90 \cdot \operatorname{deg})$


Resonance
Series resonance
Voltage "leads" current, makes sense, voltage has to present to make current change, so voltage comes first.


The resonance frequency is calculated the same way for either case:
$\omega_{\mathrm{o}}=\frac{1}{\sqrt{\mathrm{~L} \cdot \mathrm{C}}}\left(\frac{\mathrm{rad}}{\mathrm{sec}}\right) \quad$ OR.. $\quad \omega_{\mathrm{o}}=\frac{1}{\sqrt{\mathrm{~L}_{\mathrm{eq}} \cdot \mathrm{C}_{\mathrm{eq}}}}$
$\begin{aligned} & \text { If you have multiple capacitors or } \\ & \text { inductors which can be combined. }\end{aligned} \quad \mathrm{f}_{\mathrm{o}}=\frac{\omega_{\mathrm{o}}}{2 \cdot \pi}$
(Hz)

## Steady-state of Final conditions

If a circuit has been connected for "a long time", then it has reached a steady state condition. that means the currents and voltages are no longer changing.

$$
\frac{\mathrm{d}}{\mathrm{dt}} \mathrm{i} \mathrm{~L}=0 \quad{ }^{\mathrm{v}} \mathrm{~L}=\mathrm{L} \cdot \frac{\mathrm{~d}}{\mathrm{dt}} \mathrm{i} \mathrm{~L}=0
$$


no voltage means it looks like a short

## Examples

Ex 1
Find the resonant frequency (or frequencies) of the circuit shown (in cycles/sec or Hz ).

$\omega_{\mathrm{o}}:=\frac{1}{\sqrt{\mathrm{~L}_{\mathrm{eq}} \cdot \mathrm{C}_{\mathrm{eq}}}}$
$\omega_{o}=11547 \cdot \frac{\mathrm{rad}}{\mathrm{sec}}$
$\mathrm{f}_{\mathrm{o}}=\frac{\omega_{\mathrm{o}}}{2 \cdot \pi}=1838 \cdot \mathrm{~Hz}$

The current through a 0.3 mH inductor is shown below. Make an accurate drawing of the inductor voltage.
Make reasonable assumptions where necessary. Label your graph.


$0-2 \mu \mathrm{~s}: \quad$ No change in current, so: ${ }^{\mathrm{v}} \mathrm{L}=0$
$2 \mu \mathrm{~s}-4 \mu \mathrm{~s}: \quad{ }^{\mathrm{v}} \mathrm{L}_{\mathrm{L}}=\mathrm{L} \cdot \frac{\Delta \mathrm{I}}{\Delta \mathrm{t}}=0.3 \cdot \mathrm{mH} \cdot \frac{-0.6 \cdot \mathrm{~A}}{2 \cdot \mu \mathrm{~s}}=-90 \cdot \mathrm{~V}$
$4 \mu \mathrm{~s}-8 \mu \mathrm{~s}$ : Initial slope is positive and the final slope is zero, so the voltage must be a triangle that starts at some height and ends at zero.

$$
\begin{aligned}
& \Delta \mathrm{i}_{\mathrm{L}}(\mathrm{t})=\frac{1}{\mathrm{~L}} \cdot \int_{0}^{\mathrm{t}} \mathrm{v}_{\mathrm{L}}(\mathrm{t}) \mathrm{dt} \\
& 0.6 \cdot \mathrm{~A}=\frac{1}{0.3 \cdot \mathrm{mH}} \cdot\left(\frac{4 \cdot \mu \mathrm{~s} \cdot \mathrm{height}}{2}\right) \\
& \text { height }=0.6 \cdot \mathrm{~A} \cdot \frac{0.3 \cdot \mathrm{mH} \cdot 2}{4 \cdot \mu \mathrm{~s}}=90 \cdot \mathrm{~V}
\end{aligned}
$$

$8 \mu \mathrm{~s}-10 \mu \mathrm{~s}$ : No change in current, so: $\mathrm{v}_{\mathrm{L}}=0$

