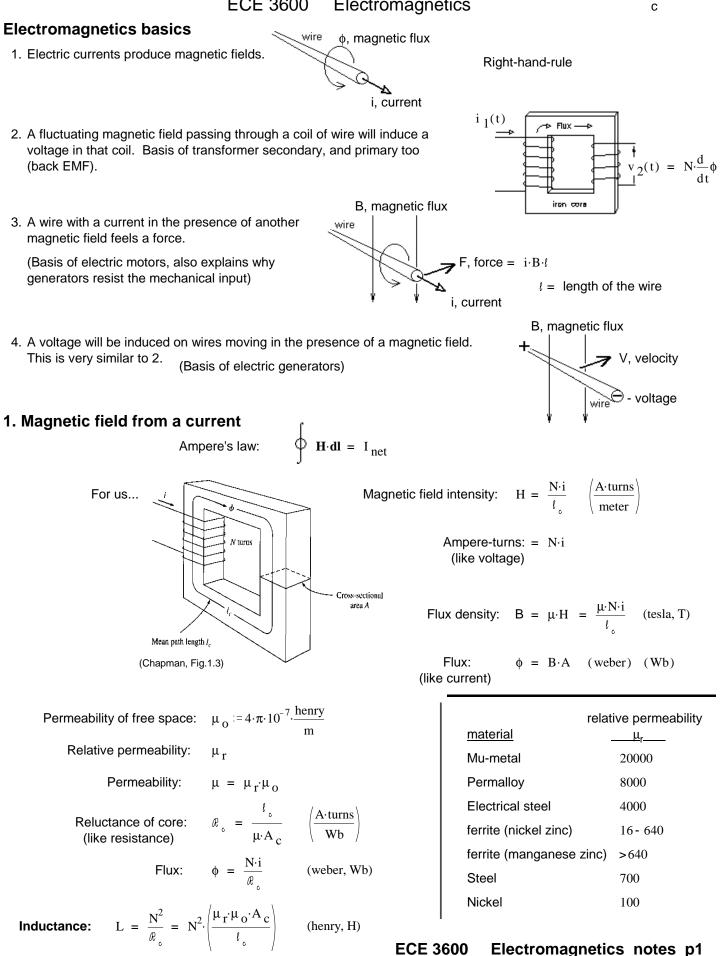
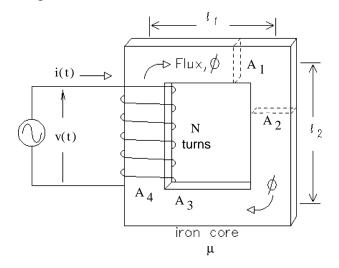
ECE 3600 Electromagnetics

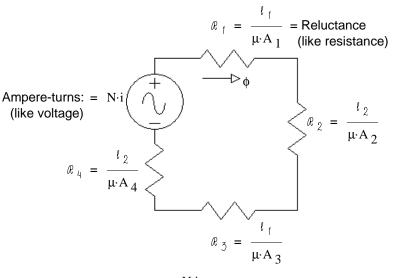


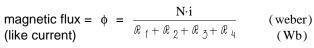
ECE 3600 Electromagnetics notes p2

Magnetic "Circuits"

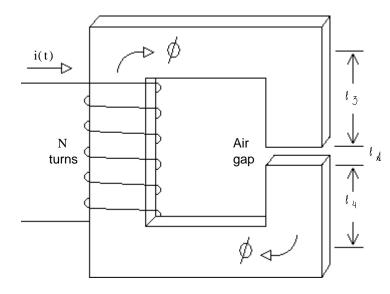


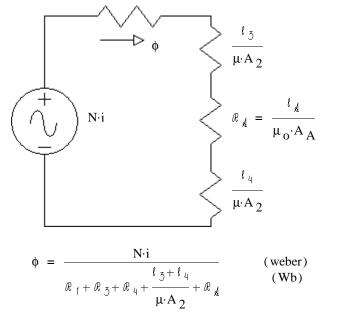
Similar to this electric circuit





 $\mathcal{R}_1 + \mathcal{R}_3 + \mathcal{R}_4$





 $B = \frac{\phi}{A} = \mu \cdot H$ Flux density: (tesla, T)

Magnetic field intensity:

$$H = \frac{B}{\mu} = \frac{\phi}{A \cdot \mu} \qquad \left(\frac{A \cdot turns}{meter}\right)$$

$$\mathbf{v}(t) = \mathbf{N} \cdot \frac{\mathbf{d}}{\mathbf{d}t} \mathbf{\phi} = \mathbf{N} \cdot \frac{\mathbf{d}}{\mathbf{d}t} \mathbf{B} \cdot \mathbf{A}$$

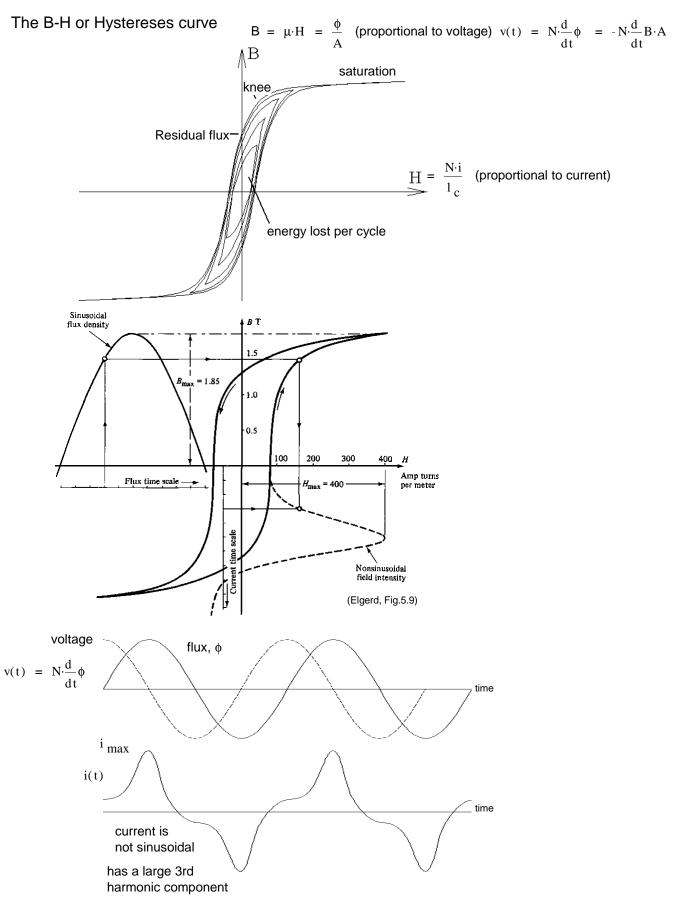
=
$$-N \cdot \frac{d}{dt} \phi$$
 = $-N \cdot \frac{d}{dt} B \cdot A$ often shown with a negative sign

