1. (20 pts) a) Draw the asymptotic Bode plot (the straight-line approximation) of the transfer function below. Accurately draw it on the graph provided.

You must show the steps you use to get the Bode plot. That is, show things like the corner frequency(ies), the approximations of the transfer function in each frequency region, calculations of dB, etc..

$$
\mathrm{H}(\mathrm{f}):=\frac{1 \cdot \mathrm{~Hz}+0.1 \cdot \mathrm{j} \cdot \mathrm{f}}{20 \cdot \mathrm{~Hz}+\frac{\mathrm{j} \cdot \mathrm{f}}{100}}
$$

## Magnitude plot

$|\mathrm{H}(\mathrm{f})|$

Straight-line approximation $\qquad$ Actual $\qquad$


## Frequency

f(Hz)
b) The asymptotic Bode plot is not exact. Using a dotted line, sketch the actual magnitude of the transfer function $|\mathrm{H}(\mathrm{f})|$ on the plot above. Indicate the point(s) where the difference between the two lines is the biggest (draw arrow(s)) and write down the actual magnitude(s) at that (those) point(s).
c) List any corners in the Bode plot associated with zeroes in the transfer function.
d) List any corners in the Bode plot associated with poles in the transfer function.
2. (20 pts) Analysis of a circuit (not pictured) yields the characteristic equation below.

$$
0=s^{2}+100 \cdot s+1600 \quad \mathrm{R}:=10 \cdot \Omega \quad \mathrm{~L}:=800 \cdot \mathrm{mH} \quad \mathrm{C}:=60 \cdot \mu \mathrm{~F}
$$

Further analysis yields the following initial and final conditions:
$\mathrm{i}_{\mathrm{L}}(0)=180 \cdot \mathrm{~mA}$
$v_{L}(0)=-8 \cdot V$
${ }^{v} C^{(0)}=12 \cdot V$
${ }^{\mathrm{i}} \mathrm{C}^{(0)}=-9 \cdot \mathrm{~mA}$
$\mathrm{i}_{\mathrm{L}}(\infty)=100 \cdot \mathrm{~mA}$
$\mathrm{v}_{\mathrm{L}}(\infty)=0 \cdot \mathrm{~V}$
${ }^{\mathrm{v}} \mathrm{C}^{(\infty)}=3 \cdot \mathrm{~V}$
${ }^{\mathrm{i}} \mathrm{C}^{(\infty)}=0 \cdot \mathrm{~mA}$

Write the full expression for $\mathrm{i}_{\mathrm{L}}(\mathrm{t})$, including all the constants that you find. $\mathrm{i}_{\mathrm{L}}(\mathrm{t})=$ ? Include units in your answer
3. (14 pts) For waveform shown, find:
a) Average $\mathrm{DC}\left(\mathrm{V}_{\mathrm{DC}}\right)$ value
b) RMS (effective) value
c) The voltage is hooked to a resistor, as shown, for 6 seconds.

How much energy is transferred to the resistor during that 6 seconds?



## ECE 2210 Exam 3 Fall 10 p2

4. (21 pts) An capacitor (C, shown below) is used to completely correct the power factor of a load.
All values are RMS. Find the following:
a) The power consumed by the load.

$$
\mathrm{P}_{\mathrm{L}}=?
$$



Hint 1: Since C corrects the power factor, its Q must exactly cancel the load's Q and the source provides only P and no Q .
Hint 2: If hint 1 doesn't make sense to you, you don't know AC power well enough to do part a) -- so skip to part b).
b) The power supplied by the source. Note: If you skipped part a), assume $\mathrm{P}_{\mathrm{L}}=300 \mathrm{~W}$ for the rest of the problem.
c) The source current (magnitude and phase).
d) The load can be modeled as 2 parts in series. Draw the model and find the values of the parts.
5. (25 pts) The switch has been open for a long time and is closed (as shown) at time $\mathrm{t}=0$.

SHOW YOUR WORK, no credit for guesses!
a) What are the final conditions of $i_{L}$ and the $v_{C}$ ?

$$
{ }^{\mathrm{i}} \mathrm{~L}^{(\infty)}=? \quad{ }^{\mathrm{v}} \mathrm{C}^{(\infty)}=?
$$

b) Find the initial condition and initial slope of $\mathrm{i}_{\mathrm{L}}$ that you would need to have in order to find all the constants in $i_{L}(t)$. Don't find $\mathrm{i}_{\mathrm{L}}(\mathrm{t})$ or it's constants, just the initial conditions.
c) Find the initial condition and initial slope of $v_{C}$ that you would need to have in order to find all the constants in $v_{C}(t)$. Don't find $\mathrm{v}_{\mathrm{C}}(\mathrm{t})$ or it's constants, just the initial conditions.

$\mathrm{R}_{2}:=200 \cdot \Omega \quad \mathrm{C}:=3 \cdot \mu \mathrm{~F}$

## Answers

1. $a \& b)$
Magnitude plot $\qquad$

c) $10 \cdot \mathrm{~Hz}$
d) $2 \cdot \mathrm{kHz}$
2. $\mathrm{i} \mathrm{L}^{(\mathrm{t}):=100 \cdot \mathrm{~mA}-60 \cdot \mathrm{~mA} \cdot \mathrm{e}^{-\frac{20}{\sec } \cdot \mathrm{t}}+140 \cdot \mathrm{~mA} \cdot \mathrm{e}^{-\frac{80}{\sec } \mathrm{t}}} \begin{array}{llll} & \text { 3. a) } 1 \cdot \mathrm{~V} & \text { b) } 4.36 \cdot \mathrm{~V} & \text { c) } 2.28 \cdot \mathrm{~J}\end{array}$
3. a) $275 \cdot \mathrm{~W}$
b) $275 \cdot \mathrm{~W}$
c) $2.5 \cdot \mathrm{~A} \quad \underline{0}^{\circ}$
M-rorn
d) $30.6 \cdot \Omega \quad 53.8 \cdot \mathrm{mH}$
4. a) $150 \cdot \mathrm{~mA} \quad 18 \cdot \mathrm{~V}$
b) $100 \cdot \mathrm{~mA} \quad 0 \cdot \frac{\mathrm{~A}}{\mathrm{sec}}$
c) $20 \cdot \mathrm{~V} \quad-22222 \cdot \frac{\mathrm{~V}}{\mathrm{sec}}$
