## ECE2210 Final given: Fall 05

1. (14 pts) The switch has been open (not making contact) for a long time and is switched closed (as shown) at time $\mathrm{t}=0$.

Find the complete expression for $\mathrm{i}_{\mathrm{L}}(\mathrm{t})$.

2. (15 pts) For partial credit, you must show work and/or intermediate results.
a) Find $\mathbf{I}_{\mathbf{2}}$
b) Find $\mathbf{V}_{\mathbf{S}}$
c) Find $\mathbf{I}_{\mathbf{1}}$ in polar form.

3. (30 pts) a) Draw the asymptotic Bode plot (the straight-line approximation) of the filter circuit below. Accurately draw it on the graph provided. $\mathrm{V}_{\mathrm{in}}$ is the input and $\mathrm{V}_{\mathrm{O}}$ is the output of this circuit. Graph is in rad/sec.
You must show the steps you use to get the Bode plot. That is, show things like the corner frequency(ies), the approximations of the transfer function in each frequency region, calculations of dB , etc..

Draw the staight-line Bode plot

$$
H(\omega)=\frac{1+\mathrm{j} \cdot \omega \cdot \mathrm{R} \cdot \mathrm{C}_{2}}{5+\mathrm{j} \cdot \omega \cdot \mathrm{R} \cdot \mathrm{C}_{2}}
$$


b) The asymptotic Bode plot is not exact. The actual magnitude of the transfer function can be a little different than the straight-line approximation. Draw in the actual frequency response curve with a dashed line. For the frequency(ies) where the curves are most different, indicate the actual dB on the plot.
c) If there are any corners in the Bode plot associated with poles in the transfer function, list that/those corner frequency(ies) below $\left(\omega_{\mathrm{p}}\right)$.
d) If there are any corners in the Bode plot associated with zeroes in the transfer function, list that/those corner frequency(ies) below $\left(\omega_{z}\right)$.
e) What is the value of $\mathrm{C}_{1}$ ?

Hint: Find the Transfer function in terms of $\mathrm{C}_{1}, \mathrm{C}_{2}, \mathrm{R}, \& \omega$ and compare what you get to my transfer function.
4. (13 pts) a) Find the s-type transfer function of ECE2210 Final given: Fall 05 the circuit shown.
$\mathrm{V}_{\mathrm{i}}$ is the input and $\mathrm{V}_{\mathrm{O}}$ is the output.
You MUST show work to get credit.
Simplify your expression for $\mathrm{H}(\mathrm{s})$ so that the denominator is a simple polynomial.
$\mathrm{H}(\mathrm{s})=$ ?
b) Find the characteristic equation of the circuit shown.

5. (18 pts) Consider the circuit at right. The current source has been 50 mA for a long time and changes from 50 mA to 20 mA at time $\mathrm{t}=0$.
a) What are the final conditions of $i_{L}$ and the $v_{C}$ ?

$$
\mathrm{i}_{\mathrm{L}}(\infty)=? \quad{ }^{\mathrm{v}} \mathrm{C}^{(\infty)}=?
$$

b) Find the initial condition and intial slope of $i_{L}$ that you would need to have in order to find all the constants in $i_{L}(t)$. Don't find $i_{L}(t)$ or it's constants, just the initial conditions.
c) Find the initial condition and intial slope of $\mathrm{v}_{\mathrm{C}}$ that you would need to have in order to find all the constants in $\mathrm{v}_{\mathrm{C}}(\mathrm{t})$. Don't find $\mathrm{v}_{\mathrm{C}}(\mathrm{t})$ or it's constants, just the initial conditions.
$\mathrm{t}<0$ : $\mathrm{I}_{\mathrm{S}}:=50 \cdot \mathrm{~mA}$
$\mathrm{t} \geq 0: \mathrm{I}_{\mathrm{S}}:=20 \cdot \mathrm{~mA}$

Use constant-voltage-drop models for the diodes and LEDs on this exam.
6. (18 pts) Assume that diode $\mathrm{D}_{1}$ does NOT conduct. Assume that diode $\mathrm{D}_{2}$ does conduct.
a) Find $\mathrm{I}_{\mathrm{R} 1}, \mathrm{I}_{\mathrm{R} 2}, \mathrm{I}_{\mathrm{R} 3}, \& \mathrm{I}_{\mathrm{V} 2}$ based on these assumptions. Stick with these assumptions even if your answers come out absurd
$\qquad$ ${ }^{\mathrm{I}} \mathrm{R}_{3}=$ $\qquad$
${ }^{\mathrm{I}} \mathrm{R}=$ $\qquad$ $\mathrm{I}_{\mathrm{D} 2}=$ $\qquad$
(circle one)
b) Was the assumption about $\mathrm{D}_{1}$ correct? yes no How do you know? (Specifically show a value which is or is not within a correct range.)
c) Was the assumption about $\mathrm{D}_{2}$ correct? How do you know?

7. ( 18 pts ) A voltage waveform (dotted line) is applied to the circuit shown. Accurately draw the output waveform ( $\mathrm{v}_{\mathrm{o}}$ ) you expect to see. Label important times and voltage levels.


