## ECE2210/00 Exam 3 given: Fall 06

1. (18 pts)
a) Find $\mathbf{V}_{\text {in }}$ in polar form.
b) Find $\mathbf{I}_{\mathbf{T}}$ in polar form..
c) Circle 1:
i) The source current leads the source voltage
ii) The source voltage leads the source current

2. ( 15 pts ) a) Find the s-type transfer function of the circuit shown. $V_{i}$ is the input and $V_{O}$ is the output.
You MUST show work to get credit.
Simplify your expression for $\mathrm{H}(\mathrm{s})$ so that the denominator is a simple polynomial beginning with $\mathrm{s}^{2}$.

$$
\mathbf{H}(\mathrm{s})=\text { ? }
$$

b) Find the characteristic equation of the circuit shown.

c) The solutions to the characteristic equation are called the $\qquad$ of the transfer function.
d) Does the transfer function have one or more zeros? If yes, express it (them) in terms of $\mathrm{R}_{1}, \mathrm{R}_{2}, \mathrm{C}$, \& L .
3. (20 pts) Analysis of a circuit (not pictured) yields the characteristic equation below.

$$
0=\mathrm{s}^{2}+500 \cdot \mathrm{~s}+62500 \quad \mathrm{R}:=80 \cdot \Omega \quad \mathrm{~L}:=640 \cdot \mathrm{mH} \quad \mathrm{C}:=25 \cdot \mu \mathrm{~F} \quad \mathrm{~V}_{\text {in }}:=12 \cdot \mathrm{~V}
$$

Further analysis yields the following initial and final conditions:
$\mathrm{i}_{\mathrm{L}}(0)=50 \cdot \mathrm{~mA}$
$v_{L}(0)=-9 \cdot V$
${ }^{\mathrm{v}} \mathrm{C}^{(0)}=4 \cdot \mathrm{~V}$
${ }^{\mathrm{i}} \mathrm{C}^{(0)}=80 \cdot \mathrm{~mA}$
${ }^{\mathrm{i}} \mathrm{L}^{(\infty)}=110 \cdot \mathrm{~mA}$
$\mathrm{v}_{\mathrm{L}}(\infty)=0 \cdot \mathrm{~V}$
${ }^{\mathrm{v}} \mathrm{C}^{(\infty)}=12 \cdot \mathrm{~V}$
${ }^{\mathrm{i}} \mathrm{C}^{(\infty)}=0 \cdot \mathrm{~mA}$

Write the full expression for $\mathrm{i}_{\mathrm{L}}(\mathrm{t})$, including all the constants that you find.
$\mathrm{i}_{\mathrm{L}}(\mathrm{t})=$ ?
Include units in your answer
4. (10 pts) For waveform shown, find:
a) Average $D C\left(V_{D C}\right)$ value
b) RMS (effective) value


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5. (13 pts) The transformer shown in the circuit below is ideal. It is rated at $120 / 12 \mathrm{~V}, 8 \mathrm{VA}, 60 \mathrm{~Hz}$ Find the following:
a) $I_{1}=$ ?
b) $V_{2}=$ ?

6. (24 pts) Consider the circuit at right. The switch has been in the closed position for a long time and is open (as shown) at time $t=0$.
a) What are the final conditions of $i_{L}$ and the $v_{C}$ ?

$$
\mathrm{i}_{\mathrm{L}}(\infty)=? \quad \mathrm{v}_{\mathrm{C}}(\infty)=?
$$

$$
\mathrm{I}_{\mathrm{S}}:=300 \cdot \mathrm{~mA}
$$


b) Find the initial condition and initial slope of $v_{C}$ that you would need to have in order to find all the constants in $\mathrm{v}_{\mathrm{C}}(\mathrm{t})$. Don't find $\mathrm{v}_{\mathrm{C}}(\mathrm{t})$ or it's constants, just the initial conditions.
c) Find the initial condition and initial slope of $i_{L}$ that you would need to have in order to find all the constants in $\mathrm{i}_{\mathrm{L}}(\mathrm{t})$. Don't find $\mathrm{i}_{\mathrm{L}}(\mathrm{t})$ or it's constants, just the initial conditions.

## Answers

1. a) $\mathbf{V}_{\text {in }}=3.6 \mathrm{~V} /-36.9^{\circ}$
b) $\mathbf{I}_{\mathbf{T}}=154 \mathrm{~mA} /-27.9^{\circ}$
c) i) $-27.9^{\circ}>-36.90$
2. a) $\frac{s^{2}+\frac{R_{2}}{L} \cdot s}{s^{2}+\left(\frac{R_{1}+R_{2}}{L}\right) \cdot s+\frac{1}{L \cdot C}}$
b) $0=\mathrm{s}^{2}+\left(\frac{\mathrm{R}_{1}+\mathrm{R}_{2}}{\mathrm{~L}}\right) \cdot \mathrm{s}+\frac{1}{\mathrm{~L} \cdot \mathrm{C}}$
c) poles
d) 0 and $-\frac{\mathrm{R}_{2}}{\mathrm{~L}}$
3. $\mathrm{i}_{\mathrm{L}}(\mathrm{t}):=110 \cdot \mathrm{~mA}-60 \cdot \mathrm{~mA} \cdot \mathrm{e}^{-\frac{250}{\sec } \cdot \mathrm{t}}-29 \cdot \frac{\mathrm{~A}}{\mathrm{sec}} \cdot \mathrm{t} \cdot \mathrm{e}^{-\frac{250}{\sec } \cdot \mathrm{t}}$
$\begin{array}{ll}\text { 4. a) } 0 \cdot V & \text { b) } 4.9 \cdot V\end{array}$
4. a) $40 \cdot \mathrm{~mA}$
b) $8 \cdot \mathrm{~V}$
5. a) $300 \cdot \mathrm{~mA} \quad 60 \cdot \mathrm{~V}$
b) $20 \cdot \mathrm{~V} \quad 50000 \cdot \frac{\mathrm{~V}}{\mathrm{sec}}$
c) $100 \cdot \mathrm{~mA} \quad 2500 \cdot \frac{\mathrm{~A}}{\mathrm{sec}}$

ECE 2210 Exam \#3
Arn Stolp
Name
Scores:
Pgs 1\&2 $\qquad$ of a possible 33 points

Pgs 3\&4 $\qquad$ of a possible 30 points

Pgs 5\&6 $\qquad$ of a possible 37 points

Total $\qquad$ of a possible 100 points

