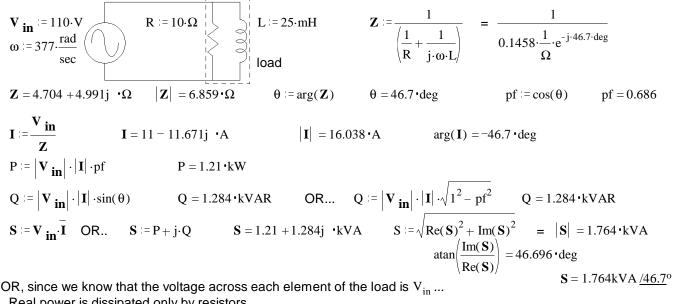
## ECE 3600

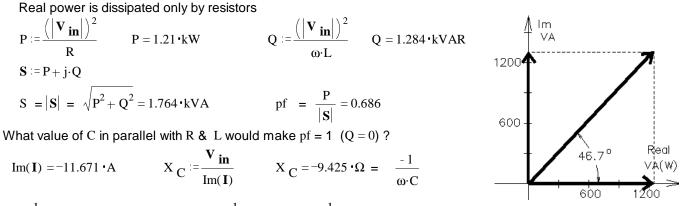
# **AC Power Examples**

A.Stolp 11/06/02 rev 8/28/20

**Ex. 1** R & L together are the load. Find the real power P, the reactive power Q, the complex power S, the apparent power |S|, & the power factor pf. Draw phasor diagram for the power.



OR, since we know that the voltage across each element of the load is V<sub>in</sub> ... Real power is dissipated only by resistors



$$\frac{1}{|X_{C}| \cdot \omega} = 281 \cdot \mu F \quad \text{OR..} \quad \omega = \frac{1}{\sqrt{L \cdot C}} \quad C := \frac{1}{L \cdot \omega^{2}} \quad C = 281 \cdot \mu F$$

**Ex. 2** R & L together are the load. Find the real power P, the reactive power Q, the complex power S, the apparent power |S|, & the power factor pf. Draw phasor diagram for the power.

Series R & L  

$$\mathbf{V}_{in} := 110 \cdot \mathbf{V}_{\omega}$$
  
 $\omega := 377 \cdot \frac{rad}{sec}$ 
 $\mathbf{I} := 25 \cdot mH$ 
 $\mathbf{H} := arg(\mathbf{Z})$ 
 $\mathbf{U} := 13.742 \cdot \Omega$   
 $\mathbf{I} := \frac{\mathbf{V}_{in}}{\mathbf{Z}}$ 
 $\mathbf{I} = 5.825 - 5.49\mathbf{j} \cdot \mathbf{A}$   
 $|\mathbf{I}| = 8.005 \cdot \mathbf{A}$ 
 $arg(\mathbf{I}) = -43.304 \cdot deg$ 
 $\mathbf{P} := |\mathbf{V}_{in}| \cdot |\mathbf{I}| \cdot pf$ 
 $\mathbf{P} = 0.641 \cdot kW$   
 $\mathbf{Q} := |\mathbf{V}_{in}| \cdot |\mathbf{I}| \cdot sin(\theta)$ 
 $\mathbf{Q} = 0.604 \cdot kVAR$   
 $\mathbf{S} := \mathbf{V}_{in} \cdot \mathbf{\bar{I}}$ 
 $\mathbf{S} = 0.641 + 0.604\mathbf{j} \cdot kVA$   
 $|\mathbf{S}| = 0.881 \cdot kVA$ 
 $arg(\mathbf{S}) = 43.304 \cdot deg$ 
 $\mathbf{S} = 881VA/43.3^{\circ}$ 
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# ECE 3600 AC Power Examples, p.2

OR, if we first find the magnitude of the current which flows through each element of the load...

