

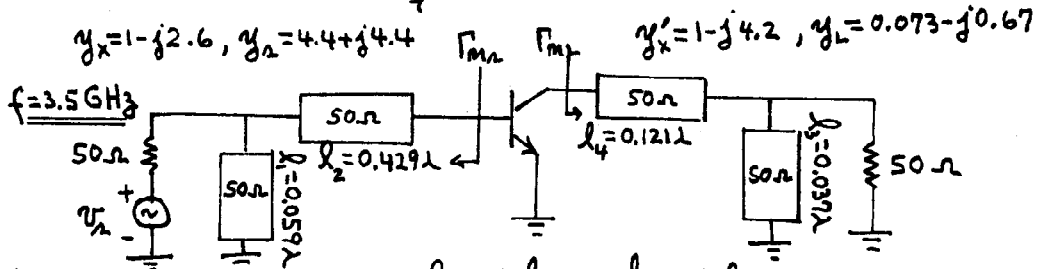
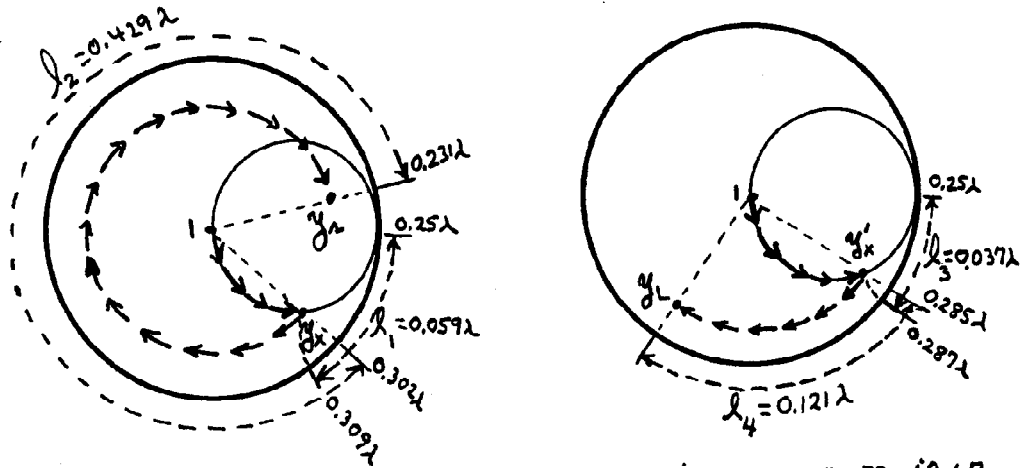
WHICH WILL BE  $y_x = 1$  ( $Z_x = 50\Omega$  OR  $Y_x = 0$ ).

3.24) (a) SINCE  $K = 1.19$  AND  $\Delta = 0.399 \angle 126.5^\circ$  (I.E.,  $|\Delta| < 1$ ) THE BJT IS UNCONDITIONALLY STABLE AT 3.5 GHz. THEREFORE, IT CAN BE DESIGNED FOR A SIMULTANEOUS CONJUGATE MATCH.

(b) FROM (3.6.5) AND (3.6.6):  $\Gamma_{M_L} = 0.798 \angle -166.9^\circ$ ,  $\Gamma_{M_S} = 0.904 \angle 68^\circ$

FROM (3.6.10):  $G_{T,max} = 23.06$  OR  $13.63$  dB.

A DESIGN FOR THE AMPLIFIER AT 3.5 GHz IS:



(c)

$f$ (GHz)	$\lambda$	$\lambda_1$	$\lambda_2$	$\lambda_3$	$\lambda_4$	
$f_1 = 3$	$\lambda_1 = \frac{c}{f_1}$	$\lambda_2 = \frac{f_1}{f_2} \lambda_1 = 0.857 \lambda_1$	$0.051 \lambda_1$	$0.368 \lambda_1$	$0.032 \lambda_1$	$0.104 \lambda_1$
$f_2 = 3.5$	$\lambda_2 = \frac{c}{f_2}$	$\lambda_2$	$0.059 \lambda_2$	$0.429 \lambda_2$	$0.037 \lambda_2$	$0.121 \lambda_2$
$f_3 = 4$	$\lambda_3 = \frac{c}{f_3}$	$\lambda_2 = \frac{f_3}{f_2} \lambda_3 = 1.143 \lambda_3$	$0.067 \lambda_3$	$0.49 \lambda_3$	$0.042 \lambda_3$	$0.138 \lambda_3$

