ECE 3600 Direct Current (DC) Motors

Armature

The rotating part (rotor)

Field (Excitation)

Provided by the stationary part of the motor (Stator)

Permanent Magnet

Winding

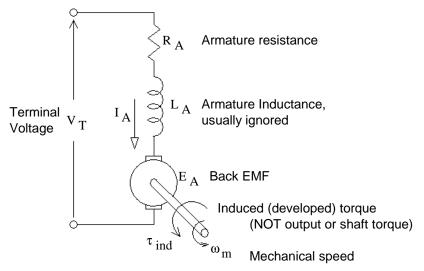
Separately excited Parallel with terminal voltage source (Shunt excited) Series with terminal voltage source (Series excited)

Commutator and commutation

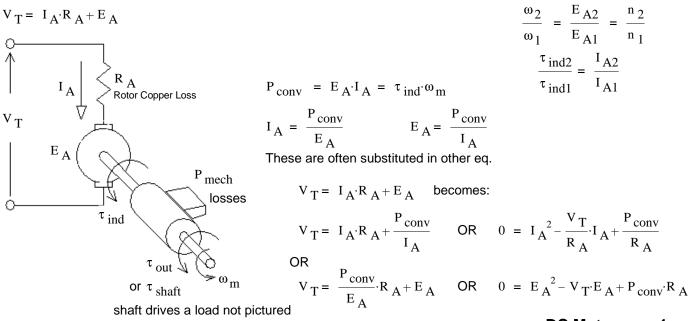
Rotary contacts and brushes which keep switching the current direction in the armature so that the motor torque is always in the same direction.

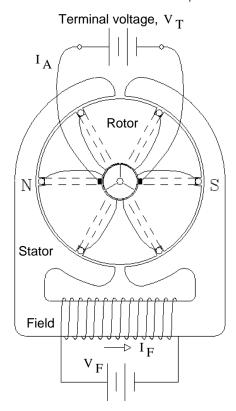
Explained and visualized in class

Electrical Model



Simplified Model we will use





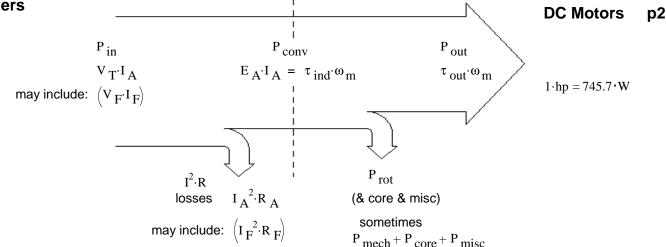
 $E_{A} = K \cdot \phi \cdot \omega_{m}$ $\tau_{ind} = K \cdot \phi \cdot I_{A}$ $\frac{\omega_{2}}{\omega_{1}} = \frac{E_{A2}}{E_{A1}} \frac{\phi_{1}}{\phi_{2}} = \frac{n_{2}}{n_{1}}$

Important relationships

 $\frac{\tau_{\text{ind2}}}{\tau_{\text{ind1}}} \frac{\phi_1}{\phi_2} = \frac{I_{\text{A2}}}{I_{\text{A1}}}$

If the field is constant

DC Motors p1



Nameplate Operation

The Nameplate gives the rated Voltage, Current(s), Speed and output Power (often as horsepower, hp). 1 hp = 745.7 W This is considered full-load operation.

