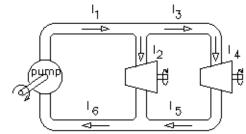
Scan your homework and convert to a pdf file. Turn in on Canvas. Homework is due by 11:59 p.m. on the due date.

The following problems are not meant to be hard. You should be able to do most of them in your head with no special formulas or calculations. In fact you should find them rather dumb and trivial. That's the point, I want to drill these concepts into your head so that you'll find them easy.

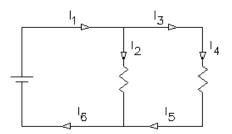
1. The figure at right shows a hydraulic system with a pump that converts rotational energy to fluid energy and two turbines which convert that energy back to rotational energy. Do NOT assume that the turbines are equal in size. This is a closed system containing an incompressible fluid with no places for that fluid to collect; i.e. flow in = flow out of any point or object. Kirchhoff's current law applies. The volumetric fluid flows are indicated by the arrows.  $I_1 := 0.01 \cdot \frac{m^3}{s}$   $I_2 := 0.007 \cdot \frac{m^3}{s}$ 



$$I_{A} =$$

$$I_3 =$$
  $I_4 =$   $I_5 =$   $I_6 =$ 

2. The figure at right shows an electrical circuit with a battery that converts chemical energy to electrical energy and two resistors which convert that electrical energy to heat energy. Do NOT assume that the resistors are equal in size. All electrical circuits are closed systems containing incompressible charges with no places for those charges to collect; i.e. flow in = flow out of any point or object. Kirchhoff's current law applies. . The electrical currents are indicated by the arrows.



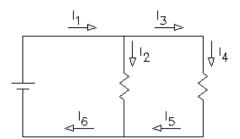
$$I_1 := 0.01 \cdot A$$
  $I_2 := 0.007 \cdot A$ 

$$I_2 = 0.007 \cdot A$$

$$I_A =$$

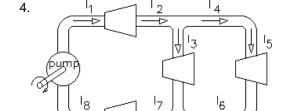
$$I_3 =$$
\_\_\_\_\_  $I_4 =$ \_\_\_\_  $I_5 =$ \_\_\_\_  $I_6 =$ \_\_\_\_

3. The figure at right shows a similar electrical circuit only now the electrical currents are indicated by the arrows next to the wires. This is a more common way to show the current flow because a little arrow in the wire is too easily confused with the electrical symbol for a diode. You'll learn about diodes later.



$$I_2 = 20 \cdot mA$$
  $I_5 = 14 \cdot mA$ 

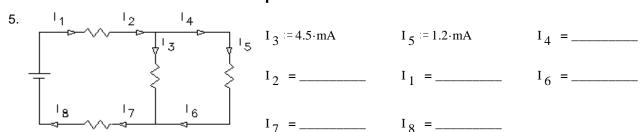
$$I_6 =$$
\_\_\_\_\_  $I_1 =$ \_\_\_\_  $I_3 =$ \_\_\_\_  $I_4 =$ \_\_\_\_



$$I_3 = 0.004 \cdot \frac{m^3}{m^3}$$

$$I_5 := 0.001 \cdot \frac{m^3}{m^3}$$

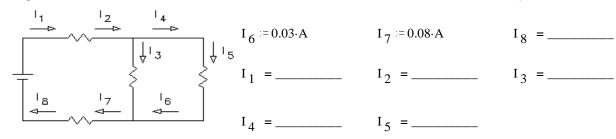
$$I_3 := 0.004 \cdot \frac{m^3}{s}$$
  $I_5 := 0.001 \cdot \frac{m^3}{s}$   $I_4 =$ 



$$I_3 = 4.5 \cdot mA$$

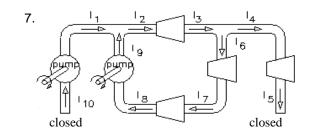
$$I_5 = 1.2 \cdot mA$$

6. Again, a similar electrical circuit with the electrical current arrows in the more common position, next to the wires.