USING THE SMITH CHART IT IS SIMPLE TO FIND THE VALUES OF  $\Gamma_L$  AND  $\Gamma_R$  AT  $f_1$  AND  $f_3$ . THE VALUES OF  $G_T$  ARE CALCULATED USING

(3.2.1). THE RESULTS ARE:

$f$ (GHz)	$\Gamma_L$	$\Gamma_R$	$G_T$
3	0.833 $\angle$ -118.5°	0.934 $\angle$ 82.2°	0.944 OR -0.25 dB
3.5	0.798 $\angle$ -166.9°	0.904 $\angle$ 68°	23.06 OR 13.63 dB
4	0.749 $\angle$ 145.6°	0.878 $\angle$ 51.5°	2.257 OR 3.54 dB

3.25(a) THE TRANSISTOR IS UNCONDITIONALLY STABLE ( $K=1.033$ ,  $\Delta=0.324 \angle -64.8^\circ$ )

WITH  $g_p = \frac{G_p}{|S_{21}|^2} = \frac{10}{(1.92)^2} = 2.713$ , WE OBTAIN FROM (3.7.4) AND (3.7.5):

$$C_p = 0.781 \angle 33.85^\circ \quad \text{AND} \quad \gamma_p = 0.214$$

THE  $G_p=10\text{dB}$  GAIN CIRCLE IS DRAWN IN THE SMITH CHART. SELECTING  $\Gamma_L$  AT POINT "A":  $\Gamma_L = 0.567 \angle 33.85^\circ$ , GIVES

$$\Gamma_{IN} = \Gamma_{IN}^* = 0.276 \angle 93.33^\circ$$

AND  $\Gamma_{OUT} = 0.86 \angle -33.85^\circ$

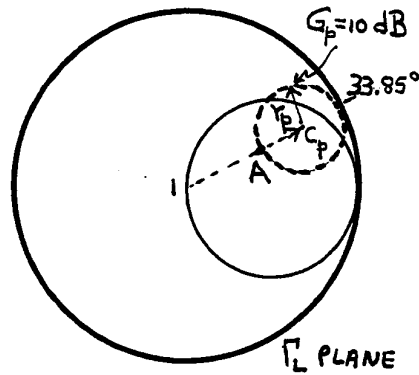
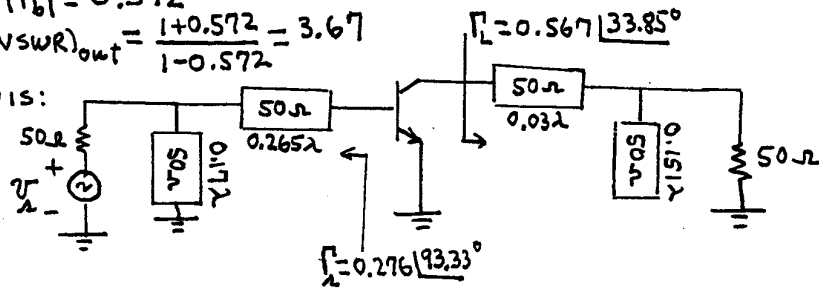
FROM (2.8.3):  $|\Gamma_{IN}| = 0$  (SINCE  $\Gamma_{IN} = \Gamma_{IN}^*$ )

HENCE:  $(VSWR)_{IN} = 1$

FROM (2.9.6):  $|\Gamma_b| = 0.572$

HENCE:  $(VSWR)_{out} = \frac{1+0.572}{1-0.572} = 3.67$

A DESIGN IS:



(b)  $G_{p,max} = G_{T,max} = 19.08$  OR  $12.8\text{dB}$

THE  $G_{p,max}$  GAIN CIRCLE (i.e., a point) OCCURS AT:

$$g_{p,max} = \frac{G_{p,max}}{|S_{21}|^2} = \frac{19.08}{(1.92)^2} = 5.176, \quad C_{p,max} = 0.95 \angle 33.8^\circ, \quad \gamma_{p,max} = 0.$$

OBSERVE (SEE PROBLEM 3.21) THAT:  $\Gamma_{ML} = C_{p,max} = 0.95 \angle 33.8^\circ$

AND  $\Gamma_{IN} = \Gamma_{IN}^* = 0.73 \angle 135^\circ$  IS IDENTICAL TO  $\Gamma_{ML}$ .