- indicates that this voltage tries to

produce a current to oppose the change.

Non-ideal Ferrromagnetic materials (B-H curve)

Magnetics are not really linear



Sources: <u>Electric Machinery and Power System Fundamentals</u>, Stephen J. Chapman <u>Basic Electric Power Enineering</u>, Ollie I. Elgerd

ECE 3600 Transformers

Transformer basics and ratings

A Transformer is two coils of wire that are magnetically coupled.

Transformers are only useful for AC, which is one of the big reasons electrical power is generated and distributed as AC.

Transformer turns and turns ratios are rarely given, V_p/V_s is much more common where V_p/V_s is the rated primary voltage over rated secondary voltage. Ideally, you may take this to be the same as N_1/N_2 although in reality N_2 is usually a little bit bigger to make up for losses. Another commonway to show the same thing: $V_p : V_s$.

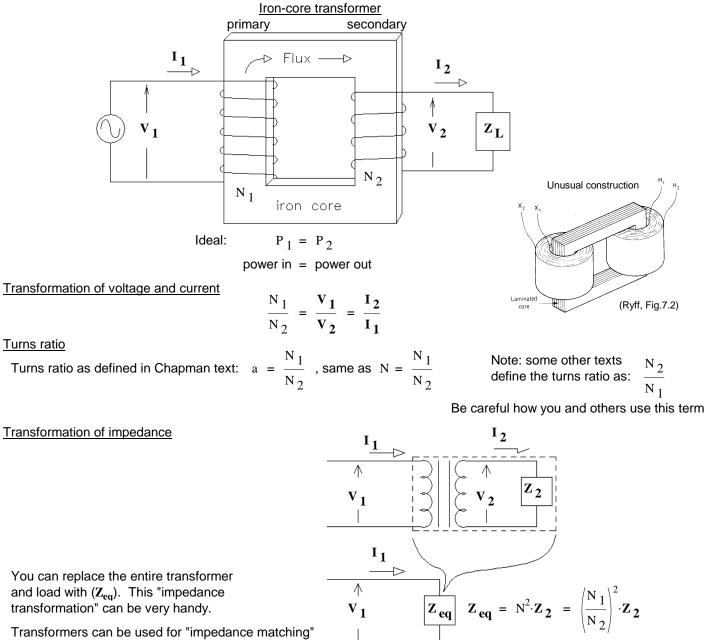
Transformers are rated in VA Transformer Rating (VA) = (rated V) x (rated I), on either side.

Don't allow voltages over the rated V, regardless of the actual current.

Don't allow steady-state currents over the rated I, regardless of the actual voltage.

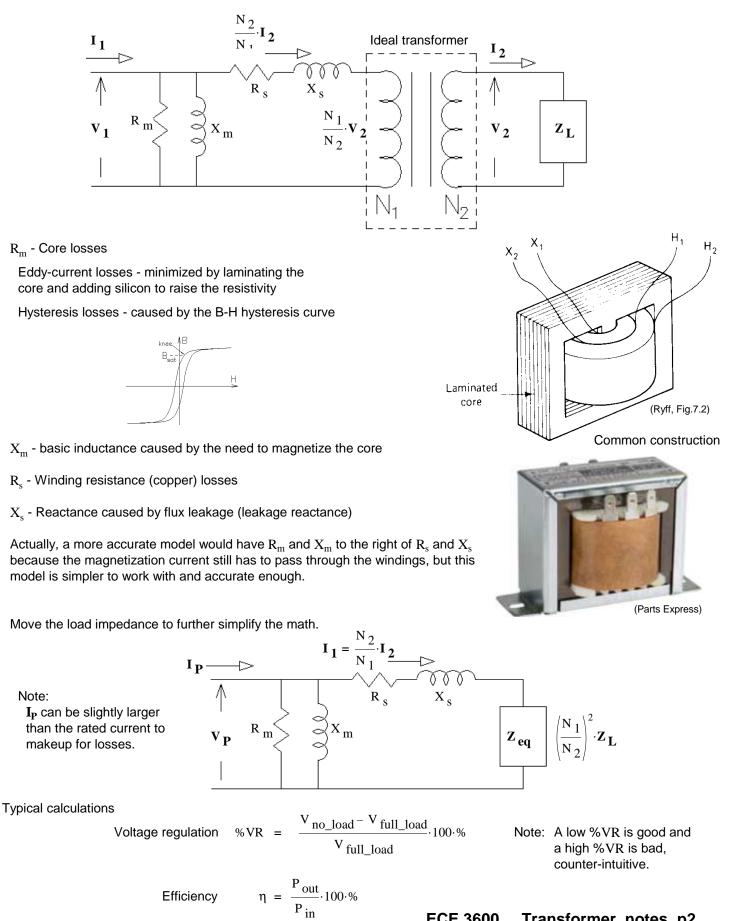
Short-term inrush and startup currents may be higher as long as there's no overheating.

