

Problem 1 - (30 points)

Solution

Use: ignore r_o , $|V_{BE}|=0.7$, $\beta=100$
 $V_I = 20 + 0.001\sin(20t)$

For DC analysis, assume that the capacitors are open

(a) Solve for the DC currents:

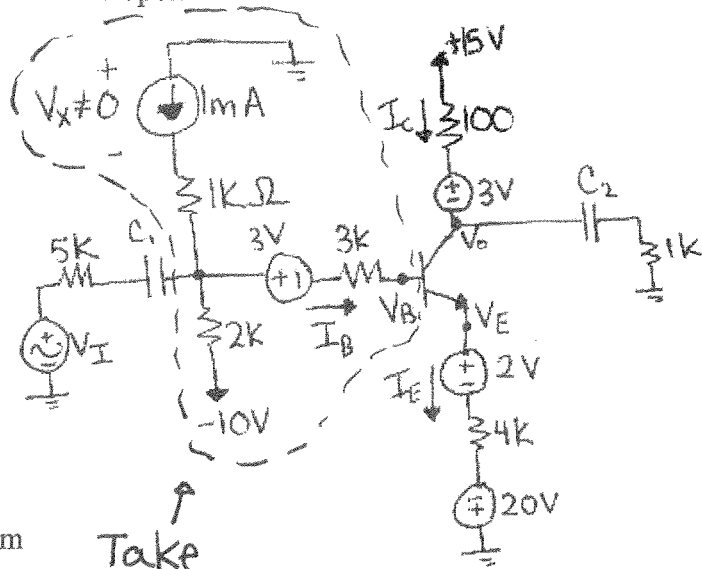
- a. $I_B = 15.6 \mu A$
- b. $I_E = 1.58 mA$
- c. $I_C = 1.56 mA$

(b) Solve for the DC voltages:

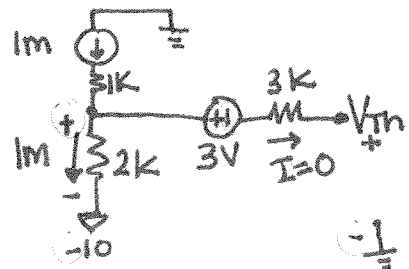
- a. $V_B = -11.08 V$
- b. $V_E = -11.78 V$
- c. $V_o = +11.08 V$

(c) What region of operation is this transistor acting? **ACTIVE**

(d) Sketch the total instantaneous waveform observed for V_o if $V_o/V_I = 5V/V$.



Take Thevenin at the base

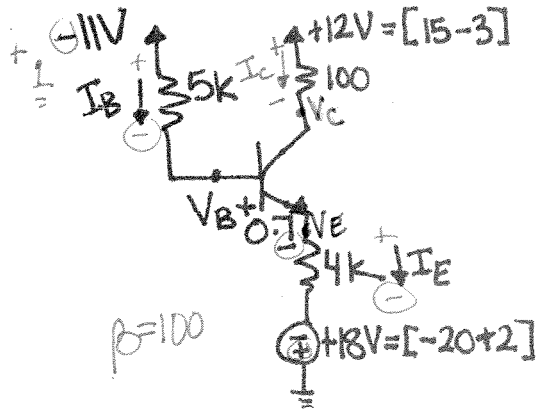


$$-10 + I(2k) - 3 - V_{Th} = 0$$

$$V_{Th} = -3 + I(2k) = -11V$$

$$R_{Th} = 3k + 2k = 5k$$

(Note that 1mA becomes an open)



$$-11 - I_B(5k) - 0.7 - I_E(4k) + 18 = 0$$

$$I_B = \frac{I_E}{\beta + 1}$$

$$\frac{(+18 - 11.7)}{\frac{5k}{101} + 4k} = I_E \approx \frac{6.3}{4k} \approx 1.58 mA$$

$$I_B = \frac{I_E}{101} = \frac{1.58m}{101} = 15.6 \mu A$$

$$I_C = \beta I_B = 1.56 mA$$

Problem 1: (extra page)