$$|\mathbf{I}| = \frac{\mathbf{V}_{\mathbf{in}}}{\sqrt{\mathbf{R}^2 + (\omega \cdot \mathbf{L})^2}} = 8.005 \cdot \mathbf{A}$$

$$\mathbf{P} := (|\mathbf{I}|)^2 \cdot \mathbf{R} \qquad \mathbf{P} = 0.641 \cdot \mathbf{kW} \qquad \mathbf{Q} := (|\mathbf{I}|)^2 \cdot (\omega \cdot \mathbf{L}) \qquad \mathbf{Q} = 0.604 \cdot \mathbf{kVAR}$$

$$\mathbf{S} := \mathbf{P} + \mathbf{j} \cdot \mathbf{Q} \qquad |\mathbf{S}| = \sqrt{\mathbf{P}^2 + \mathbf{Q}^2} = 0.881 \cdot \mathbf{kVA} \qquad \mathbf{pf} = \frac{\mathbf{P}}{|\mathbf{S}|} = 0.728$$
What value of C in parallel with R & L would make pf = 1 (Q = 0)?  

$$\mathbf{Q} = 603.9 \cdot \mathbf{VAR} \qquad \text{so we need:} \qquad \mathbf{Q}_{\mathbf{C}} := -\mathbf{Q} \qquad \mathbf{Q}_{\mathbf{C}} = -603.9 \cdot \mathbf{VAR} = \frac{\mathbf{V}_{\mathbf{in}}^2}{\mathbf{X}_{\mathbf{C}}}$$

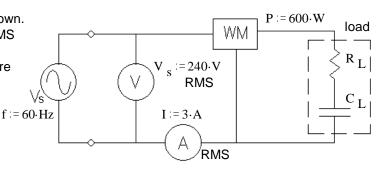
$$X_{C} := \frac{V_{in}^{2}}{Q_{C}} \qquad X_{C} = -20.035 \cdot \Omega = \frac{-1}{\omega \cdot C} \qquad C := \frac{1}{|X_{C}| \cdot \omega} \qquad C = 132 \cdot \mu F$$

Check: 
$$\frac{1}{\frac{1}{R+j\cdot\omega\cdot L}+j\cdot\omega\cdot C} = 18.883\cdot\Omega$$
 No j term, so  $\theta = 0^{\circ}$ 

- Ex. 3 R, & C together are the load in the circuit shown. The RMS voltmeter measures 240 V, the RMS ammeter measures 3 A, and the wattmeter measures 600 W. Find the following: Be sure to show the correct units for each value.
  - a) The value of the load resistor.  $R_L = ?$

$$P = I^2 \cdot R_L$$

$$R_{L} = \frac{P}{I^{2}} \qquad R_{L} = 66.7 \cdot \Omega$$



- b) The apparent power.  $|\mathbf{S}| = ?$   $\mathbf{S} := \mathbf{V}_{\mathbf{S}} \cdot \mathbf{I}$   $\mathbf{S} = 720 \cdot \mathbf{VA}$ c) The reactive power.  $\mathbf{Q} = ?$   $\mathbf{Q} := -\sqrt{\mathbf{S}^2 - \mathbf{P}^2}$   $\mathbf{Q} = -398 \cdot \mathbf{VAR}$ d) The complex power.  $\mathbf{S} = ?$   $\mathbf{S} := \mathbf{P} + \mathbf{j} \cdot \mathbf{Q}$   $\mathbf{S} = 600 - 398\mathbf{i} \cdot \mathbf{VA}$ e) The power factor.  $\mathbf{pf} = ?$   $\mathbf{pf} := \frac{\mathbf{P}}{\mathbf{V}_{\mathbf{S}} \cdot \mathbf{I}}$   $\mathbf{pf} = 0.833$
- f) The power factor is leading or lagging? leading (leading (leading )

leading (load is capacitive, Q is negative)

g) The two components of the load are in a box which cannot be opened. Add (draw it) another component to the circuit above which can correct the power factor (make pf = 1). Show the correct component in the correct place and <u>find its value</u>. This component should not affect the real power consumption of the load.