3.26) FOR THIS TRANSISTOR:  $K=1.053$  AND  $\Delta=0.576 \angle -85.4^\circ$ .  
THEREFORE, IT IS UNCONDITIONALLY STABLE.

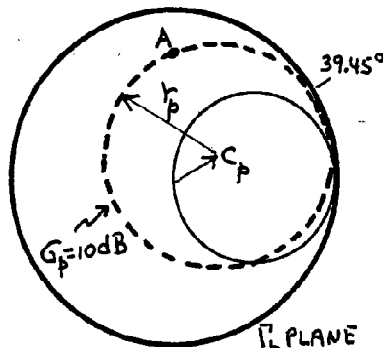
$$G_{p,max} = G_{T,max} = 77.12 \text{ OR } 18.87 \text{ dB}$$

$$G_p = 10 \text{ dB CIRCLE: } g_p = 0.977, C_p = 0.306 \angle 39.45^\circ, \gamma_p = 0.693$$

THE  $G_p = 10 \text{ dB}$  CONSTANT-GAIN CIRCLE  
IS SHOWN IN THE SMITH CHART. THE  $\Gamma_L$   
SELECTED IS SHOWN AS "A":  $\Gamma_L = 0.85 \angle 89^\circ$ .  
THEN:  $\Gamma_{in} = \Gamma_{in}^* = 0.793 \angle 64.2^\circ$ ,  $\Gamma_{out} = 0.798 \angle -42.3^\circ$

$$|\Gamma_a| = 0, (VSWR)_{in} = 1$$

$$|\Gamma_b| = 0.9, (VSWR)_{out} = 18.9$$



3.27) (a)  $K=0.53$ ,  $\Delta=0.524 \angle -142.9^\circ$ ; IT IS POTENTIALLY UNSTABLE.

OUTPUT STABILITY CIRCLE [(3.3.7) AND (3.3.8)]:

$$C_L = 1.47 \angle 76.6^\circ \text{ AND } \gamma_L = 0.668$$

$G_p = 10 \text{ dB}$  CONSTANT-GAIN CIRCLE [(3.7.4) AND (3.7.5)]:  $g_p = \frac{10}{(2.43)^2} = 1.694$ ,  
 $C_p = 0.41 \angle 76.6^\circ$  AND  $\gamma_p = 0.641$

(b) THE  $G_p = 10 \text{ dB}$  GAIN CIRCLE IS DRAWN ON THE SMITH CHART. THREE  
VALUES OF  $\Gamma_L$  ARE DENOTED BY "a", "b", AND "c". THEN,

	$\Gamma_L$	$\Gamma_{in} = \Gamma_{in}^*$	$\Gamma_{out}$	$ \Gamma_b $	$(VSWR)_{in}$	$(VSWR)_{out}$
"a"	$0.59 \angle 0^\circ$	$0.687 \angle 106.11^\circ$	$0.84 \angle -70.73^\circ$	0.889	1	17
"b"	$0.24 \angle -90^\circ$	$0.757 \angle 100.35^\circ$	$0.83 \angle -76.22^\circ$	0.891	1	17.3
"c"	$0.67 \angle 145^\circ$	$0.851 \angle 97.7^\circ$	$0.84 \angle -83.74^\circ$	0.889	1	17

THE 3 VALUES OF  $\Gamma_L$  ARE IN THE STABLE REGION, SINCE  $C_L = 1.3 \angle 115.7^\circ$  AND  $\gamma_L = 0.46$ .