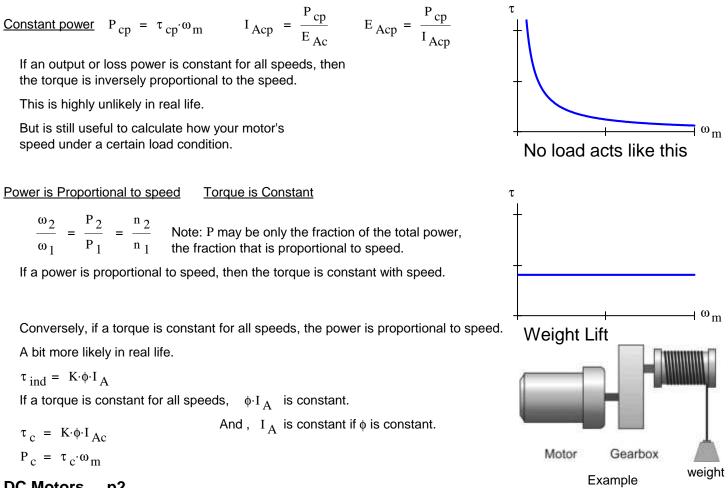
Motor Constant, K

Our book defines the motor constant such that it does not include the field flux, . Often the motor constant is defined differently, as $K\phi$, but just called K, which is a function of the field current. $K\phi$ (or K) is most easily found by operating the motor as a generator with no load, then $V_T = E_A$.

Spin Direction: Reverse the leads to either of the windings and the motor will run in the opposite direction.

Mechanical Loads, Losses and Torgue - Speed Curves

And how the different loads translate into motor calculations.



DC Motors p2

Power is proportional to the Square of the speed, Torque is Proportional to speed

Torque is proportional to speed AND, I A is proportional to speed

 $\frac{\omega_2}{\omega_1} = \frac{\tau_2}{\tau_1} = \frac{\phi_2 \cdot I_{A2}}{\phi_1 \cdot I_{A1}} = \frac{n_2}{n_1} = \frac{E_{A2}}{E_{A1}} \cdot \frac{\phi_1}{\phi_2}$ Note: τ is only the torque that is proportional to speed.

AND, if ALL torque is proportional to $\frac{n}{n} \frac{2}{1} = \frac{V}{V} \frac{T2}{T2}$ speed, AND flux (ϕ) is a constant, $\frac{n}{n} \frac{2}{1} = \frac{V}{V} \frac{T2}{T1}$

Power is proportional to the square of the speed.

 $\frac{\omega_2^2}{\omega_1^2} = \frac{P_2}{P_1} = \frac{n_2^2}{n_1^2}$ Note: P is only the power that is proportional to speed².

Models simple dynamic friction.

Approximates more real-life loads, torque required to turn a load usually increases with speed.

Torque is proportional to the Square of the speed

When an object moves though the air or a fluid, the drag force on the object is usually characterized by a drag coefficient (C_D) which relates the drag force to the velocity squared. This drag coefficient is then adjusted for friction drag, pressure drag, laminar flow and turbulent flow. In short, it's complicated, but a torque can be proportional to the rotational speed squared, at least over some region of operation, especially when air or fluid motion is involved. For us, that means that true load torque-speed curves often curve upward.

$$\frac{\omega_2^2}{\omega_1^2} = \frac{\tau_2}{\tau_1} = \frac{\phi_2 \cdot I_{A2}}{\phi_1 \cdot I_{A1}} = \frac{n_2^2}{n_1^2} = \frac{E_{A2}^2}{E_{A1}^2} \cdot \left(\frac{\phi_1}{\phi_2}\right)^2$$

Also notice the "Breakaway torque" in the last torque-speed curve. That is due to the static, sticky friction (stiction). Almost all real loads have some stiction.

$$\tau_{s} = K \cdot \phi \cdot I_{As} = K_{sload} \cdot \omega_{m}^{2}$$

 $P_{s} = \tau_{s} \cdot \omega_{m} = K_{sload} \cdot \omega_{m}^{3}$

A combination of the last three cases

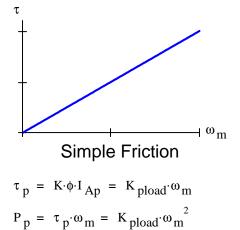
Superposition, separate causes and add results.

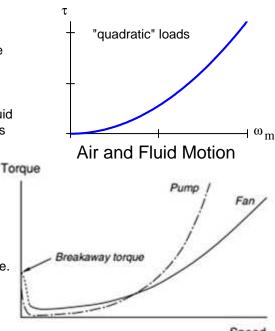
In these cases the power (P), torque (τ) and even the armature current and EMF (I_A and E_A) may be split into multiple pieces, each with its own characteristics.

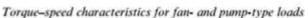
Plus some Stiction

The parts are usual expressed in proportionalities to some known point of operation, like that shown on the nameplate.

