## ECE2210 Final given: Fall 11

1. (20 pts)
a) Find $\mathbf{V}_{\text {in }}$ in polar form.
b) Find $\mathbf{I}_{\mathbf{T}}$.
c) Circle 1:
i) The source current leads the source voltage
ii) The source voltage leads the source current

d) By how much? I.E. what is the phase angle between the voltage and current?
2. ( 15 pts ) a) Find the s-type transfer function of the circuit shown. Consider $\mathbf{I}_{\text {in }}$ as the input and $\mathrm{I}_{\mathbf{O}}$ as the "output".

You MUST show work to get credit. Simplify your expression for $\mathrm{H}(\mathrm{s})$ so that the denominator is a simple polynomial with no coefficient before the highest-order sterm in the denominator.

$$
\mathbf{H}(\mathrm{s})=\text { ? }
$$


b) How many zeroes does this transfer function have?
c) How many poles does this transfer function have?
3. (31 pts) A transformer is rated at $1000 \mathrm{~V} / 200 \mathrm{~V}$, 1 kVA . Assume the transformer is ideal and all voltages and currents are RMS.
a) The primary has 250 turns of wire. How many turns does the secondary have?
$\mathrm{f}:=60 \cdot \mathrm{~Hz}$

b) The the source voltage, $\mathbf{V}_{\mathbf{S}}=600 \cdot \mathrm{~V}$ How big is voltage across the load $\left(\left|\mathbf{V}_{\mathbf{2}}\right|\right)$ ?
pf $:=82 . \%$ leading
c) The secondary load draws 720 VA of apparent power at a power factor of $82 \%$. Find the secondary load, $\mathbf{Z}_{\mathbf{L}}$ (magnitude and angle).
d) Find the primary current, $\mathbf{I}_{1}$ (magnitude and angle).
e) What is the load as seen by $\mathbf{V}_{\mathbf{S}}$ ? (magnitude and angle)
f) How much average power does the load dissipate?
g) How much average power does the power source $\left(\mathbf{V}_{\mathbf{S}}\right)$ supply?
h) Is this transformer operating within its ratings?

How do you know? (Specifically show a values which are or are not within a correct range.)
Within range? yes no (circle one)
i) Using the given load voltage and power factor, what is the smallest load impedance magnitude that you could hook to this transformer and still operate within its ratings? $\quad\left|\mathbf{Z}_{\mathbf{L m i n}}\right|=$ ?
j) $\mathbf{Z}_{\mathbf{L}}$ is that found in part c). Add a component to the secondary side of the transformer so as to minimize the currents. Do not change the real power delivered to the load. Draw the part on the drawing and find its value.
k) Is this transformer operating within its ratings with this new part?

How do you know? (Specifically show a values which are or are not within a correct range.)

## ECE2210 Final given: Fall 11 p2

4. (31 pts) The same input signal (at right) is connected to several op-amp circuits below. Sketch the output waveform for each circuit. Clearly label important voltage levels on each output. If I can't easily make out what your peak values are, l'll assume you don't know. Don't forget to show inversions. The op-amp is connected to $+12 \mathrm{~V} \&-12 \mathrm{~V}$ power supplies.
a)

b) $\quad \mathrm{R}_{2}:=7 \cdot \mathrm{k} \Omega$



$\mathrm{v}_{\mathrm{od}}(\mathrm{t})$
$(\mathrm{V})$


## ECE2210 Final given: Fall 11 p3

5. ( 34 pts ) A couple of transistors are used to control the current flow through an inductive load. The switch has been closed, as shown, for a long time.
a) Assume both transistors are in saturation. Find the minimum $\beta$ for transistor $Q_{2}$.
$\beta_{2}=$ ?
Hint: You will need to find the voltage at the base of $Q_{2}$. You may assume that $\mathrm{I}_{\mathrm{E}} \simeq \mathrm{I}_{\mathrm{C}}$ for both transistors.
b) Find the minimum $\beta$ for transistor $Q_{1}$ to be in saturation.

$$
\beta_{1 \min }=\text { ? }
$$

c) Something is wrong. Transistor $Q_{2}$ is getting too hot. You measure the voltage across the load and find that $\mathrm{V}_{\mathrm{L}}:=4 \cdot \mathrm{~V}$.
How much power is being dissipated in transistor $\mathrm{Q}_{2}$ ?
d) Next you measure the voltage at the collector of $\mathrm{Q}_{1}$ and find that $\mathrm{V}_{\mathrm{C} 1}:=8.1$ with respect to ground.
Find the actual $\beta s$ of both transistors and tell me what's wrong.
You replace the faulty component and everything is back to the way is was in part a)

e) The diode in this circuit conducts a significant current: (circle one)
A) never.
D) always.
B) when the switch closes.
E) when the switch opens.
C) whenever the switch is closed.
F) whenever the switch is open.
g) What is the maximum diode current you expect when the switch is cycled. (Answer 0 if it never conducts.)