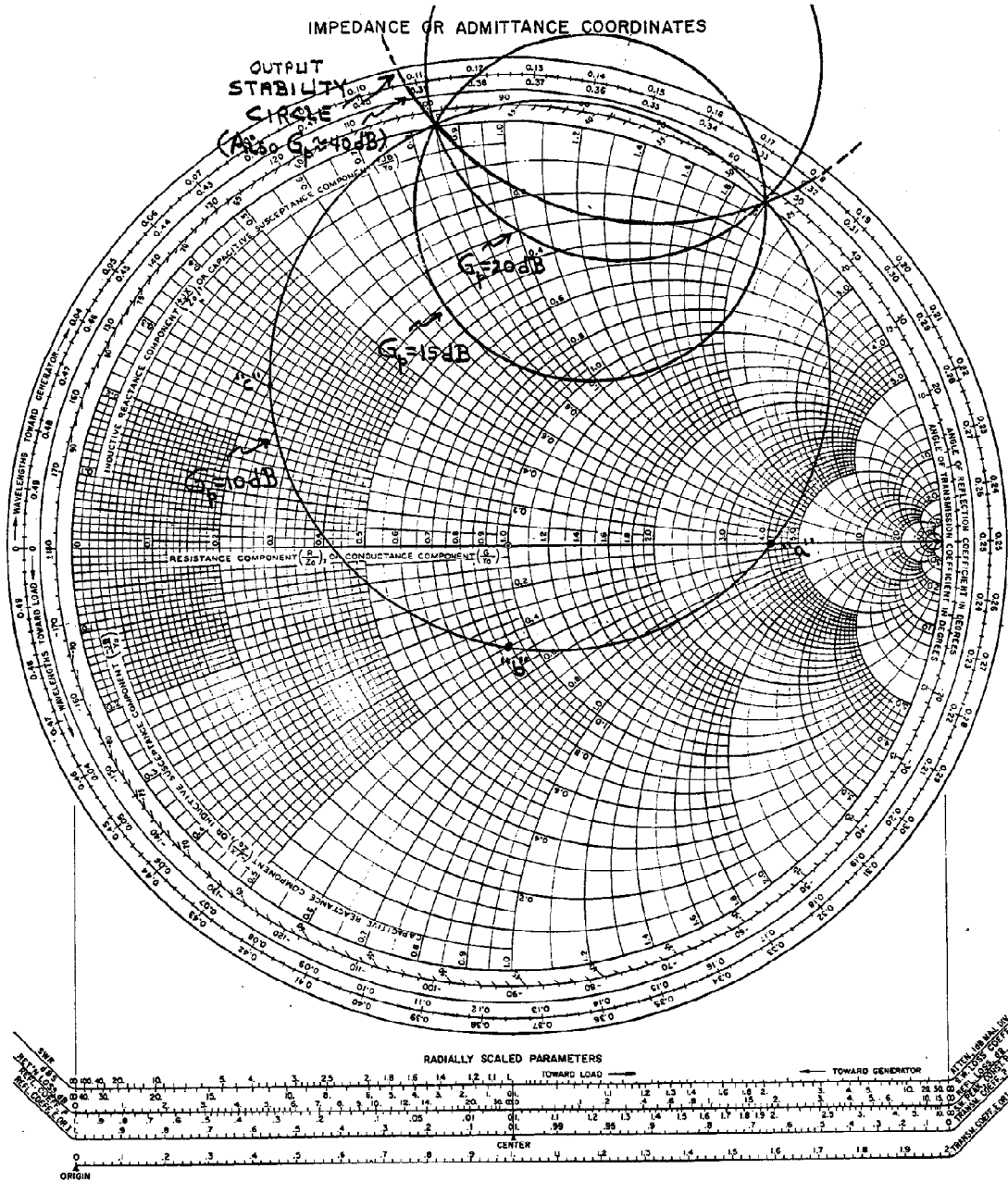
(c) FOR  $G_p = 15 \text{ dB}$ :  $g_p = \frac{10^{1.5}}{(2.43)^2} = 5.355$ ,  $C_p = 0.81 \angle 76.6^\circ$ ,  $\gamma_p = 0.402$

FOR  $G_p = 20 \text{ dB}$ :  $g_p = \frac{10^2}{(2.43)^2} = 16.94$ ,  $C_p = 1.17 \angle 76.6^\circ$ ,  $\gamma_p = 0.457$

FOR  $G_p = 40 \text{ dB}$ :  $g_p = \frac{10^4}{(2.43)^2} = 1694$ ,  $C_p = 1.46 \angle 76.6^\circ$ ,  $\gamma_p = 0.665$

THE  $G_p = 15 \text{ dB}$ ,  $20 \text{ dB}$ , AND  $40 \text{ dB}$  GAIN CIRCLES ARE ALSO DRAWN  
ON THE SMITH CHART. THE  $G_p = 40 \text{ dB}$  CIRCLE ALMOST COINCIDES WITH  
THE OUTPUT STABILITY CIRCLE.