Ideal Transformers



This also works the opposite way, to move an impedance from the primary to the secondary, multiply by:

Model of non-ideal Transformer



ECE 3600

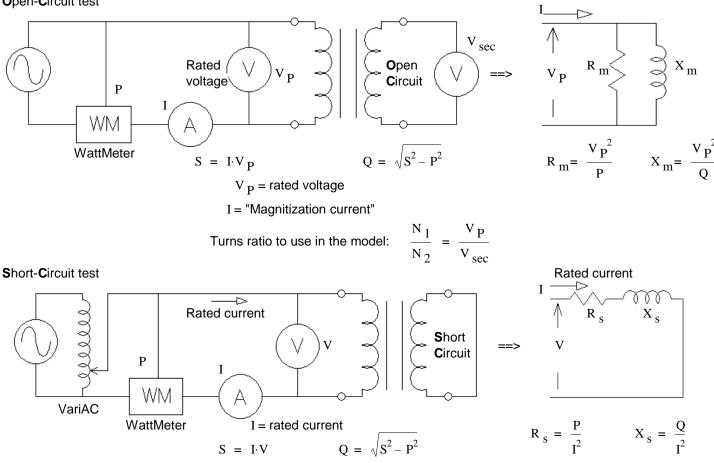
Transformer notes p2

Tests to find parameters Open-Circuit test

ECE 3600

Transformer notes p3

Model reduces to



Determining $\frac{N_1}{N_2}$ if you're working from transformer ratings and parameters.

Manufacturers of transformers are well aware of R_s and X_s and how they reduce the output voltage, so they add a few windings (1 - 5%) to the secondary in order to make up for the loss. This lowers the effective turns ratio of the ideal transformer in the model by the same 1 - 5%.

If you're given transformer ratings as V_{Prated}/V_{Srated} , S_{rated} along with R_s and X_s , what turn ratio (N) would the manufacturer actually use for the transformer?

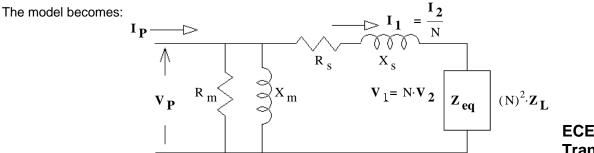
The following calculations are based on: $V_P = V_{Prated}$ $V_S = V_{Srated}$ $P_{out} = S_{rated}$ and pf = 1

Then:
$$R_L = \frac{V_{Srated}^2}{S_{rated}}$$
 define: $R_x = \frac{V_{Prated}^2}{S_{rated}} - 2 \cdot R_s$ for ease of calculation below

$$R_L$$
, referred to primary side = $R_{eq} = \frac{R_x + \sqrt{R_x^2 - 4 \cdot \left(R_s^2 + X_s^2\right)}}{2}$ and, $N = \sqrt{\frac{R_{eq}}{R_L}}$

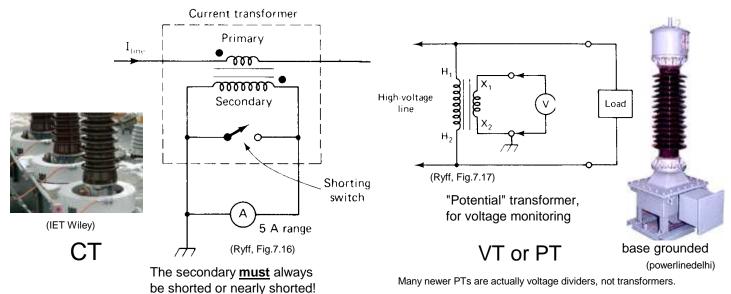
Finding $R_{_{eq}}$ required lots of messy algebra, which I'm skipping here.

Just use the calculations above as formulas if you're not given a value for N along with the other parameters.



ECE 3600 Transformers p3

Special Sensing Transformers

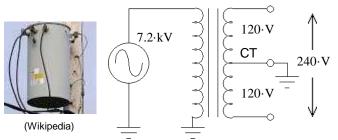


Other Transformers

Multi-tap transformers

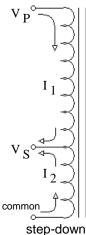
Many transformers have more than two connections to primary and/or the secondary. The extra connections are called "taps" and may allow you to select from several different voltages or get more than one voltage at the same time.

A center tap is very common.



Typical tranformer for residential distribution

Autotransformers



Single-winding transformers where the primary and secondary share windings. For step-down, the secondary is some fraction of the primary. For step-up, the primary is some fraction of the secondary.

Because of the way the currents flow within the windings, the current of the low-voltage side is greater than any current within the windings. Less current meas that autotransformers can be economical.

A variAC is an adjustable autotransformer.

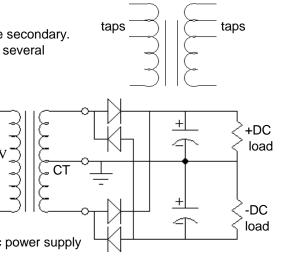
Normal transformers can also be wired as autotransformers. More info to come. Simple + dc power supply

Load tap changing

120

Multiple taps near the top of the transformer can be used to boost or buck (reduce) the voltage a bit. Transformers like this are often used in substations for voltage regulation. Typically, they can adjust the voltage + 10% in 33 steps (0.625% per step). Those that can change taps while under load are called "Load tap changing". They can either be regular transformers or autotransformers, the latter are usually just called "voltage regulators". Most can be set up to work automatically.

The tap changing circuitry is not shown at right. It can be rather tricky in that it can not short two taps together nor can it open the circuit during switching.