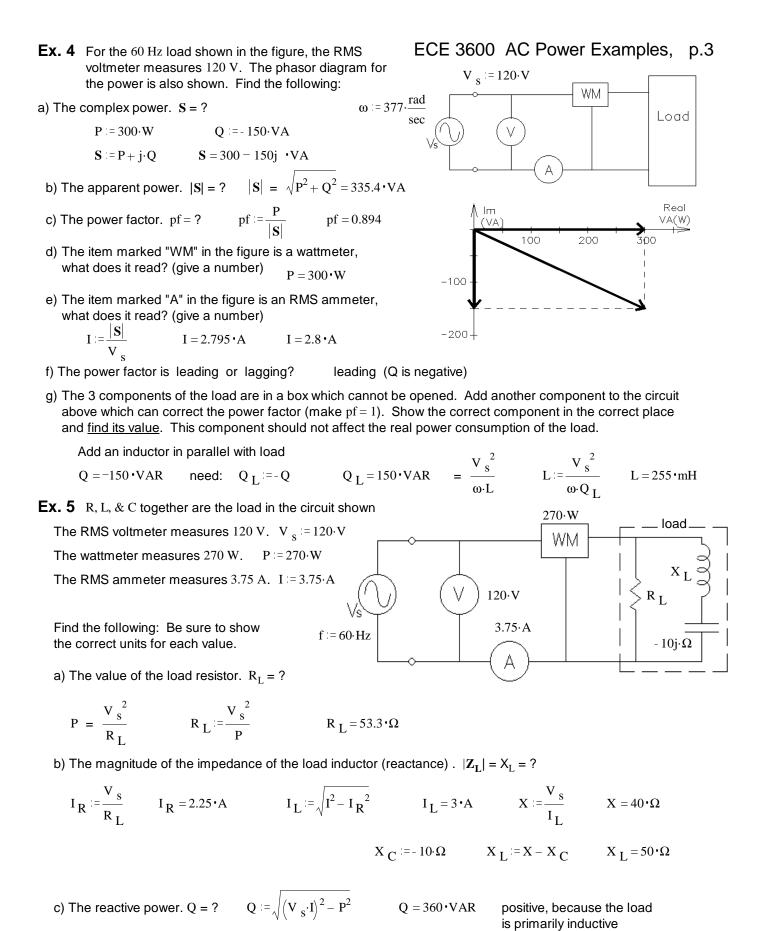
Add an inductor in parallel with load  

$$f = 60 \cdot Hz \qquad \omega := 2 \cdot \pi \cdot f \qquad \omega = 376.991 \cdot \frac{140}{sec}$$

$$Q = -398 \cdot VAR \qquad so we need: \qquad Q_{L} := -Q \qquad \qquad Q_{L} = 398 \cdot VAR \qquad = \frac{V_{s}^{2}}{X_{L}}$$

$$X_{L} := \frac{V_{s}^{2}}{Q_{L}} \qquad \qquad X_{L} = 144.725 \cdot \Omega = \omega \cdot L \qquad \qquad L := \frac{|X_{L}|}{\omega} \qquad \qquad L = 384 \cdot mH$$

## ECE 3600 AC Power Examples, p.2



d) The power factor is leading or lagging?

lagging (load is inductive, Q is positive)

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#### ECE 3600 AC Power Examples, p.4

e) The 3 components of the load are in a box which cannot be opened. Add another component to the circuit above which can correct the power factor (make pf = 1). Show the correct component in the correct place and <u>find its value</u>. This component should not affect the real power consumption of the load.