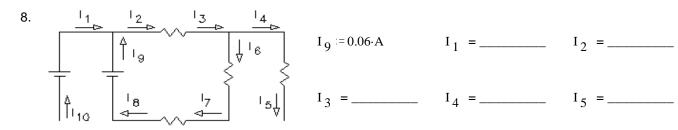
$$I_6 = 0.03 \cdot A$$

$$I_7 = 0.08 \cdot A$$

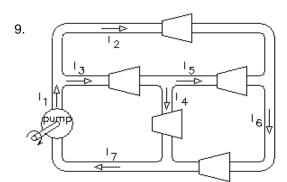


$$I_9 = 0.04 \cdot \frac{m^3}{s}$$
  $I_1 = 1_2 = 1_2 = 1_3 = 1_4 = 1_5$ 

$$I_6 = _{---}$$
  $I_7$ 



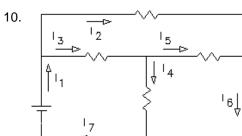
$$I_9 = 0.06 \cdot A$$



$$I_4 := 0.05 \cdot \frac{m^3}{s}$$

$$I_4 := 0.05 \cdot \frac{m^3}{s}$$
  $I_5 := 0.014 \cdot \frac{m^3}{s}$   $I_6 := 0.03 \cdot \frac{m^3}{s}$ 

$$I_6 := 0.03 \cdot \frac{m^3}{s}$$

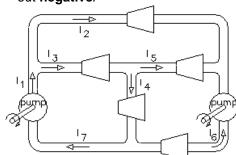


$$I_4 := 20 \cdot mA$$
  $I_5 := 10 \cdot mA$   $I_6 := 22 \cdot mA$ 

$$I_5 = 10 \cdot mA$$

$$I_6 = 22 \cdot mA$$

11. Careful here, there are now two pumps. Also, given the flow arrows shown, one or more of the flows must come out negative.



$$I_2 := 0.005 \cdot \frac{m^3}{s}$$
  $I_6 := 0.03 \cdot \frac{m^3}{s}$   $I_7 := 0.015 \cdot \frac{m^3}{s}$ 

$$I_6 := 0.03 \cdot \frac{m^3}{s}$$

$$I_7 := 0.015 \cdot \frac{m^3}{s}$$

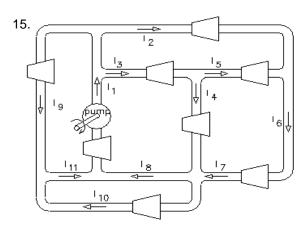
12. What does a negative fluid flow physically mean?

$$I_1 := 0.01 \cdot A$$
  $I_5 := -20 \cdot mA$   $I_6 := 35 \cdot mA$ 

$$I_5 = -20 \cdot m$$

$$I_6 = 35 \cdot mA$$

14. What does a negative electrical current physically mean?

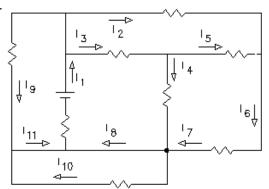


$$I_4 = 0.05 \cdot \frac{m^3}{s}$$

$$I_4 := 0.05 \cdot \frac{m^3}{s}$$
  $I_5 := 0.03 \cdot \frac{m^3}{s}$   $I_7 := 0.045 \cdot \frac{m^3}{s}$ 

$$I_7 := 0.045 \cdot \frac{m^3}{s}$$

$$I_9 = 0.06 \cdot \frac{m^3}{s}$$

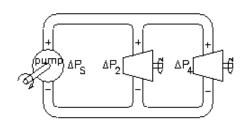


 $I_1 = 100 \cdot \text{mA}$   $I_2 = 50 \cdot \text{mA}$   $I_3 = 30 \cdot \text{mA}$ 

$$I_2 := 50 \cdot mA$$

$$I_{6} = 66 \cdot mA$$

17. The figure at right shows the pressure differentials across elements in a hydraulic system. The side indicated by the + sign is the higher pressure side. Conversely, - indicates the lower pressure.  $\Delta P_S$  is the pressure difference supplied by the pump (S for  $\underline{\mathbf{S}}$  ource).  $\Delta P_2$  is the pressure difference driving the left turbine and  $\Delta P_4$  is the pressure difference driving the right turbine. Assume no pressure losses or discontinuities in the pipes, joints, or corners; i.e. all connected pipes are at exactly the same pressure. Finally, the fluid has no mass, so gravity and Bernoulli can go take a hike.



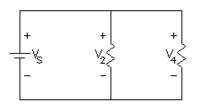
$$\Delta P_S := 12 \cdot \frac{N}{m^2} = 12 \cdot Pa$$

$$\Delta P_2 =$$

$$\Delta P_4 =$$

Yes, I know that these are ridiculously low pressures for a hydraulic system.