$$-11 - I_B(5K) - V_B = 0$$

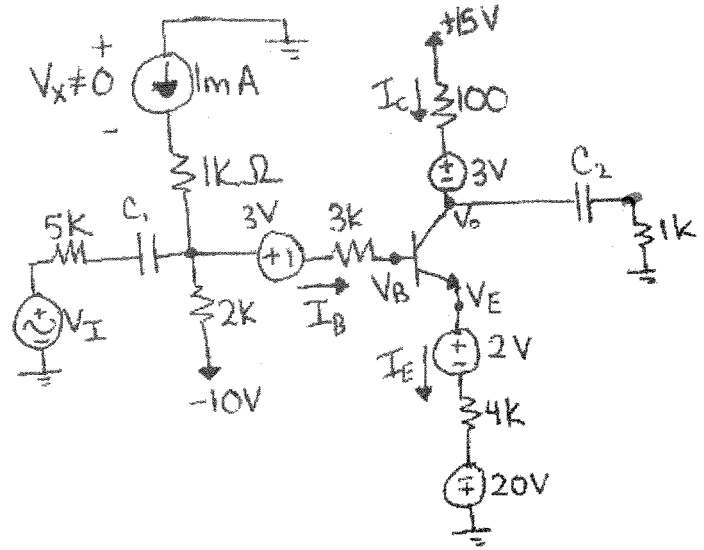
$$V_B = -11 - I_B(5K) = \underline{-11.08V}$$

$$V_E = V_B - 0.7 = \underline{-11.78V}$$

$$V_C = +12 - I_C(100) = \underline{+11.8V}$$

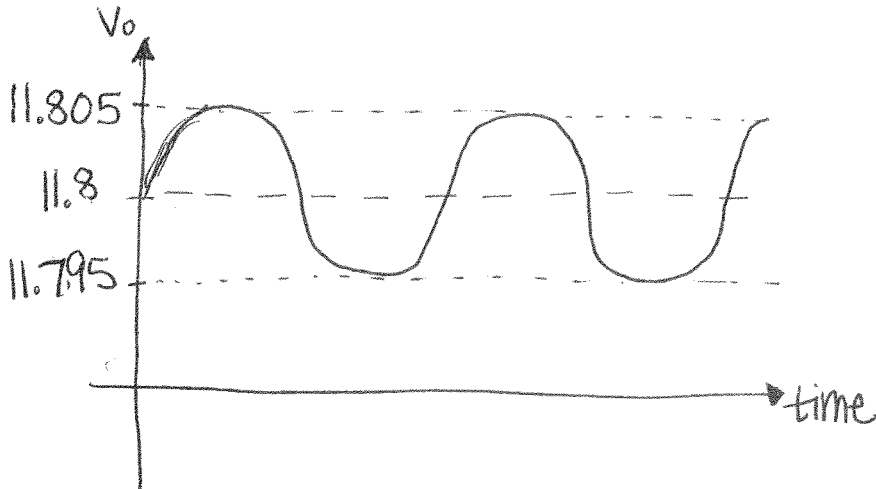
$$V_C = V_o = 11.8 > V_B = -11.08 \checkmark$$

∴ Acting in Active mode



For $\frac{V_o}{V_I} = 5 \text{ V/V}$ then $V_{oAC} = 1m(5)\sin(20t) = 5m\sin(20t)$

$$V_{o\text{ total}} = V_{oDC} + V_{oAC} = 11.8 + 5m\sin(20t)$$



Problem 2 – (30 points)