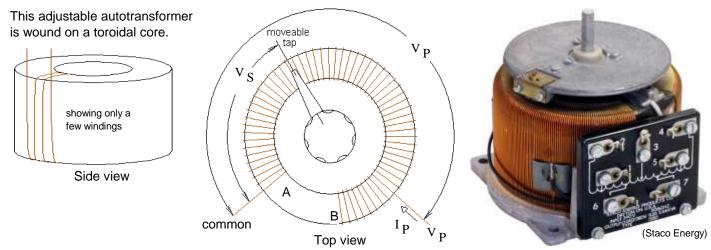




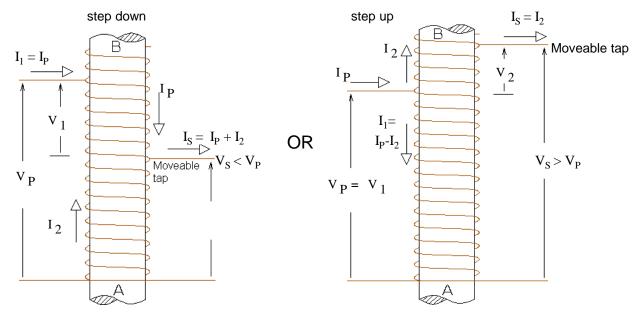
Isolation Transformers

All transformers (except autotransformers) isolate the primary from the secondary. An Isolation transformer has a 1:1 turns ratio and is just for isolation.

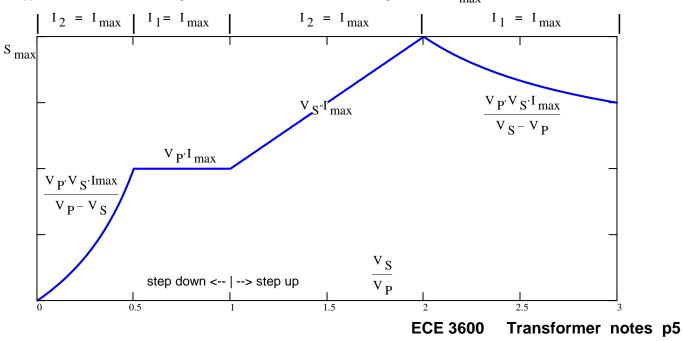
VariAC-type Autotransformer



If you cut the toroid open and straightened it out, you would get the views below.



Vari-AC type autotransformer "Rating" , $\,$ Based or the maximum winding current: $\,$ I $_{max}$



Regular winding connections

$$I_{P} = \overline{I_{1}} \xrightarrow{\longrightarrow} I_{2} = I_{S}$$

$$V_{P} = V_{1} \xrightarrow{\longrightarrow} I_{2} = V_{S}$$

$$\swarrow \xrightarrow{\longrightarrow} I_{2} = V_{S}$$

Auto Transformer Connections

4 basic possibilities

Addition connections

$$I_{P} = I_{1} + I_{2} \xrightarrow{} I_{1} \xrightarrow{} I_{1} \xrightarrow{} I_{2} \xrightarrow{$$

Rating:

 $I_{P} = I_{1} \xrightarrow{P}$ $V_{P} = V_{1} + V_{2}$ $I_1 + I_2 = I_S$ I_2 Î_{I 1}

⊲-

$$v_2 = v_S$$

Rating: $(I_{1_rated} + I_{2_rated}) \cdot v_S$

Currents I_1 and I_2 are flowing reverse of normal.

Subtraction connections

$$\begin{array}{c|c} & I_2 & \stackrel{I_2}{\longrightarrow} & I_1 \\ I_p & \stackrel{I_2}{=} & I_2 \\ V_p = V_1 \\ \hline \\ V_p$$



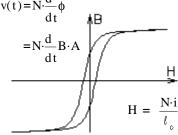
Inrush current

When a transformer is de-energized (switched off) its core may remain partially magnetized. When it is then re-energized (switched on) it may take several cycles before the B and the H re-center around the 0,0 point of the B-H plot. That can result in pushing the core far into saturation with large peaks of magnetic field intensity (H). H is directly proportional to current, so there are correspondingly large peaks of current. This inrush current is not sinusoidal and usually has a large DC component. Since it is dependent on where in the voltage cycle the transformer was de-energized it will be different each time the transformer is re-energized.

 $v(t) = N \cdot \frac{d}{dt} \phi$

Transformer notes p7

ECE 3600



Normal inrush currents can be just as large as abnormal short-circuit currents, yet protection devices (breakers and fuses) should not trip or blow-- a difficult protection problem.

Any device with a magnetic core will experience similar inrush currents.

Cooling and Oil-Immersion

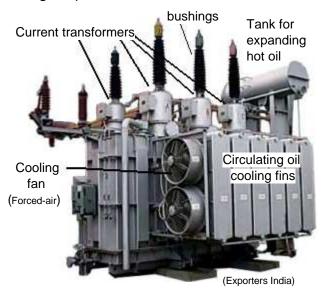
High-voltage transformers are almost universally immersed in oil. That is, the core and windings are in a big enclosure filled with oil. Oil is a much better electrical insulator than air and also has much better thermal conductivity. Typically, it's mineral oil, but other, more expensive, oils and chemicals are also used to reduce fire and/or environmental hazards. PCBs are no longer used. Although PCB reduced the fire risk, it's highly toxic and stays in the environment a long time.

Core losses in a transformer will cause it to heat up even if it's not loaded. I²R losses increase the heating under loaded conditions. Small transformers may just be air-cooled, but larger transformers require more cooling. Large oil-filled transformers typically cool that oil in radiators with fins next to the transformer. Those fins often have fans for forced-air cooling and the oil may be pumped through the transformer for forced-oil cooling. Transformers often have a tank to accommodate the thermal expansion of the oil. A bladder or inert gas inside the tank prevents contact with air.