Ex 3 Given a voltage, find the current, $\mathrm{L}:=4 \cdot \mathrm{mH}$

$$
\begin{aligned}
\Delta \mathrm{i}_{\mathrm{L}}(\mathrm{t})= & \frac{1}{\mathrm{~L}} \cdot \int_{1 \cdot \mu \mathrm{~s}}^{2 \cdot \mu \mathrm{~s}} 20 \cdot \mathrm{~V} \mathrm{dt}=5 \cdot \mathrm{~mA} \\
& \frac{1}{\mathrm{~L}} \cdot \int_{4 \cdot \mu \mathrm{~s}}^{8 \cdot \mu \mathrm{~s}}-10 \cdot \mathrm{Vdt}+5 \cdot \mathrm{~mA}=-5 \cdot \mathrm{~mA} \\
& \frac{1}{\mathrm{~L}} \cdot \int_{8 \cdot \mu \mathrm{~s}}^{10 \cdot \mu \mathrm{~s}} \quad \mathrm{~V}(\mathrm{t}) \mathrm{dt}+-5 \cdot \mathrm{~mA}
\end{aligned}
$$



$$
=\frac{1}{\mathrm{~L}} \cdot \frac{20 \cdot \mathrm{~V} \cdot 2 \cdot \mu \mathrm{~s}}{2}-5 \cdot \mathrm{~mA}=0 \cdot \mathrm{~mA} \quad \text { etc } \ldots
$$

Ex 4 The following circuit has been connected as shown for a long time. Find the energy stored in the
 capacitor and the inductor.


# Capacitor, Inductor Notes 

## Capacitors

$\mathrm{C}=\frac{\mathrm{Q}}{\mathrm{V}} \quad$ farad $=\frac{\mathrm{coul}}{\mathrm{volt}}=\frac{\mathrm{amp} \cdot \mathrm{sec}}{\mathrm{volt}}$

${ }^{\mathrm{i}} \mathrm{C}^{\mathrm{dt}}=\frac{1}{\mathrm{C}} \cdot \int_{0}^{\mathrm{t}} \quad \mathrm{i}_{\mathrm{C}} \mathrm{dt}+\mathrm{v}_{\mathrm{C}}(0)$
${ }^{\mathrm{i}} \mathrm{C}=\mathrm{C} \cdot \frac{\mathrm{d}}{\mathrm{dt}} \mathrm{v}_{\mathrm{C}}$
Capacitor voltage cannot change instantaneously
Energy stored in electric field: $\mathrm{W}_{\mathrm{C}}=\frac{1}{2} \cdot \mathrm{C} \cdot \mathrm{V}_{\mathrm{C}}{ }^{2}$
parallel: $\mathrm{C}_{\mathrm{eq}}=\mathrm{C}_{1}+\mathrm{C}_{2}+\mathrm{C}_{3}+\ldots$


Steady-state sinusoids:
Impedance: $\quad Z_{C}=\frac{1}{j \cdot \omega \cdot C}=\frac{-j}{\omega \cdot C} \quad$ Current leads voltage by 90 deg

## Inductors

henry $=\frac{\text { volt } \cdot \text { sec }}{\mathrm{amp}}$
 $v_{L}=L \cdot \frac{d}{d t} i_{L}$

Energy stored in magnetic field: $\mathrm{W}_{\mathrm{L}}=\frac{1}{2} \cdot \mathrm{LI} \mathrm{L}^{2}$
series: $\mathrm{L}_{\mathrm{eq}}=\mathrm{L}_{1}+\mathrm{L}_{2}+\mathrm{L}_{3}+\ldots$

$$
x_{1} x_{3}-L_{4}
$$

## Steady-state sinusoids:

Impedance: $\mathrm{Z}_{\mathrm{L}}=\mathrm{j} \cdot \omega \cdot \mathrm{L} \quad$ Current lags voltage by 90 deg
Inductor current cannot change instantaneously
parallel: $\mathrm{L}_{\mathrm{eq}}=\frac{1}{\frac{1}{\mathrm{~L}_{1}}+\frac{1}{\mathrm{~L}_{2}}+\frac{1}{\mathrm{~L}_{3}}}+\ldots$

## RC and RL first-order transient circuits

For all first order transients: ${ }^{\mathbf{X}}{ }^{(t)}={ }^{\mathrm{v}} \mathrm{X}^{(\infty)}+\left(\mathrm{v}_{\mathrm{X}}(0)-\mathrm{v}_{\mathrm{X}}(\infty)\right) \cdot \mathrm{e}^{\tau}$

$$
{ }^{i} X^{(t)}={ }^{i} X^{(\infty)}+\left(i^{i} X^{(0)-i} X^{(\infty)}\right) \cdot e^{-\frac{t}{\tau}}
$$