Then use the proportionalities to substitute into the basic motor equation:







 $P_{conv} = P_{cp} + P_c + P_p + P_s$

Most likely in real life.

 $\tau_{ind} = \tau_{cp} + \tau_{c} + \tau_{p} + \tau_{s}$ $I_{A} = I_{Acp} + I_{Ac} + I_{Ap} + I_{As}$ $E_{A} = E_{Acp} + E_{Ac} + E_{Ap} + E_{As}$ $V_{T} = I_{A} \cdot R_{A} + E_{A}$

Speed

Torque - Speed curves

to get:
$$V_T = \frac{\tau_{ind}}{K \cdot \phi} \cdot R_A + K \cdot \phi \cdot \omega_m$$
 $\tau_{ind} = \left(V_T - K \cdot \phi \cdot \omega_m \right) \cdot \frac{K \cdot \phi}{R_A}$

 $V_T = I_A \cdot R_A + E_A$

replace: $I_A = \frac{\tau_{ind}}{K \cdot \phi} \qquad E_A = K \cdot \phi \cdot \omega_m$

 $\tau_{\text{ind}} = (V_T) \cdot \frac{K \cdot \phi}{R_A}$

 $0 = \left(V_T - K \cdot \phi \cdot \omega_{max} \right) \cdot \frac{K \cdot \phi}{R_A}$

At 0 speed (locked rotor): $V_T = \frac{\tau_{ind}}{K \cdot \phi} R_A$

At max speed (no induced torque): $V_T = K \cdot \phi \cdot \omega_{max}$

Output Torque instead of Induced Torque

If lost torgue is proportional to speed:

$$\tau_{\text{shaft}} = \tau_{\text{ind}} - \text{fric} \cdot \omega_{\text{m}} \qquad \qquad V_{\text{T}} = \frac{\tau_{\text{shaft}} + \text{fric} \cdot \omega_{\text{m}}}{K \cdot \phi} \cdot R_{\text{A}} + K \cdot \phi \cdot \omega_{\text{m}} \qquad = \frac{\tau_{\text{shaft}}}{K \cdot \phi} \cdot R_{\text{A}} + \left(\frac{\text{fric} \cdot R_{\text{A}}}{K \cdot \phi} + K \cdot \phi\right) \cdot \omega_{\text{m}}$$