Cooling Types: AA Dry-type, Air cooled AFA Dry-type, Forced-Air cooled OA Oil Immersed, Air-cooled OA/FA Oil Immersed, Air / Forced-Air cooled OA/FA/FOA Oil Immersed, Air / Forced-Air / Forced-Oil and air cooled

Dissolved Gas Analysis

Analysis of the oil can reveal information about the health of the transformer. The simple version: Oxygen and Nitrogen indicate the oil has had contact with air. Carbon monoxide and dioxide indicate insulation degradation. Hydrogen indicates corona discharge. Methane, ethane, ethylene, and acetylene all indicate increasing levels of electrical faults and/or overheating with acetylene being the worst, indicating arcing. The oil is also checked for water, even a little of which is very bad. Regular maintenance includes filtering and drying the oil.



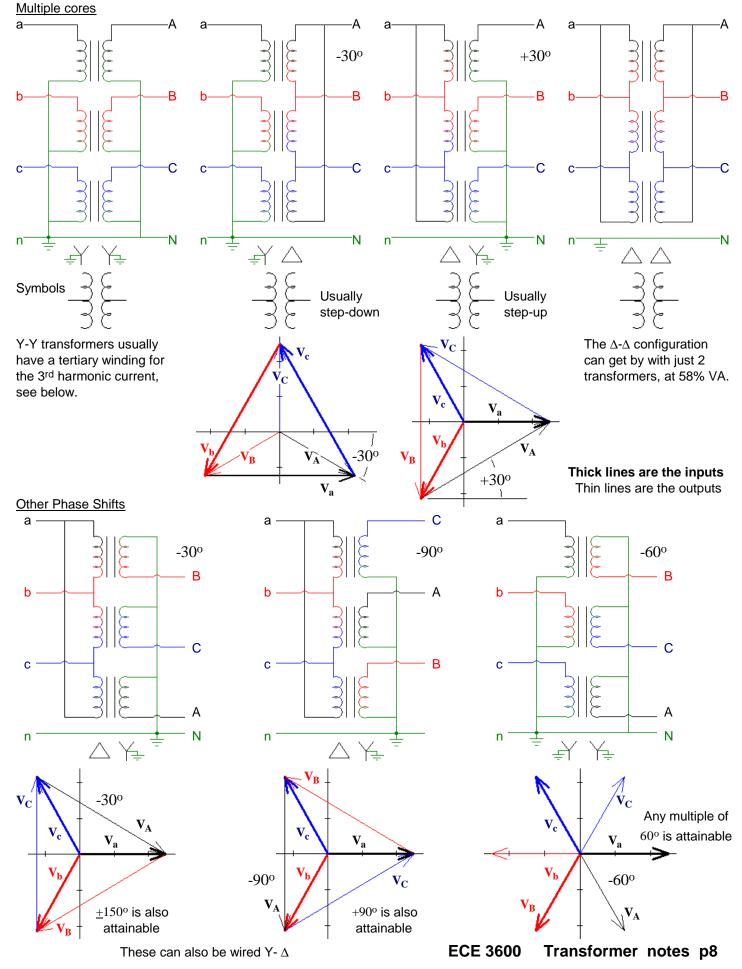
Large 3-phase Substation Transformer

Mineral Oil is Flammable (or is that inflammable?)



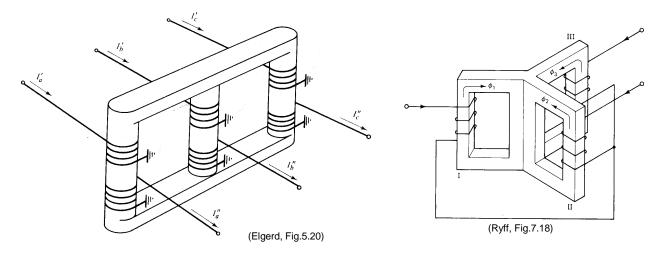
^{.za)} ECE 3600 Transformer notes p7

3-phase Transformer Connections



Single-Core 3-phase Transformers

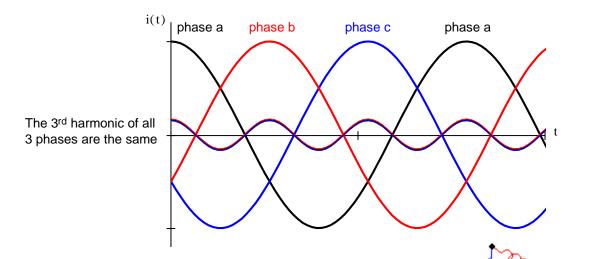
Cheaper and have less core loss than using individual cores or transformers.



Single-core transformers can also create all phase shifts shown on the previous page.

Third-Harmonic Currents

Third-harmonic currents (due to B-H non-linearity) add up to a significant neutral current.



Any Δ -connected winding will allow the third-harmonic current to flow in a loop.



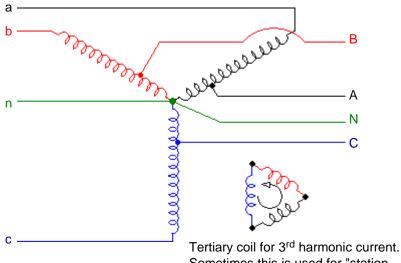
Transformer notes p9 ECE 3600

(iStock)



3-phase autotransformers

Becoming more popular because they're cheaper for a given VA.

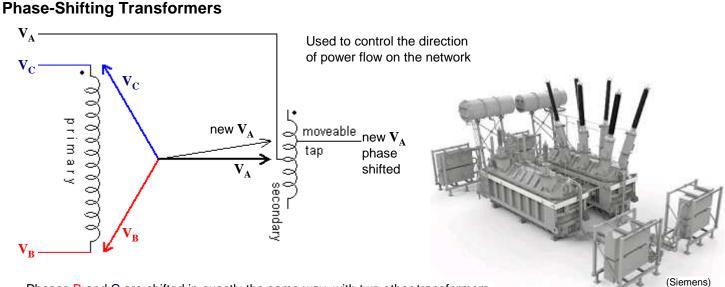


Tertiary coil for 3rd harmonic current Sometimes this is used for "station power", that is, used to power the substation.