Find initial Conditions $\quad\left(v_{C}\right.$ and/or $\left.i_{L}\right)$
Find conditions just before time $t=0, v_{C}\left(0^{-}\right)$and $i_{L}(0-)$. These will be the same just after time $t=0, v_{C}(0+)$ and $\mathrm{i}_{\mathrm{L}}\left(0^{+}\right)$and will be your initial conditions. (If initial conditions are zero: Capacitors are shorts, Inductors are opens.) Use normal circuit analysis to find your desired variable: ${ }^{\mathrm{v}} \mathrm{X}^{(0)}$ or ${ }^{\mathrm{i}} \mathrm{X}^{(0)}$
Find final conditions ("steady-state" or "forced" solution) Inductors are shorts Capacitors are opens Solve by DC analysis ${ }^{\mathrm{v}} \mathrm{X}^{(\infty)}$ or ${ }^{\mathrm{i}} \mathrm{X}^{(\infty)}$


RL Time constant $=\tau=\frac{L}{R}$




1) Find $C_{e q}$ in each case
a)

b)

c)

2. Each of the following circuits have been connected as shown for a long time. Find the voltage across each capacitor and the energy stored in each.


Name: $\qquad$ You may want to hand in this page with answers to problems $3 \& 4$.
3. The current waveform shown below flows through a $0.025 \mu \mathrm{~F}$ capacitor. Make an accurate drawing of the voltage across it. Label your graph. Assume the initial voltage across the capacitor is 0 V .

4. The voltage across a $2 \mu \mathrm{~F}$ capacitor is shown below. Make an accurate drawing of the capacitor current. Label your graph.

5. The voltage across a $0.68 \mu \mathrm{~F}$ capacitor is $\mathrm{v}_{\mathrm{c}}=6 \cdot \mathrm{~V} \cdot \cos \left(200 \cdot \mathrm{t}+\frac{\pi}{2} \quad\right.$ find $\mathrm{i}_{\mathrm{c}}$.
6. The current through a $0.0047 \mu \mathrm{~F}$ capacitor is $\mathrm{i}_{\mathrm{c}}=18 \cdot \mu \mathrm{~A} \cdot \cos \left(628 \cdot \mathrm{t}-\frac{\pi}{4} \quad\right.$ find $\mathrm{v}_{\mathrm{c}}$.
7. A capacitor voltage and current are shown at right. What value is the capacitor?

## Answers

1. a) $0.6 \cdot \mu \mathrm{~F}$
b) $0.015 \cdot \mu \mathrm{~F}$
c) $4.5 \cdot \mu \mathrm{~F}$
2. a) $3.3 \mathrm{~V} \quad 0.027 \cdot \mathrm{~mJ}$
b) $37.5 \cdot \mathrm{~V} \quad 0.33 \cdot \mathrm{~mJ}$
c) $11 \cdot \mathrm{~V} \quad 0.0411 \cdot \mathrm{~mJ} \quad 5 \cdot \mathrm{~V} \quad 2.75 \cdot \mu \mathrm{~J}$
3. $1.8 \cdot \mathrm{~V} \quad 0.6 \cdot \mathrm{~V} \quad 2.4 \cdot \mathrm{~V}$
4. $-6 \cdot \mathrm{~mA} \quad 12 \cdot \mathrm{~mA}$ ramp to -8 mA
5. $\mathrm{i}_{\mathrm{c}}=0.816 \cdot \mathrm{~mA} \cdot \cos (200 \cdot \mathrm{t}+\pi)$
6. $\mathrm{v}_{\mathrm{c}}=6.1 \cdot \mathrm{~V} \cdot \cos 628 \cdot \mathrm{t}-\frac{3 \cdot \pi}{4}$
7. $0.25 \cdot \mu \mathrm{~F}$


ECE 2210/00 homework \# 8

Name:
ECE 2210 / 00 hw \# 9
Due: Fri, 10/1/21
You will need another paper for your calculations, but you may want to hand this sheet in with your drawings.

1. Find $\mathrm{L}_{\mathrm{eq}}$ in each case
a)

b)

2. Find the stored energy in each capacitor and/or inductor under steady-state conditions. Note: Treat caps as opens and inductors as shorts to find DC voltages and currents.