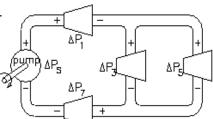
18. The figure at right shows the voltage differentials across elements in an electrical circuit. The side indicated by the + sign is the higher voltage side. Conversely, - indicates the lower voltage.  $V_S$  is the voltage supplied by the battery. V2 is the voltage across the left resistor and V4 is the voltage across the right resistor. You may assume no voltage drops across any of the wires or connections in practically all electrical schematics; i.e. all connected wires are at exactly the same voltage (electrical potential).





$$(V = volts)$$

19.

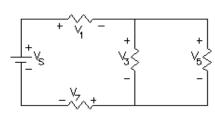


$$\Delta P_S := 400 \cdot kPa$$
  $\Delta P_1 := 180 \cdot kPa$   $\Delta P_3 := 100 \cdot kPa$ 

$$\Delta P_2 = 100 \cdot kPa$$

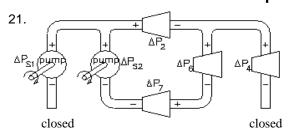
$$\Delta P_7 =$$

20.



$$V_1 := 10 \cdot V$$
  $V_5 := 3 \cdot V$   $V_7 := 2 \cdot V$ 

$$V_{\pi} = 2 \cdot V$$



$$\Delta P_{S1} := 200 \cdot kPa$$
  $\Delta P_{S2} := 150 \cdot kPa$   $\Delta P_{2} := 50 \cdot kPa$   $\Delta P_{6} := 60 \cdot kPa$ 

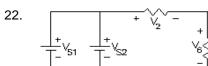
$$\Delta P_{S2} := 150 \cdot kP$$

$$\Delta P_2 := 50 \cdot kPa$$

$$\Delta P_6 := 60 \cdot kP$$

$$\Delta P_4 =$$

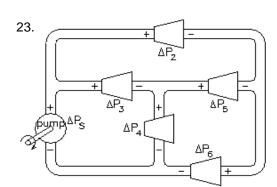
$$\Delta P_7 =$$



$$V_{S1} := 6 \cdot V$$

$$V_2 := 2 \cdot V$$

$$v_{S1} := 6 \cdot v$$
  $v_2 := 2 \cdot v$   $v_6 := 2.4 \cdot v$   $v_7 := 3.2 \cdot v$ 



$$\Delta P_3 := 120 \cdot kPa$$
  $\Delta P_4 := 80 \cdot kPa$   $\Delta P_6 := 110 \cdot kPa$ 

$$\Delta P_A := 80 \cdot kPa$$

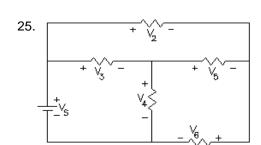
$$\Delta P_{\epsilon} := 110 \cdot kPa$$

$$\Delta P_S =$$

$$\Delta P_2 =$$

$$\Delta P_5 =$$

### 24. What does a negative pressure difference physically mean?

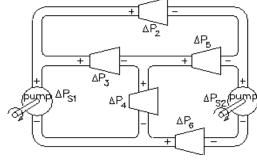


$$V_3 := 2.3 \cdot V_3$$

$$V_5 = 0.5 \cdot V$$

$$V_3 := 2.3 \cdot V$$
  $V_5 := 0.5 \cdot V$   $V_6 := 3.2 \cdot V$ 

#### 26. Watch your + and - signs very carefully now.



$$\Delta P_2 := 140 \cdot kPa$$
  $\Delta P_3 := 230 \cdot kPa$   $\Delta P_4 := 50 \cdot kPa$   $\Delta P_6 := 210 \cdot kPa$ 

$$\Delta P_a := 230 \cdot kP$$

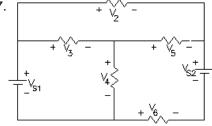
$$\Delta P_A := 50 \cdot kPa$$

$$\Delta P_6 = 210 \cdot kPa$$

$$\Delta P_{S1} =$$

$$\Delta P_{S2} =$$

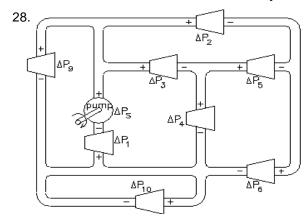




$$v_{S1} := 14 \cdot v - v_{S2} := 3 \cdot v - v_{2} := 6 \cdot v - v_{3} := 4 \cdot v$$

$$V_3 := 4 \cdot V$$

Think about the current through the 2nd battery. What is happening to that battery?