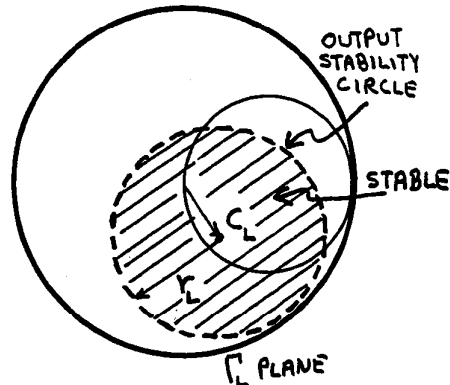
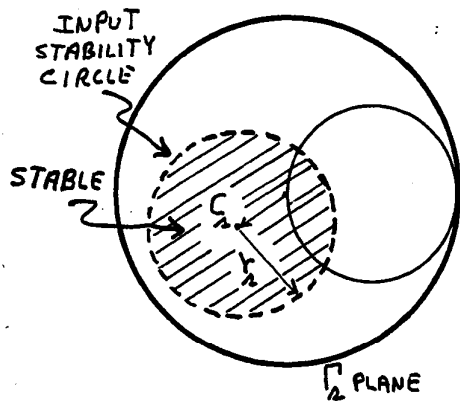
IMPEDANCE OR ADMITTANCE COORDINATES



3.29) (a)  $K = 1.032$ ,  $\Delta = 1.65 \angle 78.1^\circ$   $\therefore$  POTENTIALLY UNSTABLE

FROM (3.3.7) TO (3.3.10):

$$\text{INPUT STAB. CIRCLE} \begin{cases} C_2 = 0.285 \angle -161.1^\circ \\ r_2 = 0.65 \end{cases} \quad \text{OUTPUT STAB. CIRCLE} \begin{cases} C_L = 0.315 \angle -61.5^\circ \\ r_L = 0.627 \end{cases}$$



(b) FROM (3.2.3) WITH  $\Gamma_L = 0$ : (AND  $\Gamma_{IN} = S_{11}$  WHEN  $\Gamma_L = 0$ )

$$G_p = \frac{|S_{21}|^2}{1 - |S_{11}|^2} = \frac{4^2}{1 - (0.5)^2} = 21.33 \text{ OR } 13.3 \text{ dB}$$

(c)  $G_p$  CAN BE INFINITE, BECAUSE IT IS POTENTIALLY UNSTABLE.  
AS  $\Gamma_L$  APPROACHES THE STABILITY CIRCLE,  $G_p \rightarrow \infty$ .

3.30) FROM EXAMPLE 3.8.1:  $G_{A, \max} = 9.66 \text{ dB}$ ,  $G_A = 9.66 - 2 = 7.66 \text{ dB}$ .

FROM (3.7.15) AND (3.7.16), FOR THE  $G_A = 7.66 \text{ dB}$  GAIN CIRCLE:

$$g_a = \frac{10^{0.766}}{(2.3)^2} = 1.103, \quad C_a = 0.503 \angle -40.45^\circ, \quad r_a = 0.436$$

THE VALUES OF  $\Gamma_a$  ON THE 7.6 dB GAIN CIRCLE ARE GIVEN BY:

$$\Gamma_a = C_a + r_a e^{j\theta_1} = 0.503 \angle -40.45^\circ + 0.436 e^{j\theta_1}$$

LETTING  $\theta_1 = 0, \frac{\pi}{2}, \pi$ , AND  $\frac{3\pi}{2}$  WE OBTAIN THE VALUES OF  $\Gamma_a$  SHOWN IN THE TABLE. THE ASSOCIATED VALUES OF  $\Gamma_{OUT}$  ARE ALSO SHOWN.

FOR  $(VSWR)_{out} = 1.5$  (OR  $|\Gamma_b| = 0.2$ ), USING (3.8.7) AND (3.8.8), THE CENTER AND RADIUS OF THE  $(VSWR)_{out} = 1.5$  CIRCLE ARE CALCULATED.