3. The current waveform shown below flows through a 2 mH inductor. Make an accurate drawing of the voltage across it. Label your graph.


4. The voltage across a 0.5 mH inductor is shown below. Make an accurate drawing of the inductor current. Label your graph. Assume the initial current is 0 mA .

${ }^{i}$ L


## ECE 2210 / 00 homework \# 9

5. The voltage across a 1.2 mH inductor is $\mathrm{v}_{\mathrm{L}}=4 \cdot \mathrm{mV} \cdot \cos (300 \cdot \mathrm{t})$ find $\mathrm{i}_{\mathrm{L}}$.
6. The current through a 0.08 mH inductor is $\mathrm{i}_{\mathrm{L}}=20 \cdot \mathrm{~mA} \cdot \cos \left(628 \cdot \mathrm{t}-\frac{\pi}{4}\right)$ find $\mathrm{v}_{\mathrm{L}}$.
7. Refer to the circuit shown. Assume that $\mathrm{V}_{\mathrm{s}}$ is a sinusoidal input voltage whose frequency can be adjusted. At some frequency of $\mathrm{V}_{\mathrm{S}}$ this circuit can resonate. At that frequency $\mathrm{i}_{\mathrm{C}}(\mathrm{t})=-\mathrm{i}_{\mathrm{L}}(\mathrm{t})$. $\left(\mathrm{i}_{\mathrm{C}}(\mathrm{t})\right.$ is 180 degrees out-of-phase with $\mathrm{i}_{\mathrm{L}}(\mathrm{t})$ ). Show that resonance occurs at this frequency:

$$
\omega_{o}=\frac{1}{\sqrt{L \cdot C}}, \quad f_{o}=\frac{1}{2 \cdot \pi \cdot \sqrt{L \cdot C}}
$$


8. Find the resonant frequency, $\mathrm{f}_{\mathrm{o}}$ in each case.


## Answers

1. $1.2 \cdot \mathrm{mH}$
$0.62 \cdot \mathrm{mH}$
2. a) $0.05 \cdot \mathrm{~mJ}$
b) $\quad 1.62 \cdot \mathrm{~mJ} \quad 0.081 \cdot \mathrm{~mJ} \quad 0.09 \cdot \mathrm{~mJ} \quad 0.18 \cdot \mathrm{~mJ}$
3. Straight lines between the following points: $(0 \mathrm{~ms},-8 \mathrm{mV}),(2 \mathrm{~ms},-8 \mathrm{mV}),(2 \mathrm{~ms}, 0 \mathrm{mV}),(3 \mathrm{~ms}, 0 \mathrm{mV}),(3 \mathrm{~ms}, 16 \mathrm{mV})$, $(5 \mathrm{~ms}, 16 \mathrm{mV}),(5 \mathrm{~ms}, 0 \mathrm{mV}),(6 \mathrm{~ms}, 0 \mathrm{mV}),(9 \mathrm{~ms},-10.67 \mathrm{mV}),(9 \mathrm{~ms}, 0 \mathrm{mV}),(10 \mathrm{~ms}, 0 \mathrm{mV})$
4. Straight lines between the following points: $(0 \mathrm{~ms}, 0 \mathrm{~A}),(0.2 \mathrm{~ms}, 1.2 \mathrm{~A}),(0.6 \mathrm{~ms},-0.4 \mathrm{~A})$, curves until it's flat at ( $0.76 \mathrm{~ms},-0.72 \mathrm{~A}$ ), continues to curve up to ( $1 \mathrm{~ms}, 0 \mathrm{~A}$ ), $(1.1 \mathrm{~ms}, 0 \mathrm{~A})$
5. $\mathrm{i}_{\mathrm{L}}=11.1 \cdot \mathrm{~mA} \cdot \cos (300 \cdot \mathrm{t}-90 \cdot \mathrm{deg})$
6. $\mathrm{v}_{\mathrm{L}}=1 \cdot \mathrm{mV} \cdot \cos \left(628 \cdot \mathrm{t}+\frac{1}{4} \cdot \pi\right)$
7. Assume a sinusoidal voltage, find $\mathrm{i}_{\mathrm{C}}$ and $\mathrm{i}_{\mathrm{L}}$ by integration and differentiation, and show that they are equal and opposite at the resonant frequency.
8. 

a) $17.79 \cdot \mathrm{kHz}$
b) $5305 \cdot \mathrm{~Hz}$