Use constant-voltage-drop models for the diodes and LEDs on this exam.
6. ( 32 pts ) Assume that diodes $\mathrm{D}_{1}$ and $\mathrm{D}_{4}$ DO conduct. Assume that diodes $\mathrm{D}_{2}$ and $\mathrm{D}_{3}$ do NOT conduct.
a) Stick with these assumptions even if your answers come out absurd. Find the following and anything else you need in order to check the assumptions:
$\mathrm{I}_{\mathrm{R} 1}=\quad \mathrm{I}_{\mathrm{R} 2}=$ $\qquad$
$\mathrm{I}_{\mathrm{D} 1}=$ $\qquad$ $\mathrm{V}_{\mathrm{R} 4}=$ $\qquad$
b) Was the assumption about $\mathrm{D}_{1}$ correct? yes

How do you know? (Show a value \& range.)
(circle one)
c) Was the assumption about $\mathrm{D}_{2}$ correct? yes no How do you know? (Show a value \& range.)
d) Was the assumption about $\mathrm{D}_{3}$ correct? yes no How do you know? (Show a value \& range.)
e) Was the assumption about $\mathrm{D}_{4}$ correct? yes no How do you know? (Show a value \& range.)

f) Based on your answers to parts b), c), d) \& e), Circle one:
i) The real $\mathrm{I}_{\mathrm{D} 1}<\mathrm{I}_{\mathrm{D} 1}$ calculated in part a. Justify your answer.
ii) The real $\mathrm{I}_{\mathrm{D} 1}=\mathrm{I}_{\mathrm{D} 1}$ calculated in part a.
iii) The real $\mathrm{I}_{\mathrm{D} 1}>\mathrm{I}_{\mathrm{D} 1}$ calculated in part a.

## ECE2210 Final given: Fall 11 p4

7. (17 pts) A voltage waveform (dotted line) is applied to the circuit shown. Accurately draw the output waveform $\left(\mathrm{v}_{\mathrm{o}}\right)$ you expect to see. Label important times and voltage levels.


If you're not specific about your times and


## Answers

1. a) $6 \mathrm{~V} / 53.13^{\circ}$
b) $131 \mathrm{~mA} / 65.5^{\circ}$
c) i)
d) $12.35 \cdot \mathrm{deg}$
2. a) 50
b) $120 \cdot \mathrm{~V}$
c) $20 \Omega /-34.9^{\circ}$
d) $1.2 \mathrm{~A} / 34.9^{\circ}$
3. $\frac{s^{2}+\frac{\mathrm{R}_{3}}{\mathrm{~L}} \cdot \mathrm{~s}+\frac{1}{\mathrm{~L} \cdot \mathrm{C}}}{\mathrm{s}^{2}+\left(\frac{1}{\mathrm{R}_{2} \cdot \mathrm{C}}+\frac{\mathrm{R}_{3}}{\mathrm{~L}}\right) \cdot \mathrm{s}+\frac{1}{\mathrm{~L} \cdot \mathrm{C}} \cdot\left(\frac{\mathrm{R}_{3}}{\mathrm{R}_{2}}+1\right)} \quad$ () 2
$\begin{array}{lll}\text { e) } 500 \Omega /-34.9^{\circ} & \text { f) } \& \text { g) } 590.4 \cdot \text { W } & \text { h) No } 6 \cdot \mathrm{~A}>5 \cdot \mathrm{~A}\end{array}$
i) $24 \cdot \Omega$
j) Add a $92.7-\mathrm{mH}$ inductor in parallel with the load
k) YES
4. a) 10 V to 2 ms , then drops to -5 V , stays there to 6 ms , repeats.
b) -11 V to 2 ms , then rises to 7 V , stays there to 6 ms , repeats.
c) -11 V to 2 ms , then rises to 6 V , stays there to 6 ms , repeats.
d) 0 V at 0 ms , ramps down to -10 V at 2 ms , then ramps up to 0 V at 6 ms , repeats.
5. a) 28 or 29 acceptable ans
b) 177
c) $4 \cdot \mathrm{~W}$
d) 177 and 15.95 or 16.95 acceptable ans $\beta_{2}$ is too low $\quad$ e) $E \quad$ f) $2.9 \cdot \mathrm{~A}$
6. 

a) $16 \cdot \mathrm{~mA}$
$25 \cdot \mathrm{~mA}$
$19 \cdot \mathrm{~mA}$
$1.8 \cdot \mathrm{~V}$
b) yes $\mathrm{I}_{\mathrm{D} 1}=19 \cdot \mathrm{~mA}>0$
c) $\mathrm{no} \mathrm{V}_{\mathrm{D} 2}=1.2 \cdot \mathrm{~V}>0.7 \mathrm{~V}$
d) yes
$\mathrm{V}_{\mathrm{D} 3}=-0.5 \cdot \mathrm{~V}<0.7 \mathrm{~V}$
e) yes $\mathrm{I}_{\mathrm{D} 4}=25 \cdot \mathrm{~mA}>0$
f) iii $D_{2}$ will conduct current, all of which will have to come through $D_{1}$
7. Starts at 0 V , ramps up to 0.7 V at 0.7 ms , ramps up to 1.4 V at 2.1 ms , flat at 1.4 V to 3.5 ms , drops instantly to -3.5 V , ramps up to 0.7 V at 7.7 ms , Finally it ramps toward 1.4 V at 9.1 ms .