$$\Delta P_1 := 200 \cdot kPa$$

$$\Delta P_3 := 600 \cdot kPa$$

$$\Delta P_2 := 1100 \cdot kPa$$

$$\Delta P_9 := 1800 \cdot kPa$$

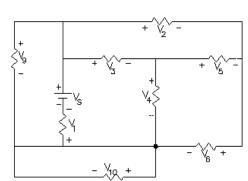
$$\Delta P_S =$$

$$\Delta P_A =$$

$$\Delta P_5 =$$

$$\Delta P_6 = \underline{\hspace{1cm}}$$

$$\Delta P_{10} =$$
\_\_\_\_\_



$$V_{c} := 18.V$$

$$V_S := 18 \cdot V$$
  $V_3 := 6 \cdot V$ 

$$V_A := 8 \cdot V$$

$$V_4 := 8 \cdot V$$
  $V_5 := 2 \cdot V$ 

**1.** 
$$I_3 = I_4 = I_5 = 0.003 \cdot \frac{m^3}{s}$$
,  $I_6 = 0.01 \cdot \frac{m^3}{s}$ 
**2.**  $I_3 = I_4 = I_5 = 0.003 \cdot A$ ,  $I_6 = 0.01 \cdot A$ 

**3.** 
$$I_6 = I_1 = 34 \cdot \text{mA}$$
,  $I_3 = I_4 = 14 \cdot \text{mA}$ 

**5.** 
$$I_4 = I_6 = 1.2 \cdot \text{mA}$$
,  $I_1 = I_2 = I_7 = I_8 = 5.7 \cdot \text{mA}$ 

7 L<sub>1</sub>= L<sub>2</sub>= L<sub>3</sub>= L<sub>4</sub>= 
$$\frac{1}{1}$$
 L<sub>2</sub>= L<sub>3</sub>= L<sub>4</sub>= L<sub>5</sub>= 0.

**2.** 
$$I_3 = I_4 = I_5 = 0.003 \cdot A$$
 ,  $I_6 = 0.01 \cdot A$ 

3. 
$$I_6 = I_1 := 34 \cdot \text{mA}$$
,  $I_3 = I_4 := 14 \cdot \text{mA}$ 
4.  $I_4 = I_6 := 0.001 \cdot \frac{\text{m}^3}{\text{s}}$ ,  $I_1 = I_2 = I_7 = I_8 := 0.005 \cdot \frac{\text{m}^3}{\text{s}}$ 

**5.** 
$$I_4 = I_6 := 1.2 \cdot \text{mA}$$
,  $I_1 = I_2 = I_7 = I_8 := 5.7 \cdot \text{mA}$  **6.**  $I_1 = I_2 = I_8 := 80 \cdot \text{mA}$ ,  $I_3 := 50 \cdot \text{mA}$ ,  $I_4 = I_5 := 30 \cdot \text{mA}$ 

7. 
$$I_1 = I_{10} = I_4 = I_5 := 0 \cdot \frac{m^3}{s}$$
,  $I_2 = I_3 = I_7 = I_8 := 0.04 \cdot \frac{m^3}{s}$ 

$$I_1 = I_{10} = I_4 = I_5 := 0 \cdot A$$
,  $I_2 = I_3 = I_7 = I_8 := 0.06 \cdot A$ 

$$I_2 = I_3 = I_7 = I_8 = 0.06 \cdot A$$

**9.** 
$$I_1 = I_7 = 0.080 \cdot \frac{m^3}{s}$$
,  $I_2 = 0.016 \cdot \frac{m^3}{s}$ ,  $I_3 = 0.064 \cdot \frac{m^3}{s}$ 
**10.**  $I_1 = I_7 = 42 \cdot mA$ ,  $I_2 = 12 \cdot mA$ ,  $I_3 = 30 \cdot mA$ 