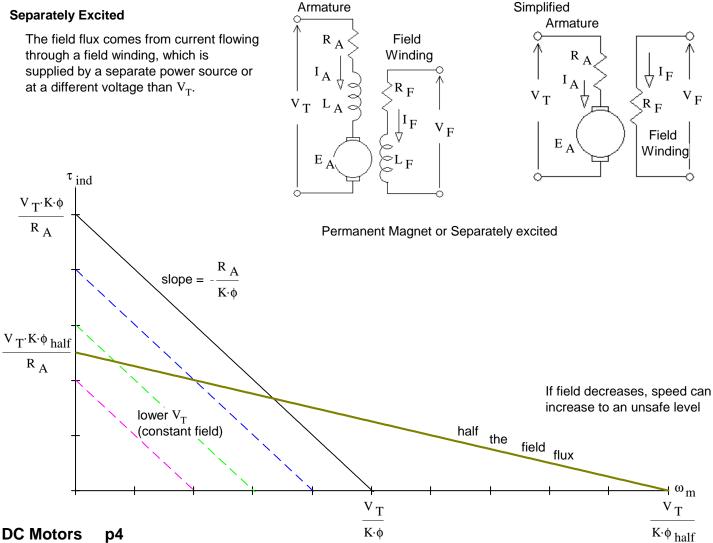
DC Motor Types and Characteristics

Permanent Magnet

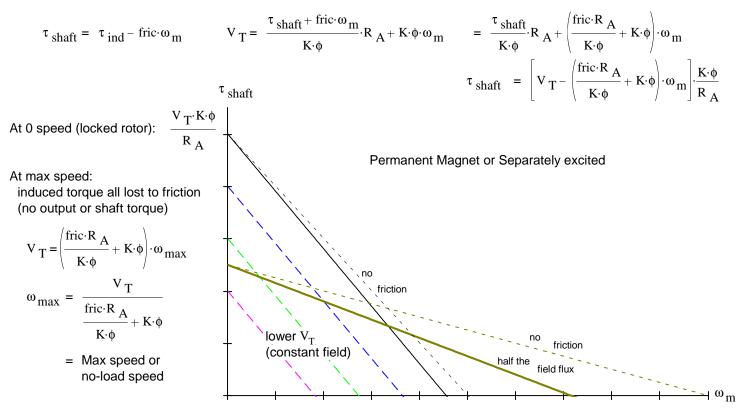
Permanent-Magnet motors are typically small. They can be quite powerful for their size, especially if made with rare-earth magnets. These motors are common in children's toys and servo systems. Some electric cars use Large permanent-magnet DC motors.

The characteristics are like the separately excited motor with a constant flux. Since the flux can't be changed, the motor constant times flux, Ko, is usually simplified to just a different motor constant, usually also called K, which includes the constant flux.

Separately Excited

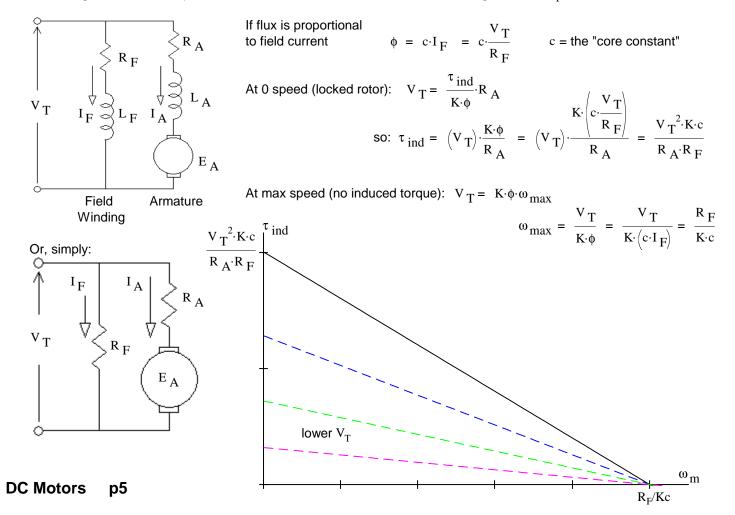


Output Torque instead of Induced Torque, If lost torque is proportional to speed:

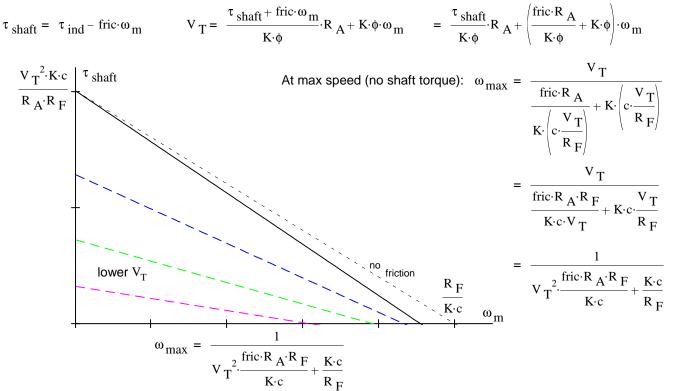


Shunt Excited

Field winding is connected in parallel with the armature to the same terminal voltage source, V_T.

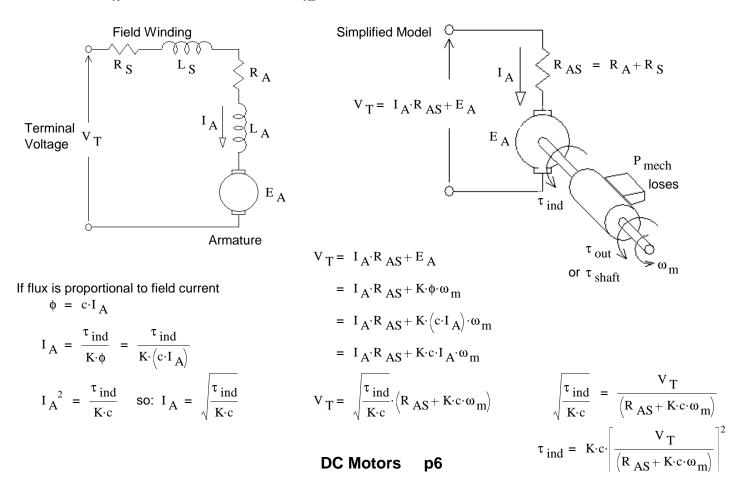


Output Torque instead of Induced Torque, If lost torque is proportional to speed:



Series Excited (Often called an AC/DC or Universal Motor)

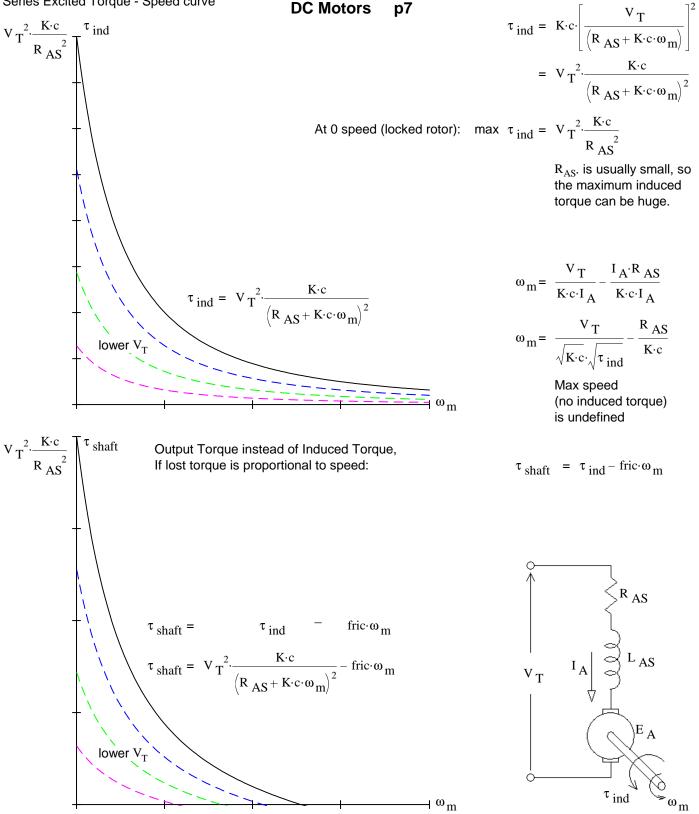
Field winding is connected in series with the armature and is designed with much thicker windings, so it can handle much larger current and has much less resistance. The resistance of the field winding is now called R_S . Since R_S is in series with R_A , they are often combined into R_{AS} .



DC Motors p6

Series Excited Torque - Speed curve

DC Motors p7



AC/DC or Universal Motor (Series Excited DC motor)

Because the same current flows through both the field and the armature, the series-excited motor will turn the same direction even if the current flows the opposite direction-- or even if goes back and forth (AC). These motors are common in AC devices because they can provide a lot of power and torque in small, lightweight motor. They are very common in handheld power tools like drills, saws, grinders, weed eaters, hedge trimmers, etc.. They are also found in vacuum cleaners, blenders and food processors. If you look at the motor of an AC device and see brushes and a commutator, then it is a universal motor.

It is easy to vary the speed of these motors by changing the average voltage, usually with a thyristor-based control similar to a light dimmer.

DC Motors p8

Universal motors tend to be very noisy.

When used with AC supply, the inductance of the windings becomes important.