ECE 3600 Transformer notes p10



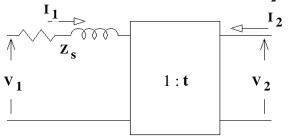
345kV/138kV Autotransformer at Terminal ^{(/} Substation in Salt Lake City. Note oil tank and cooling fins.



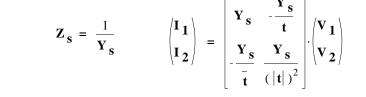
Phases B and C are shifted in exactly the same way, with two other transformers.

Off-Nominal Turns Ratio

Note the weird I₂ direction



If there is a phase shift, t will be complex



t = complex conjugate of t

Ex.1 a) An ideal transformer has 360 turns on the primary winding and 36 turns on the secondary. If the primary is connected across a 120 V (rms) generator, what is the rms output voltage?

 $120 \cdot \text{volt} \cdot \frac{36}{360} = 12 \cdot \text{volt}$

b) If you used a full-wave rectifier and a capacitor to make a DC power supply with this transformer, what DC voltage should you get?

$$12 \cdot V \cdot \sqrt{2 - 2 \cdot 0.7} \cdot V = 15.6 \cdot V$$
 less under load peak 2 diodes

Ex.2 A transformer has $N_1 = 320$ turns and $N_2 = 1000$ turns. If the input voltage is $v(t) = (255 \text{ V})\cos(\omega t)$, what rms voltage is developed across the secondary coil?

$$\frac{253.4\text{out}}{\sqrt{2}} \cdot \frac{1000}{320} = 563.4\text{volt}$$

- **Ex.3** A transformer is rated at 480V / 120V, 1.2kVA. Assume the transformer is ideal and all voltages and currents are RMS.
 - a) What is the current rating of the primary?

$$\frac{1.2 \cdot kVA}{480 \cdot V} = 2.5 \cdot A$$

b) What is the current rating of the secondary?

$$\frac{1.2 \cdot k V A}{120 \cdot V} = 10 \cdot A$$

c) The secondary has 100 turns of wire. How many turns does the primary have?

N₂ := 100 N₁ :=
$$\frac{480 \cdot V}{120 \cdot V} \cdot N_2$$
 N₁ = 400 turns

d) $\mathbf{V}_{\mathbf{L}} = 110 \cdot \mathbf{V}$ How big is the source voltage ($|\mathbf{V}_{\mathbf{S}}|$)?

$$\mathbf{V} \mathbf{S} := \frac{\mathbf{N}}{\mathbf{N}} \frac{1}{2} \cdot \mathbf{V} \mathbf{L} \qquad \mathbf{V} \mathbf{S} = 440 \cdot \mathbf{V}$$

e) The secondary load (Z_L) has a magnitude of 20 Ω at a power factor of 75%. Find the secondary current, I_2 (magnitude and <u>angle</u>). pf := 75.%

$$I_2 = \frac{V_L}{20 \cdot \Omega} = 5.5 \cdot A$$
 pf = 0.75 acos(pf) = 41.4 · deg $I_2 = 5.5 A / -41.4^\circ$

f) Find the primary current, I_1 (magnitude **and** <u>**angle**</u>).

$$\mathbf{I_1} = \frac{100}{400} \cdot 5.5 \cdot \mathbf{A} = 1.375 \cdot \mathbf{A}$$

$$a\cos(pf) = 41.4 \cdot deg$$

$$\mathbf{I_1} = 1.375 \cdot \mathbf{A} / -41.4^{\circ}$$
Transformer is ideal, so angle is exactly the same as the load.

g) How much average power does the load dissipate?

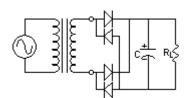
$$\mathbf{P}_{\mathbf{L}} = |\mathbf{V}_{\mathbf{2}}| \cdot |\mathbf{I}_{\mathbf{2}}| \cdot \text{pf} = 110 \cdot \mathbf{V} \cdot 5.5 \cdot \mathbf{A} \cdot 75 \cdot \% = 453.8 \cdot \text{watt}$$

h) How much average power does the power source (V_S) supply?

$$P_S = P_L = 454$$
·watt

i) What is the load as seen by $\mathbf{V}_{S}?$ (magnitude and $\underline{angle})$

$$\left(\frac{400}{100}\right)^2 \cdot 20 \cdot \Omega = 320 \cdot \Omega \qquad a\cos(pf) = 41.4 \cdot deg \qquad \mathbf{Z}_{eq} = 320\Omega \, \underline{/41.4^{\circ}}$$
OR:
$$\frac{440 \cdot V}{1.375 \cdot A} = 320 \cdot \Omega \, \underline{/0 - 41.4^{\circ}} \qquad \text{Transformer Examples p1}$$



pf := 75.% lagging

= $20 \cdot \Omega$

ZL

 Z_L

$$\mathbf{L} := 110 \cdot \mathbf{V}$$

Ex.4 A transformer is rated at 480V/240V, 1.2kVA. Assume the transformer is ideal and all voltages and currents are RMS.

