1. (16 pts) Use the method of superposition to find $V_{c}$, the voltage across $R_{3}$.

Be sure to clearly show and circle your intermediate results.
2. (12 pts) If you wanted to solve the problem above using nodal analysis, you would have to write one or more nodal equations. Write all the necessary equation(s) in terms of the resistors, the sources, and the unknown nodes. Just write and circle the
 equations, do not try to simplify or solve them. Don't panic, this is an easy problem and it has more than one right answer.
3. (18 pts) a) Find and draw the Thévenin equivalent of the circuit shown. The load resistor is $R_{L}$.
b) Find and draw the Norton equivalent of the same circuit.

4. (8 pts) a) What is the time constant of this circuit? Hint: notice the similarity to the circuit above.
b) What will be the final value of $\mathrm{v}_{\mathrm{C}}$ ? (After the switch has been closed for a long time)

5. (26 pts) a) Find Z.

c) By how much? I.E. what is the phase angle between the voltage and current?
d) What is the power factor of this circuit? (as seen by $V_{S}$ )
e) How much average power does $\mathrm{V}_{\mathrm{S}}$ supply to the circuit?
6. (15 pts) The input voltage to the circuit below is shown at right (dotted line). Show the output voltage across the diode. Make it accurate and label the important voltages and times

$$
\mathrm{R}_{1}:=15 \cdot \Omega
$$


$\mathrm{R}_{2}:=25 \cdot \Omega$


## EE1050 Final given: Fall 00 p2

7. ( 30 pts) Fill in the blanks in the circuit. You may neglect $I_{B}$ 's effect on $I_{E}$, but do not neglect it on the

b) Is the transistor operating in the active region? Show your evidence. Yes No
c) What is the value of $\beta$ for this transistor?
d) If we neglect $I_{B}$ and use the values of $R_{1}$ and $R_{2}$ above to calculate $V_{B}$, what do you get?
e) Considering only $\mathrm{I}_{\mathrm{C}}$ and $\mathrm{V}_{\mathrm{CE}}$, how much power does this transistor dissipate or contribute?
f) If the $v_{s}$ signal were applied at the base, an AC signal would also appear at the collector. How much larger would it be. (Voltage gain).
8. OUT OF ORDER, Problem 8 is shown on last page
9. (14 pts) Find the characteristic equation of the circuit at right.
10. (9 pts) A circuit has the following characteristic equation:


$$
\mathrm{s}^{2}+\left(\frac{\mathrm{R}_{1}}{\mathrm{~L}}\right) \cdot \mathrm{s}+\left(\frac{\mathrm{R}_{1}}{\mathrm{R}_{2} \cdot \mathrm{~L} \cdot \mathrm{C}}\right)=0 \quad \mathrm{R}_{1}:=50 \cdot \Omega \quad \mathrm{~L}:=20 \cdot \mathrm{mH} \quad \mathrm{C}:=40 \cdot \mu \mathrm{~F}
$$

a) For what value of $R_{2}$ is the circuit critically damped?
b) To make the circuit overdamped, the value of $R_{2}$ should be: (circle one)
i) Larger
ii) Smaller
11. (10 pts) Consider the following transient waveform.
a) This circuit is: (circle one)
i) underdamped
ii) critically damped
iii) overdamped iv) can't tell
b) The final value of the capacitor voltage is:
c) The initial value of the capacitor voltage is:

d) The initial current through the capacitor is: (circle one)
i) positive (+)
ii) zero (0)
iii) negative (-)
iv) can't tell

## EE1050 Final given: Fall 00 p3

8. (20 pts) The same input signal is connected to several opamp circuits below. Sketch the output waveform for each circuit. Clearly label important voltage levels on each output. If I can' t easily make out what your peak values are, I' II assume you don' t know.


## EE1050 Final given: Fall 00 p4

## Answers

1. $\mathrm{V}_{\mathrm{c} . \mathrm{Is}}:=2 \cdot \mathrm{~V}_{\mathrm{c} . \mathrm{Is}}:=-5 \cdot \mathrm{~V}_{\mathrm{c}}:=-3 \cdot \mathrm{~V}$
2. node $\mathrm{a}: \mathrm{V}_{\mathrm{a}}=10 \cdot \mathrm{~V} \begin{aligned} & \text { This equation really } \\ & \text { isn' } \mathrm{t} \text { necessary }\end{aligned}$ node $\mathrm{b}: \frac{\mathrm{V}_{\mathrm{S}}-\mathrm{V}_{\mathrm{b}}}{\mathrm{R}_{1}}=\frac{\mathrm{V}_{\mathrm{b}}-\mathrm{V}_{\mathrm{c}}}{\mathrm{R}_{2}}+\mathrm{I}_{\mathrm{S}}$ node $\mathrm{c}: \frac{\mathrm{V}_{\mathrm{b}}-\mathrm{V}_{\mathrm{c}}}{\mathrm{R}_{2}}=\frac{\mathrm{V}_{\mathrm{c}}}{\mathrm{R}_{3}}$
3. a)
$\mathrm{R}_{\mathrm{Th}}:=150 \cdot \Omega \quad \mathrm{~B}$
b) $\quad \mathrm{R}_{\mathrm{N}}=\mathrm{R}_{\mathrm{Th}}=150 \cdot \Omega$