THE VALUES OF  $\Gamma_L$  ON THE  $(VSWR)_{out} = 1.5$  CIRCLE ARE GIVEN BY:

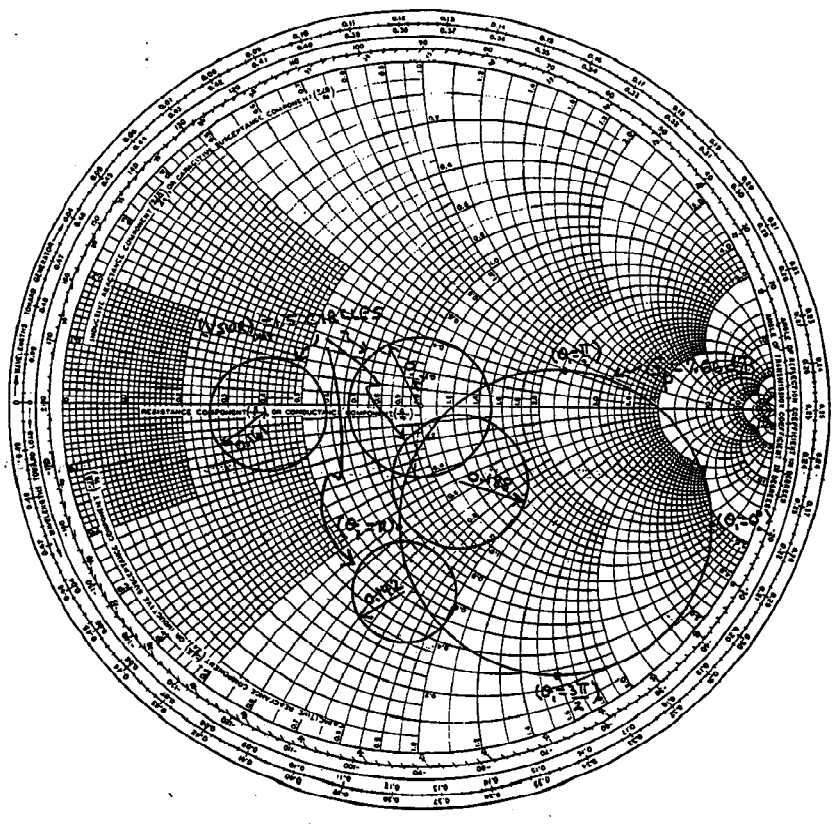
$$\Gamma_L = C_v + r_v e^{j\theta_2}. \text{ LETTING } \theta_2 = 0, \frac{\pi}{2}, \pi, \text{ AND } \frac{3\pi}{2}, \text{ FOUR VALUES OF } \Gamma_L \text{ ON THE } (VSWR)_{out} = 1.5 \text{ CIRCLE ARE CALCULATED, AS SHOWN IN THE TABLE.}$$

THE ASSOCIATED VALUES OF  $\Gamma_{IN}$ ,  $|\Gamma_a|$ , AND  $(VSWR)_{in}$  ARE ALSO SHOWN.