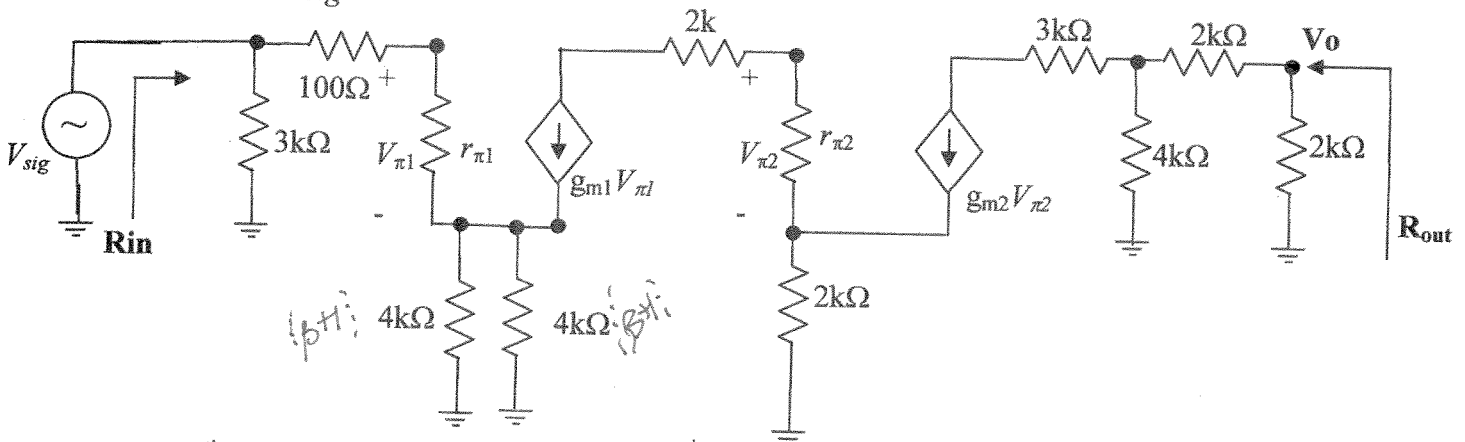
Use: ignore r_o and r_x , $|V_{BE}|=0.7$, $\beta=100$, $V_T=25\text{mV}$
 $V_I = 10+0.002\sin(20t)$

$$g_{m1} = \frac{\beta}{r_{\pi1}} = \frac{100}{1,200} = 83.3\text{m}$$

$$r_{\pi1}=1,200 \quad g_{m2}=25\text{mA/V}, \text{ and } I_{B2}=6.25\mu; \quad r_{\pi2} = \frac{\beta}{g_m} = \frac{100}{25\text{m}} = 4\text{K} \text{ or } r_{\pi2} = \frac{V_T}{I_B} = \frac{25\text{m}}{6.25\mu}$$

For the following hybrid- π equivalent circuit below, find the following values:

- (a) R_{in} (input resistance –ignore only the input source, V_{sig} and include all resistors at the base)
 (b) R_{out} (output resistance-include **all** resistors at the collector{no load is connected})
 (c) midband gain, $\frac{V_o}{V_{sig}}$



$$R_{in} = 3k \parallel [100 + r_{\pi1} + 2k(\beta+1)]$$

$$R_{in} = 3k \parallel 203.3k = \boxed{2.96k\Omega}$$

$$R_{out} = 2k \parallel (2k + 4k) = 2k \parallel 6k$$

$$R_{out} = \boxed{1.5k\Omega}$$

$$V_o = \left[\underbrace{-g_{m2} V_{\pi2} (4k)}_{I} \right] \cdot 2k = -25\text{m} \cdot 1k V_{\pi2} = -25 V_{\pi2}$$

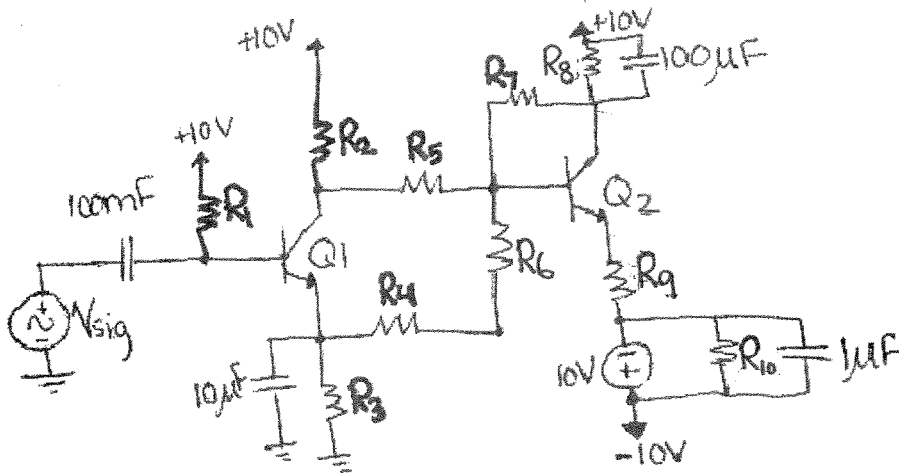
$$V_{\pi2} = -g_{m1} V_{\pi1} \cdot r_{\pi2} = -\underbrace{\frac{\beta}{1,200}}_{83.3\text{m}} \cdot V_{\pi1} \cdot 4k = -333 V_{\pi1}$$

$$V_{\pi1} = \frac{V_{sig} (r_{\pi1})}{100 + r_{\pi1} + 2k(\beta+1)} = \frac{V_{sig} (1,200)}{203.3k} = 5.9\text{m} V_{sig}$$