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8. (27 pts) The same input signal (at right) is connected to several op-amp circuits below. Sketch the output waveform for each circuit. Clearly label important voltage levels on each output. If I can' t easily make out what your peak values are, I' II assume you don' t know. Don' t forget to show inversions. All op-amps are powered by $\pm 15 \mathrm{~V}$ power supplies.
a)
b)

c)

$\mathrm{V}_{\mathrm{of}} \mathrm{V}^{(\mathrm{t})}$
$\mathrm{V}_{\mathrm{o4}}{ }^{(\mathrm{t})}$
(V)

$\mathrm{V}_{\mathrm{O2}}\left({ }^{(t)}\right.$
(V)

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$\mathrm{V}_{03}(\mathrm{t})$
(V)

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9. (27 pts)
a) $\beta=25$

Assume the transistor is in the active region, find $\mathrm{I}_{\mathrm{sw}}, \mathrm{I}_{\mathrm{L}}, \mathrm{V}_{\mathrm{L}}, \mathrm{V}_{\mathrm{EC}}$ and $\mathrm{P}_{\mathrm{Q}}$.
$\mathrm{I}_{\mathrm{sw}}=$ ?
$\mathrm{I}_{\mathrm{L}}=$ ?
$\mathrm{V}_{\mathrm{L}}=$ ?
$\mathrm{V}_{\mathrm{EC}}=$ ?
$\mathrm{P}_{\mathrm{Q}}=$ ?
b) Was the transistor actually operating in the active region? yes no (circle one)
How do you know? (Specifically show a value which is or is not within a correct range.)
c) Find the maximum value of $R_{1}$, so that the transistor will be in saturation.

d) $\mathrm{R}_{1}=300 \cdot \Omega$ and can' t be changed, find the minimum value $o \beta$ so that the transistor will be in saturation.
e) How much power is dissipated by the transistor in d)
f) The switch is opened. What is the load current $\left(\mathrm{I}_{\mathrm{L}}\right)$ now?
10. Do you want your grade and scores posted on my door and on the internet? Yes No (Circle one) If your answer is yes, then provide some sort of alias or password: $\qquad$
The grades will be posted on my door in alphabetical order under the alias that you provide here. I will not post grades under your real name. The internet version will be a pdf file which you can download. Both will show the homework, lab, and exam scores of everyone who answers yes here.

## Answers

1. $450 \cdot \mathrm{~mA}-270 \cdot \mathrm{~mA} \cdot \mathrm{e}^{-\frac{\mathrm{t}}{0.1 \cdot \mathrm{~ms}}}$
2. a) $\mathbf{I}_{\mathbf{2}}:=20 \cdot \mathrm{~mA} \cdot \mathrm{e}^{-\mathrm{j} \cdot 30 \mathrm{deg}}$
b) $\mathbf{V}_{\mathbf{S}}=(4.61+0.814 \cdot \mathrm{j}) \cdot \mathrm{V}$

$$
=4.68 \cdot \mathrm{~V} \cdot \mathrm{e}^{-\mathrm{j} \cdot 10 \mathrm{deg}}
$$

c) $\mathbf{I}_{\mathbf{1}}=9.68 \cdot \mathrm{~mA} \cdot \mathrm{e}^{\mathrm{j} \cdot 46.3 \cdot \mathrm{deg}}$
3. a) \& b) Magnitude plot dB
$|H(\omega)|$
Straight-line
approximation____
Actual $\qquad$
c) $1500 \cdot \frac{\mathrm{rad}}{\mathrm{sec}}$
d) $300 \cdot \frac{\mathrm{rad}}{\mathrm{sec}}$

e) $0.5 \cdot \mu \mathrm{f}$
4. a) $H(s)=\frac{\frac{1}{L \cdot C}}{s^{2}+\left(\frac{R_{1}}{L}+\frac{1}{R_{2} \cdot C}\right) \cdot s+\left(1+\frac{R_{1}}{R_{2}}\right) \cdot \frac{1}{L \cdot C}}$
5. a) $2 \cdot V$
$20 \cdot \mathrm{~mA}$
b) $50 \cdot \mathrm{~mA}$
$-600 \cdot \frac{\mathrm{~A}}{\mathrm{sec}}$
c) $5 \cdot \mathrm{~V} \quad-75000 \cdot \frac{\mathrm{~V}}{\mathrm{sec}}$
6. a) 20 mA
5 mA 5 mA 10 mA
b) yes, $\mathrm{V}_{\mathrm{D} 1}=0.3 \mathrm{~V}<0.7 \mathrm{~V}$
c) yes, $\mathrm{I}_{\mathrm{D} 2}=10 \mathrm{~mA}>0$

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9. a) $31 \mathrm{~mA} \quad 775 \mathrm{~mA} \quad 7.75 \mathrm{~V} \quad 2.25 \mathrm{~V} \quad 1.744 \mathrm{~W}$
b) yes, $\mathrm{V}_{\mathrm{EC}}=2.25 \mathrm{~V}>0.2 \mathrm{~V}$
c) $237 \Omega$
$\begin{array}{lll}\text { d) } 31.6 & \text { e) } 0.196 \mathrm{~W} & \text { f) } 0\end{array}$

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Name
Scores:

| pages 1-2 | / 29 pts |
| :---: | :---: |
| pages 3-4 | / 30 pts |
| pages 5-6 | / 31 pts |
| pages 7-8 | / 36 pts |
| pgs 9-10 | / 27 pts |
| pgs 11-12 | / 27 pts |

Total $\qquad$ / 180 pts
8.

$\mathrm{V}_{\mathrm{o} 2}(\mathrm{t})$

$\mathrm{V}_{03}(\mathrm{t})$

$\mathrm{V}_{\mathrm{o4}}(\mathrm{t})$
(V)