Compounded Motor

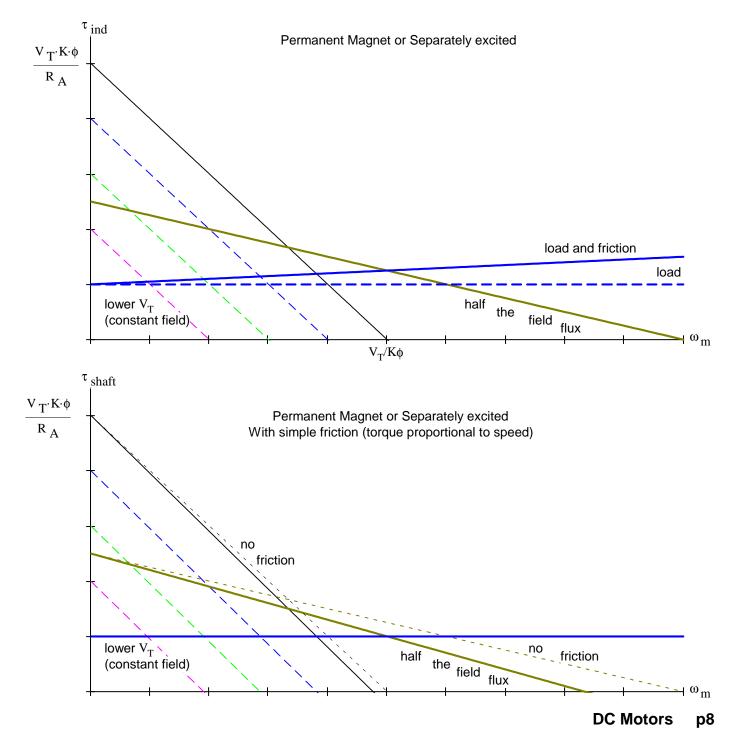
A motor with both shunt and series field windings. Covered in your book, starting on p. 420.

Adding Load Characteristics

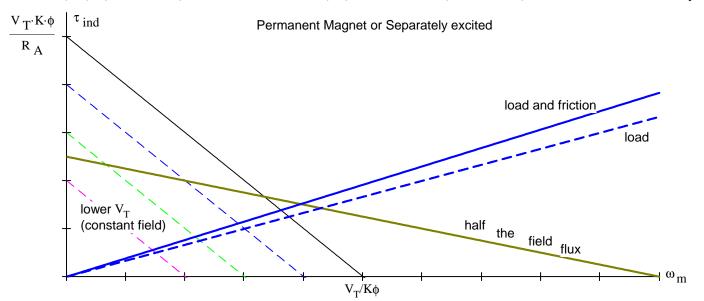
Returning to the Separately Excited (or permanent Magnet) Motor, let's add Load Torque-Speed curves $P = \tau \cdot \omega_m$

Load is Power is Proportional to speed

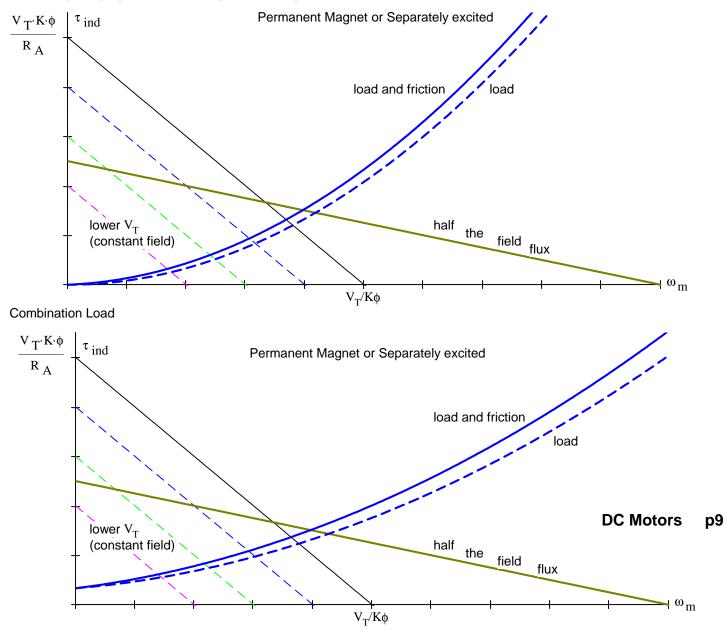
If a power is proportional to speed, then the torque is constant with speed.