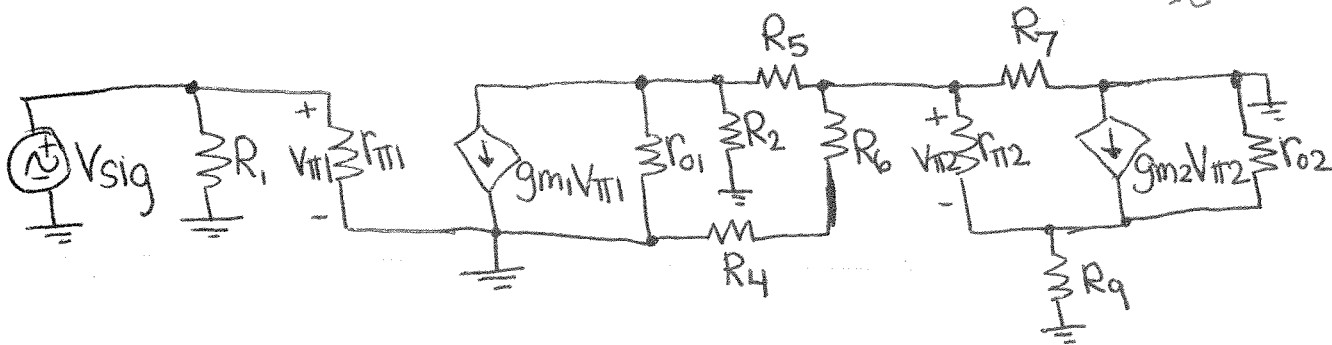
$$\frac{V_o}{V_{sig}} = -25 (-333) (5.9\text{m}) V_{sig} \cong \boxed{+49\%}$$

Problem 3 – (15 points)

For the circuit shown below, draw the AC small-signal equivalent circuit (use hybrid- π or model T). Make sure that everything is labeled in terms of the transistor number. (e.g. g_{m1} , $v_{\pi 2}$, etc.). Include r_o for all transistors. $v_{sig} = 0.001 \sin(10t)$ AC. Assume that the capacitors act as a short.

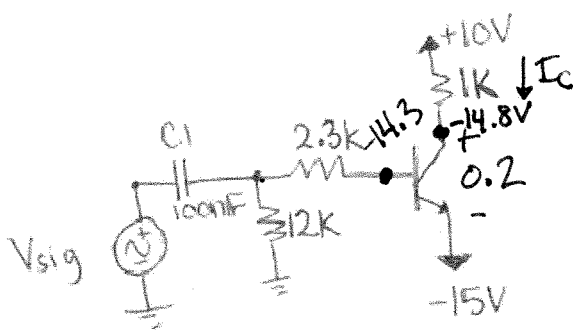


$$r_o = \frac{V_A}{I_C}$$



Problem 5

$|V_{BE}|=0.7$, $\beta=100$, $V_T=25\text{mV}$, ignore r_o , and r_x , $v_{sig}=\{2+0.1\sin(\omega t)\}$ Volts. Assume that the capacitor acts as an open for DC operation and short for AC operation. Does this circuit operate as a **linear** AC amplifier? If so, what is the gain, $\frac{V_o}{V_{sig}}$, of the following circuit? **If not, explain why.** Assume output is taken at collector of transistor. If in saturation, use the datasheet values to determine β_{forced} . $V_{CESAT}=0.2\text{V}$



$$I_c = 100\text{m} = \beta I_B$$

$$I_B = \frac{14.3}{14.3\text{k}} = 1\text{m}$$

$$V_c = 10 - 1\text{k}(100\text{m}) = -90\text{V} !$$

$V_c < V_B \therefore$ NOT ACTIVE

$$I_B = 1\text{m}, V_B = -14.3\text{V}$$

$$I_c = \frac{10 - (-14.8)}{1\text{k}} = \frac{24.8}{1\text{k}} = 24.8\text{m}$$

$$\beta_{forced} = \frac{I_c}{I_B} = \frac{24.8\text{m}}{1\text{m}} = 24.8 < 100$$

\therefore SAT