Add a capacitor in parallel with load  

$$f = 60 \cdot Hz \qquad \omega := 2 \cdot \pi \cdot f \qquad \omega = 376.991 \cdot \frac{rad}{sec}$$

$$Q = 360 \cdot VAR \qquad so we need: \qquad Q_C := -Q \qquad \qquad Q_C = -360 \cdot VAR \qquad = -\frac{V_s^2}{\frac{1}{\omega \cdot C}} = -\omega \cdot C \cdot V_s^2$$

$$C := \frac{Q_C}{-\omega \cdot V_s^2} \qquad \qquad C = 66.3 \cdot \mu F$$

**Ex. 6** An inductor is used to completely correct the power factor of a load.

Find the following: a) The power consumed by the load.  $P_L = ?$   $I_S$   $V_S := 120 \cdot V$   $\underline{I_C}^{0^0}$   $I_L := 200 \cdot mH$   $U_L := \frac{(|V_S|)^2}{\omega \cdot L}$   $Q_L = 190.986 \cdot VAR$   $Q_{load} := -Q_L$   $S_L := |V_S| \cdot I_L$   $S_L = 480 \cdot VA$   $P_L := \sqrt{S_L^2 - Q_{load}^2}$  $P_L = 440.4 \cdot W$ 

b) The power supplied by the source.  $P_S = P_L = 440 \cdot W$ 

- c) The source current (magnitude and phase).  $I_{S} := \frac{P_{L}}{V_{S}}$   $I_{S} = 3.67 \cdot A \frac{/0^{\circ}}{because the source}$ 
  - sees a pf = 1

d) The load can be modeled as 2 parts in parallel. Draw the model and find the values of the parts.

$$P = \frac{V^{2}}{R}$$

$$R_{L} := \frac{(|V_{S}|)^{2}}{P_{L}}$$

$$R_{L} = 32.7 \cdot \Omega$$

$$Q_{C} = V^{2} \cdot (\omega \cdot C)$$

$$C_{L} := \frac{-Q_{load}}{\omega \cdot (|V_{S}|)^{2}}$$

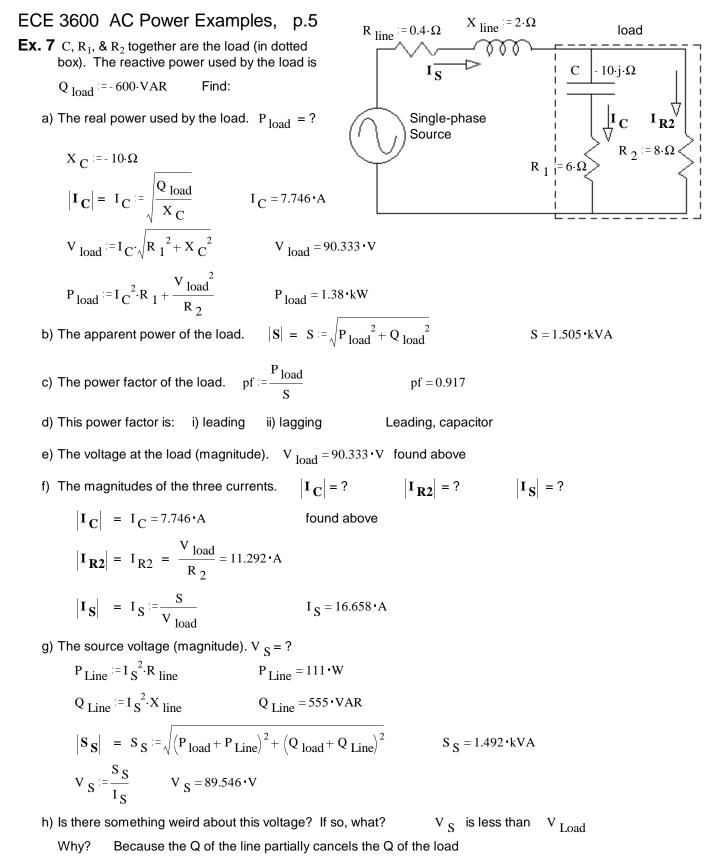
$$C_{L} = 35.181 \cdot \mu F$$

e) The inductor, L, is replaced with a 50 mH inductor.

i) The **new** source current  $|I_S|$  is **greater** than that calculated in part c). <-- Answer circle

ii) The **new** source current  $|I_S|$  is **the same** as that calculated in part c).

iii) The **new** source current  $|I_S|$  is **less** than that calculated in part c).