How much power does the load consume?

$$\mathbf{V}_{\mathbf{L}} := \mathbf{V}_{\mathbf{S}} \cdot \left(\frac{240}{480} \right) \qquad |\mathbf{V}_{\mathbf{L}}| = 220 \cdot \mathbf{V} \qquad |\mathbf{V}_{\mathbf{S}}| = 440 \cdot \mathbf{V} \qquad |\mathbf{Z}_{\mathbf{L}}| = 16 \cdot \Omega$$

$$pf := 80 \cdot \% \quad \text{lagging}$$

$$\mathbf{I}_{2} := \frac{|\mathbf{V}_{\mathbf{L}}|}{|\mathbf{Z}_{\mathbf{L}}|} \qquad \mathbf{P}_{\mathbf{L}} := |\mathbf{V}_{\mathbf{L}}| \cdot \mathbf{I}_{2} \cdot \mathbf{p} f \qquad \mathbf{P}_{\mathbf{L}} = 2.42 \cdot \mathbf{k} \mathbf{W}$$

 $|_1$

 $|_2$

V2

Z

load

Ex.5 The transformer shown in the circuit below is ideal. It is rated at 220/110 V, 200 VA, 60 Hz

Find the following:

a) The primary current (magnitude).

$$|\mathbf{I}_{1}| = ?$$

$$\mathbf{V}_{S} := 120 \cdot \mathbf{V}$$

$$\mathbf{V}_{S} := 120$$

b) The primary voltage (magnitude).

 $|V_1| = ?$

$$V_1 := I_1 \cdot \sqrt{60^2 + 80^2} \cdot \Omega$$
 $V_1 = 93.7 \cdot V$

c) The secondary voltage (magnitude).

$$|\mathbf{V}_2| = ?$$
 $\mathbf{V}_2 = \frac{110}{220} \cdot \mathbf{V}_1 = 46.85$

d) The power supplied by the source.

$$P_{S} = ?$$
 $P_{S} = I_{1}^{2} \cdot 100 \cdot \Omega = 87.8 \cdot W$

e) Is this transformer operating within its ratings? Show your evidence.

$$I_{1max} = \frac{200 \cdot VA}{220 \cdot V} = 0.909 \cdot A < I_1 = 0.937 \cdot A$$

NO
ALWAYS CHECK CURRENT
Transformer Examples p2

٠V

Ex.6 Repeat Ex.5 with a non-ideal transformer whose characteristics are shown below.

$$R_{m} := 1 \cdot k\Omega \qquad X_{m} := 400 \cdot \Omega \qquad R_{s} := 3 \cdot \Omega \qquad X_{s} := 8 \cdot \Omega \qquad N := 1.95$$

$$R_{1} := 40 \cdot \Omega \qquad I_{P} \qquad R_{s} = 3 \cdot \Omega \qquad X_{s} = 8 \cdot \Omega \qquad Z_{eq} := (1.95)^{2} \cdot (15 + 20 \cdot j) \cdot \Omega$$

$$V_{S} := 120 \cdot V \qquad V_{P} \qquad X_{m} \qquad R_{m} = 1 \cdot k\Omega \qquad V_{1} \qquad 76 \cdot j \cdot \Omega$$

Find the following:

a) The primary current (magnitude).

b) The primary voltage (magnitude).

$$|\mathbf{V}_{\mathbf{P}}| = ?$$
 $\mathbf{V}_{\mathbf{P}} := \mathbf{I}_{\mathbf{P}} \cdot (43.689 + 68.412 \cdot \mathbf{j}) \cdot \Omega$ $\mathbf{V}_{\mathbf{P}} = 85.619 + 28.105 \mathbf{j} \cdot \mathbf{V}$
 $|\mathbf{V}_{\mathbf{P}}| = 90.114 \cdot \mathbf{V}$

c) The secondary voltage (magnitude).

$$\begin{aligned} \mathbf{V}_{2} &|=? & \mathbf{I}_{1} := \frac{\mathbf{V}_{P}}{(60 + 84 \cdot \mathbf{j}_{1}) \cdot \Omega} & \mathbf{I}_{1} = 0.704 - 0.517 \mathbf{j}_{1} \cdot \mathbf{A} \\ & \mathbf{V}_{1} := \mathbf{I}_{1} \cdot (57 + 76 \cdot \mathbf{j}_{1}) \cdot \Omega & \mathbf{V}_{1} = 79.375 + 24.026 \mathbf{j}_{1} \cdot \mathbf{V} \\ & |\mathbf{V}_{1}| = 82.931 \cdot \mathbf{V} & |\mathbf{V}_{2}| = \frac{1}{N} \cdot 82.931 \cdot \mathbf{V} = 42.529 \cdot \mathbf{V} \end{aligned}$$

OR, simply:

$$I_{1} := \frac{90.114 \cdot V}{\sqrt{60^{2} + 84^{2}} \cdot \Omega} \qquad I_{1} = 0.873 \cdot A \qquad V_{2} = \frac{I_{1} \cdot \sqrt{57^{2} + 76^{2}} \cdot \Omega}{1.95} = 42.529 \cdot V$$

d) The power supplied by the source.

$$P_S = ?$$
 $P_S = 120 \cdot V \cdot Re(I_P) = 103.14 \cdot W$

e) Is this transformer operating within its ratings? Show your evidence.

$$I_{2max} = \frac{200 \cdot VA}{110 \cdot V} = 1.818 \cdot A > |I_1| \cdot N = 1.702 \cdot A$$

YES

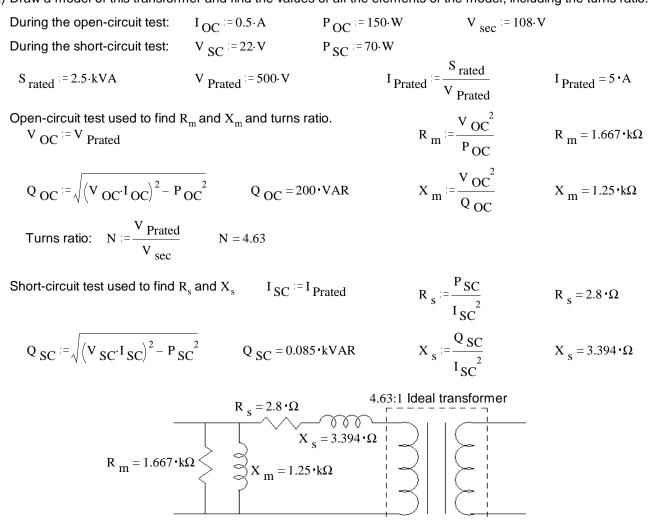
f) Find the efficiency, assuming that the only useful output is from $\mathbf{Z}_{\mathbf{L}}$.

$$\eta = \frac{\left(\left|\mathbf{I}_{\mathbf{1}}\right|\right)^2 \cdot 57 \cdot \Omega}{103.14 \cdot W} \cdot 100 \cdot \% = 42.12 \cdot \%$$

Ex.7 Find the voltage regulation and full-load efficiency of the transformer with the following ratings and characteristics.