p9

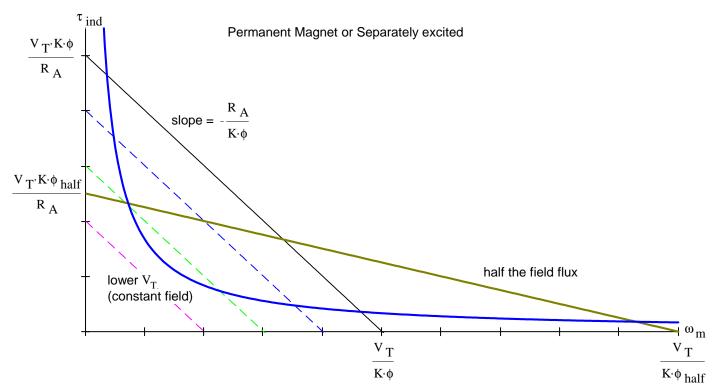


Load Torque is proportional to the square of the speed



Constant power

If an output or loss power is constant for all speeds, then the torque is inversely proportional to the speed.



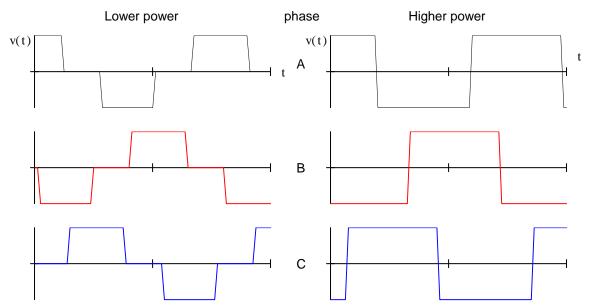
Brushless DC Motors

Many Brushless DC motors simply replace the commutator with a rotor position sensor (magnetic (Hall effect), optic, inductive, etc.) and power-electronic circuitry which switches the winding current. The field is usually on the rotor (permanent magnet or a winding fed through slip rings) and the armature windings are stationary. These motors are analyzed just like DC motors with brushes. Many DC fans are made this way.

Many Brushless DC motors are actually 3-phase Synchronous or Induction motors driven by power-electronic circuitry which produces variable-frequency, Pulse-Width-Modulated (PWM), 3-phase power to operate the motor. Actually, they don't have to be 3-phase, as long as they have at least 2 phases. 2, 3, 4, and 6 phases are common.

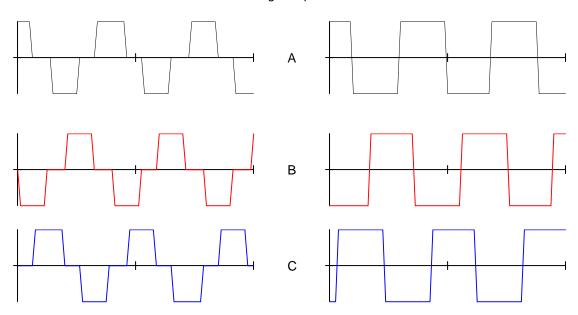
Brushless motors have some important advantages. They are mechanically simpler and more reliable. They can be operated in environments where the sparking between brushes and commutator would be undesirable or unsafe. They are relatively quiet.

Variable-Frequency, Pulse-Width-Modulated (PWM), 3-phase Power



More sample waveforms are shown on the next page.

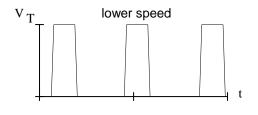
Higher speed

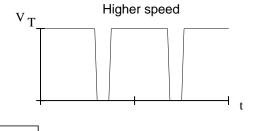


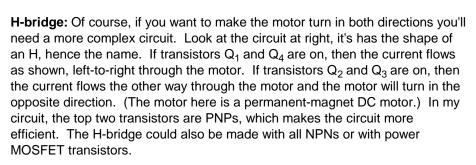
Pulse Width Modulation (PWM) for speed control

As you can see by the torque - speed curves above, regulating the terminal voltage, V_T , is a very effective way to control the speed of a DC motor. Unfortunately, it is often an inefficient process. Pulse Width Modulation, shown here, is a very efficient. It is also more linear, especially at low speeds. The torque - speed curves do not show these non-linearities-- due largely to the difference between static and dynamic friction. (Motors are often a bit sticky at startup.)