**10.** 
$$I_1 = I_7 = 42 \cdot \text{mA}$$
 ,  $I_2 = 12 \cdot \text{mA}$  ,  $I_3 = 30 \cdot \text{mA}$ 

11. 
$$I_1 := 0.015 \cdot \frac{m^3}{s}$$
,  $I_3 := 0.010 \cdot \frac{m^3}{s}$ ,  $I_4 := 0.045 \cdot \frac{m^3}{s}$ ,  $I_5 := -0.035 \cdot \frac{m^3}{s}$ 

12. Actual flow is in direction opposite to the arrow direction.

13.  $I_2 := -15 \cdot mA$ ,  $I_3 := 25 \cdot mA$ ,  $I_4 := 45 \cdot mA$ ,  $I_7 := 10 \cdot mA$ 

**13.** 
$$I_2 := -15 \cdot \text{mA}$$
,  $I_3 := 25 \cdot \text{mA}$ ,  $I_4 := 45 \cdot \text{mA}$ ,  $I_7 := 10 \cdot \text{mA}$ 

**15.** 
$$I_1 := 0.155 \cdot \frac{m^3}{s}$$
,  $I_2 := 0.015 \cdot \frac{m^3}{s}$ ,  $I_3 := 0.080 \cdot \frac{m^3}{s}$ ,  $I_6 := 0.045 \cdot \frac{m^3}{s}$ ,  $I_8 := 0.095 \cdot \frac{m^3}{s}$ ,  $I_{10} := 0 \cdot \frac{m^3}{s}$ ,  $I_{11} := 0.060 \cdot \frac{m^3}{s}$   
**16.**  $I_4 := 14 \cdot mA$ ,  $I_5 := 16 \cdot mA$ ,  $I_7 := 66 \cdot mA$ ,  $I_8 := 80 \cdot mA$ ,  $I_9 := 20 \cdot mA$ ,  $I_{10} := 0 \cdot mA$ ,  $I_{11} := 20 \cdot mA$ 

**16.** 
$$I_4 := 14 \cdot \text{mA}$$
,  $I_5 := 16 \cdot \text{mA}$ ,  $I_7 := 66 \cdot \text{mA}$ ,  $I_8 := 80 \cdot \text{mA}$ ,  $I_9 := 20 \cdot \text{mA}$ ,  $I_{10} := 0 \cdot \text{mA}$ ,  $I_{11} := 20 \cdot \text{mA}$ 

**17.** 
$$\Delta P_2 = \Delta P_4 := 12 \cdot Pa$$

**18.** 
$$V_2 = V_4 := 12 \cdot V$$

**19.** 
$$\Delta P_5 = 100 \cdot kPa$$
 ,  $\Delta P_7 = 120 \cdot kPa$ 

**20.** 
$$V_S := 15 \cdot V$$
 ,  $V_3 := 3 \cdot V$ 

**21.** 
$$\Delta P_4 = 0 \cdot kPa$$
,  $\Delta P_7 = 40 \cdot kPa$ 

**22.** 
$$V_{S2} = 7.6 \cdot V$$
,  $V_4 = 0 \cdot V$ 

**23.** 
$$\Delta P_S = 200 \cdot kPa$$
 ,  $\Delta P_2 = 90 \cdot kPa$  ,  $\Delta P_5 = -30 \cdot kPa$ 

**25.** 
$$V_S := 6 \cdot V$$
 ,  $V_2 := 2.8 \cdot V$  ,  $V_4 := 3.7 \cdot V$ 

**26.** 
$$\Delta P_{S1} = 280 \cdot kPa$$
,  $\Delta P_{S2} = 350 \cdot kPa$ ,  $\Delta P_{5} = -90 \cdot kPa$ 

**27.** 
$$V_4 := 10 \cdot V$$
,  $V_5 := 2 \cdot V$ ,  $V_6 := -5 \cdot V$  battery is charging

**27.** 
$$V_4 := 10 \cdot V$$
,  $V_5 := 2 \cdot V$ ,  $V_6 := -5 \cdot V$  battery is charging **28.**  $\Delta P_S := 2000 \cdot kPa$ ,  $\Delta P_4 := 1200 \cdot kPa$ ,  $\Delta P_5 := 500 \cdot kPa$ ,  $\Delta P_{10} := 0 \cdot kPa$ 

**29.** 
$$V_1 := 4 \cdot V$$
 ,  $V_2 := 8 \cdot V$  ,  $V_6 := 6 \cdot V$  ,  $V_9 := 14 \cdot V$ ,  $V_{10} := 0 \cdot V$