Rated at 450/120 V. 2 kVA. 60 Hz R
$$_{\rm m}$$
 = 8.4 kΩ $X_{\rm m}$ = 2.4Ω R $_{\rm s}$ = 5.Ω $X_{\rm s}$ = 15.Ω V $_{\rm s}$ = 120 V $_{\rm s}$ = 120

Ex.8 A 500/100-V, 2.5-kVA transformer is subjected to an OC test and a SC test with the results below.a) Draw a model of this transformer and find the values of all the elements of the model, including the turns ratio.



b) The transformer is connected to a primary source voltage of 360V and loaded with $\mathbf{Z}_{\mathbf{L}} := (2 + 1 \cdot \mathbf{j}) \cdot \Omega$ Find the secondary voltage. Magnitude only. $|\mathbf{V}_{2}| = ?$

$$\mathbf{V}_{1} = \mathbf{V}_{1} := \mathbf{V}_{S} \cdot \frac{\sqrt{(42.874 \cdot \Omega)^{2} + (21.437 \cdot \Omega)^{2}}}{\sqrt{(\mathbf{R}_{s} + 42.874 \cdot \Omega)^{2} + (\mathbf{X}_{s} + 21.437 \cdot \Omega)^{2}}} \qquad \mathbf{V}_{1} = \mathbf{V}_{2} = \frac{\mathbf{V}_{1}}{4.63^{2} \cdot \mathbf{V}_{1}} = 21.437 \cdot \mathbf{V}_{1}$$

c) Is this transformer operating within its ratings? Show all evidence and calculate needed to to determine this.

$$|\mathbf{I}_{2}| = \mathbf{I}_{2} := \frac{\mathbf{V}_{S}}{\sqrt{\left(\mathbf{R}_{s} + 42.874 \cdot \Omega\right)^{2} + \left(\mathbf{X}_{s} + 21.437 \cdot \Omega\right)^{2}}} \cdot \mathbf{N} \qquad \mathbf{I}_{2} = 32.059 \cdot \mathbf{A} > \mathbf{I}_{Srated} = \frac{\mathbf{S}_{rated}}{100 \cdot \mathbf{V}} = 25 \cdot \mathbf{A}$$

NO !

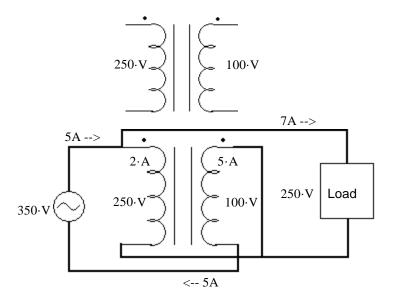
Transformer Examples p5

- $\ensuremath{\text{Ex.9}}$ You have a $250/100\mbox{-V},\,500\mbox{-VA}$ transformer.
 - a) Show the necessary connections to use this transformer to transform 350 V to 250 V. Also show the 350-V source and the load.
 - b) Connected this way, determine the maximum power that could be converted from 350 V to 250 V without overloading the transformer.

ratings:
$$\frac{500 \cdot VA}{250 \cdot V} = 2 \cdot A$$
 $\frac{500 \cdot VA}{100 \cdot V} = 5 \cdot A$

new VA rating and

maximum power: $5 \cdot A \cdot 350 \cdot V = 1.75 \cdot kVA$ OR: $7 \cdot A \cdot 250 \cdot V = 1.75 \cdot kVA$ $1.75 \cdot kWA$



c) Besides the right impedance magnitude, what other characteristic must the load posses in order to actually use this much power?

Load must be purely resistive (power factor is 1).

d) Could this transformer also be used to transform 280 V to 200 V? If yes, what is the maximum power that could be transformed?

Same connections as above Maximum power:

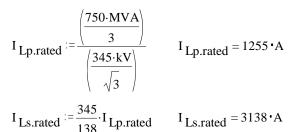
 $5 \cdot A \cdot 280 \cdot V = 1.4 \cdot kW$

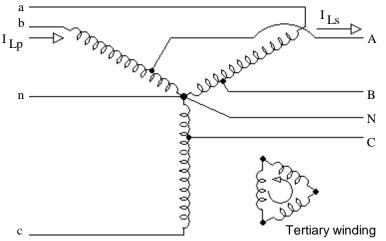
Ex.10 A 345kV/138kV, 750-MVA transformer is shown.

a) What is the purpose of the tertiary winding?

To allow 3rd harmonic currents to flow without affecting currents outside the transformer.

b) Find the maximum $I_{Lp}\, \text{and}\, I_{Ls}.$





c) Find the currents flowing in the transformer when operated at rated capacity.

Current from primary terminal to the tap: $I_p = I_{Lp.rated} = 1255 \cdot A$

Current from neutral to the tap: $I_p = I_{Ls.rated} - I_{Lp.rated} = 1883 \cdot A$

Current from tap to secondary ouput of the transformer: $I_s = I_{Ls.rated} = 3138 \cdot A$

d) At what fraction of the total turns is the tap located? $\frac{138}{345} = 0.4 = \frac{4}{10}$ OR at 40%

e) What one-line symbol would be used for this transformer?

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