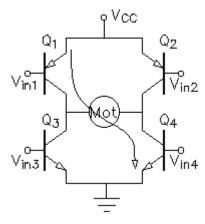
If you do use PWM to control a motor, it is important to remember that the inductance within the windings will not allow the current to go to zero instantaneously. A diode (called a flyback, flywheel, or freewheel diode when used like this) provides a path for the current still flowing through the motor when a pulse is switched off.







An H-bridge requires four inputs, all operated in concert. To turn on Q_1 and Q_4 , as shown, V_{in1} would have to be low and V_{in4} would have to be high. At the same time, the other two transistors would have to be off, so V_{in2} would have to be high and V_{in3} would have to be low.

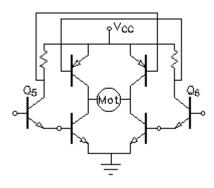


DC Motors p11

DC

。 Notor

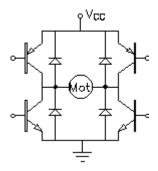
 $|I_D$



If the control circuit makes a mistake and turns on Q_1 and Q_3 (or Q_2 and Q_4) at the same time you'll have a toaster instead of a motor driver, at least for a short while.

The circuit at left requires only two inputs. Transistors Q_5 and Q_6 work as *inverters*, when their inputs are high, their outputs are low and vice-versa. The resistors are known as *pull-up* resistors.

The H-bridge should also include flyback diodes.



Regenerative Braking

Electric motors are not limited to converting electrical energy to mechanical. They can also convert energy from mechanical to electrical. If that is done for the purpose of mechanical braking, say in an electric car, then it's called Regenerative Braking. It is a way recover kinetic energy when slowing a moving mass, or potential energy of a mass moving from a higher to a lower elevation. Examples: a car coming to a stop at a traffic light or driving down Parley's canyon. This recovered energy can be used to recharge batteries or simply be wasted in resistors. Electric lawnmowers and some electric drills use this technique to stop the moving parts very quickly for safety.

Armature Reaction

This phenomenon is well explained in your book, starting on p.372. One effect is a shift of the neutral plane of the field flux. This is a small twisting of the overall North - South orientation and can increase the sparking at the brushes. If the load and rotation direction are known and constant, a small twist of the brush location (in the same direction) will help mitigate the sparking. Interpoles (shown on p. 379) are a better solution. Please note that Fig. 8-11 on p. 374 is for a generator and that ω will be in the opposite direction for a motor. The other effect is an overall flux weakening due to core saturation. A few series windings to shore up the flux at high loads can help with this.

Brush Loss

Sometimes the voltage drop across the brush-commutator connection is also considered. This voltage drop is usually estimated at about 2V for both brushes, regardless of the armature current. (p. 384 in book.)

Characterizing an Unknown DC motor

For a motor that can be operated as separately excited and as a generator; **Motor Constant:** Operate the motor as a generator with no load ($I_A = 0$), then $V_T = E_A$. Calculate K ϕ from speed and E_A measurements. You may wish to calculate this at various field currents.

 R_A : Hook an electrical load to your still-spining generator. Adjust input power to return to no-load speed. Measure V_T and I_A and calculate R_A . You may wish to repeat at several loads and take an average.

Alternatively, measure V_T , I_A , and ω at 2 different mechanical loads, solve 2 equations for 2 unknowns, $K\phi$ and R_A .

$$V_{T1} = I_{A1} \cdot R_{A} + E_{A1} = I_{A1} \cdot R_{A} + K \cdot \phi \cdot \omega_{1}$$

 $V_{T2} = I_{A2} \cdot R_{A} + K \cdot \phi \cdot \omega_{2}$ You may wish to calculate
this at various field currents.

If you can't measure the rotational speed, but can measure the time required to move something a fixed distance, that time would be inversely proportional to speed:

$$V_{T1} = I_{A1} \cdot R_A + \frac{K \cdot \phi \cdot K_T}{t_1}$$

$$V_{T2} = I_{A2} \cdot R_A + \frac{K \cdot \phi \cdot K_T}{t_2}$$

$$K_T \text{ is just another constant which is found together with K\phi as K\phi K_T.$$

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