OR Partial resonance between the inductance in the line and the capacitance of the load.

i) The efficiency.  $\eta = ?$ 

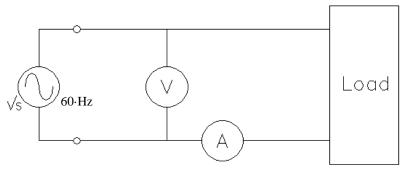
When asked for efficiency, assume the power used by  $R_{line}$  is a loss and  $P_{load}$  is the output power.

$$\eta = \frac{P_{out}}{P_{in}} = \frac{P_{out}}{P_{out} + P_{loss}} = \frac{P_{load}}{P_{load} + P_{Line}} = 92.56 \cdot \%$$
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#### ECE 3600 AC Power Examples, p.6

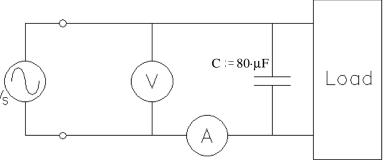
Ex. 8 In the circuit shown, the ideal voltmeter, V, reads 120V and ideal ammeter, A, reads 5A.

$$S_{load} = 120 \cdot V \cdot 5 \cdot A$$
  $S_{load} = 600 \cdot VA$ 



a) You add a capacitor, C, and the ammeter reading changes to 5.3A. Find the following:

$$P_{load} = ? \qquad Q_{load} = ?$$



#### I<sub>C</sub> is NOT 0.3A, That's subtracting magnitudes

$$S_{load} := 120 \cdot V \cdot 5 \cdot A$$
  $S_{load} = 600 \cdot VA = \sqrt{P_{load}^2 + Q_{load}^2}$   
 $OR \quad (600 \cdot VA)^2 = P_{load}^2 + Q_{load}^2$   
 $P_{load}^2 = (600 \cdot VA)^2 - Q_{load}^2$ 

$$Q_{C} := \frac{(120 \cdot V)^{2}}{\left(-\frac{1}{\omega \cdot C}\right)} = -(120 \cdot V)^{2} \cdot \omega \cdot C \qquad Q_{C} = -434.294 \cdot VAR$$

With Capacitor:

$$S_{S} = 120 \cdot V \cdot 5.3 \cdot A \qquad S_{S} = 636 \cdot VA = \sqrt{P_{load}^{2} + (Q_{load} + Q_{C})^{2}}$$
$$OR \qquad (636 \cdot VA)^{2} = P_{load}^{2} + (Q_{load} + Q_{C})^{2}$$

Substitute in

tute in 
$$(636 \cdot VA)^2 = [(600 \cdot VA)^2 - Q_{load}^2] + (Q_{load} + Q_C)^2$$
  

$$= [(600 \cdot VA)^2 - Q_{load}^2] + (Q_{load}^2 + 2 \cdot Q_C \cdot Q_{load} + Q_C^2)$$

$$= (600 \cdot VA)^2 + 2 \cdot Q_C \cdot Q_{load} + Q_C^2$$

$$Q_{load} := \frac{(636 \cdot VA)^2 - (600 \cdot VA)^2 - Q_C^2}{2 \cdot Q_C}$$

$$Q_{load} := 165.919 \cdot VAR$$

$$P_{load} := \sqrt{S_{load}^2 - Q_{load}^2} \qquad P_{load} = 576.603 \cdot W$$

 $S_{s} = \sqrt{P_{load}^{2} + (Q_{load} + Q_{c})^{2}} = 636 \cdot VA$ Double Check:

The power factor was way over corrected by  $C = 80 \cdot \mu F$