$\mathrm{I}_{\mathrm{N}}=\frac{\mathrm{V}_{\mathrm{Th}}}{\mathrm{R}_{\mathrm{Th}}}=50 \cdot \mathrm{~mA}$

4. a) $\tau:=\mathrm{R} \mathrm{Th} \cdot \mathrm{C} \quad \tau:=3.3 \cdot \mathrm{~ms}$
b) ${ }^{\mathrm{v}} \mathrm{C}^{(\infty)}=\mathrm{V}_{\mathrm{Th}}=7.5 \cdot \mathrm{~V}$
5. 

a) $Z:=(259-160 \cdot \mathrm{j}) \cdot \Omega$
b) i
c) $20 \cdot \mathrm{deg}$
d) 0.94
e) $0.197 \cdot$ watt
6. $0,0 \quad 1.4 \mathrm{~ms}, 0.7 \mathrm{~V} \quad 8.6 \mathrm{~ms}, 0.7 \mathrm{~V} \quad 15 \mathrm{~ms},-2.5 \mathrm{~V}$
7. a) $\mathrm{I}_{\mathrm{R} 2}:=020 \cdot \mathrm{~mA} \quad \mathrm{I}_{\mathrm{R} 1}:=0.21 \cdot \mathrm{~mA} \quad \mathrm{R}_{1}:=61 \cdot \mathrm{k} \Omega \quad \mathrm{V}_{\mathrm{E}}:=1.5 \cdot \mathrm{~V}^{2} \quad \mathrm{R}_{\mathrm{E}}:=598 \cdot \Omega \quad \mathrm{~V}_{\mathrm{C}}:=8.5 \cdot \mathrm{~V} \quad \mathrm{R}_{\mathrm{C}}:=2.6 \cdot \mathrm{k} \Omega$
b) Yes, $V_{\mathrm{CE}}:=7 \cdot \mathrm{~V}>0.2 \cdot \mathrm{~V} \quad$ c) $250 \quad$ d) $2.293 \cdot \mathrm{~V} \quad$ e) $17.5 \cdot \mathrm{~mW} \quad$ f) 4.33
8. a) $0,02 \mathrm{~ms}, 1 \mathrm{~V} \quad 6 \mathrm{~ms},-1 \mathrm{~V} \quad 8 \mathrm{~ms}, 0 \mathrm{~V}$
b) $0,0 \quad 2 \mathrm{~ms},-0.8 \mathrm{~V} \quad 6 \mathrm{~ms}, 0.8 \mathrm{~V} \quad 8 \mathrm{~ms}, 0 \mathrm{~V}$
c) $0,-0.2 \mathrm{~V} 2 \mathrm{~ms},-1.8 \mathrm{~V} 6 \mathrm{~ms},-0.2 \mathrm{~V} \quad 8 \mathrm{~ms},-1 \mathrm{~V}$
10. a) $40 \cdot \Omega$
b) larger
11. a) i
b) $2 \cdot \mathrm{~V}$
c) $4 \cdot V$
d) i
9. $\mathrm{s}^{2}+\left(\frac{1}{\mathrm{C} \cdot \mathrm{R}_{2}}+\frac{\mathrm{R}_{1}}{\mathrm{~L}}\right) \cdot \mathrm{s}+\frac{\mathrm{R}_{1}}{\mathrm{C} \cdot \mathrm{R}_{2} \cdot \mathrm{~L}}=0$

NOTE
By the way, if you' II look at the circuit more closely, you' Il see that it can easily be separated into two completely separate first order circuits. This means that while the characteristic equation for the total current is indeed a second order equation, it must always have two real roots (first order circuits can' $t$ ring).
Sure enough, it turns out that this characteristic equation can be factored as below:

$$
\begin{aligned}
& \mathrm{s}^{2}+\left(\frac{1}{\mathrm{C} \cdot \mathrm{R}_{2}}+\frac{\mathrm{R}_{1}}{\mathrm{~L}}\right) \cdot \mathrm{s}+\frac{\mathrm{R}_{1}}{\mathrm{C} \cdot \mathrm{R}_{2} \cdot \mathrm{~L}}=\left(\mathrm{R}_{1}+\mathrm{L} \cdot \mathrm{~s}\right) \cdot \frac{\left(\mathrm{C} \cdot \mathrm{R}_{2} \cdot \mathrm{~s}+1\right)}{\left[\mathrm{C} \cdot\left(\mathrm{R}_{2} \cdot \mathrm{~L}\right)\right]}=\left(\frac{\mathrm{R}_{1}}{\mathrm{~L}}+\mathrm{s}\right) \cdot\left(\mathrm{s}+\frac{1}{\mathrm{C} \cdot \mathrm{R}_{2}}\right) \\
& \text { This results in the two roots: } \mathrm{s}=-\frac{\mathrm{R}_{1}}{\mathrm{~L}} \text { and } \mathrm{s}=-\frac{1}{\mathrm{C} \cdot \mathrm{R}_{2}}
\end{aligned}
$$

Which, if you think about it, is pretty predictable. If you saw this and mentioned it, you could get get some extra points.