$\Gamma_{in}$	$\Gamma_{out}$	(VSWR) <sub>act</sub> CIRCLE	$\Gamma_L$	$\Gamma_{IN}$	$ \Gamma_a $	(VSWR) <sub>in</sub>
$(\theta_1 = 0^\circ)$ $0.881 \angle -21.73^\circ$	$0.451 \angle 176.74^\circ$	$C_{V_0} = 0.437 \angle -176.74^\circ$ $\Gamma_{V_0} = 0.161$	$0.276 \angle -174.8^\circ (\theta_2 = 0)$	$0.683 \angle 33.8^\circ$	0.596	3.95
			$0.457 \angle 162.7^\circ (\theta_2 = \frac{\pi}{2})$	$0.712 \angle 28.8^\circ$	0.507	3.05
			$0.598 \angle -177.6^\circ (\theta_2 = \pi)$	$0.771 \angle 30.9^\circ$	0.495	2.96
			$0.474 \angle -156.7^\circ (\theta_2 = \frac{3\pi}{2})$	$0.748 \angle 35.7^\circ$	0.604	4.05
$(\theta_1 = \pi/2)$ $0.398 \angle 15.99^\circ$	$0.005 \angle 95.36^\circ$	$C_{V_0} = 0.005 \angle -95.36^\circ$ $\Gamma_{V_0} = 0.2$	$0.2 \angle -1.4^\circ (\theta_2 = 0)$	$0.539 \angle 38.5^\circ$	0.501	3.00
			$0.195 \angle 90.1^\circ (\theta_2 = \frac{\pi}{2})$	$0.582 \angle 30.3^\circ$	0.491	2.93
			$0.2 \angle -178.6^\circ (\theta_2 = \pi)$	$0.659 \angle 34^\circ$	0.591	3.89
			$0.2 \angle -90.1^\circ (\theta_2 = \frac{3\pi}{2})$	$0.628 \angle 41.5^\circ$	0.598	3.98
$(\theta_1 = \pi)$ $0.331 \angle -99.26^\circ$	$0.249 \angle 62.12^\circ$	$C_{V_0} = 0.241 \angle -62.12^\circ$ $\Gamma_{V_0} = 0.188$	$0.368 \angle -35.2^\circ (\theta_2 = 0)$	$0.539 \angle 47^\circ$	0.473	2.79
			$0.115 \angle -12.1^\circ (\theta_2 = \frac{\pi}{2})$	$0.569 \angle 38^\circ$	0.543	3.38
			$0.225 \angle -109.6^\circ (\theta_2 = \pi)$	$0.652 \angle 40.8^\circ$	0.613	4.17
			$0.416 \angle -74.3^\circ (\theta_2 = \frac{3\pi}{2})$	$0.633 \angle 48.8^\circ$	0.56	3.54
$(\theta_1 = 3\pi/2)$ $0.853 \angle -63.34^\circ$	$0.547 \angle 94.15^\circ$	$C_{V_0} = 0.531 \angle -94.15^\circ$ $\Gamma_{V_0} = 0.142$	$0.54 \angle -78.9^\circ (\theta_2 = 0)$	$0.666 \angle 51.8^\circ$	0.526	3.22
			$0.39 \angle -95.6^\circ (\theta_2 = \frac{\pi}{2})$	$0.673 \angle 45.7^\circ$	0.606	4.07
			$0.559 \angle -108.8^\circ (\theta_2 = \pi)$	$0.742 \angle 46.3^\circ$	0.597	3.97
			$0.673 \angle -93.3^\circ (\theta_2 = \frac{3\pi}{2})$	$0.74 \angle 51.9^\circ$	0.485	2.88

10.612 | 1.17 |  $\sqrt{2} = 1.414$  | 10.74 | 10.485 | 4.80

FROM THESE CALCULATIONS IT IS SEEN THAT A DESIGN WITH  
 $\Gamma_{\lambda} = 0.331 \angle -99.26^\circ$  AND  $\Gamma_L = 0.368 \angle -35.2^\circ$  RESULTS IN  $(VSWR)_{CH} = 2.79$  AND  $(VSWR)_{OUT} = 1.5$ .





3.31) (a)  $K=1.344$ ,  $\Delta=2.156 \angle -16.6^\circ \therefore$  POTENTIALLY UNSTABLE

(b) OUTPUT STABILITY CIRCLE:  $C_L=0.261 \angle -36.3^\circ$ ,  $r_L=0.409$

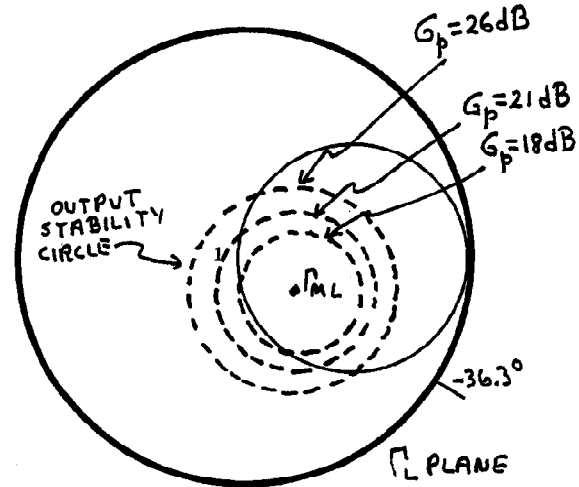
(c) FROM (3.6.6) (USING THE + SIGN):  $\Gamma_{ML}=0.319 \angle -36.3^\circ$

(d)  $G_{p,max}=G_{T,min}=44.82$  OR  $16.51$  dB

(e)

$G_p$	CENTER RADIUS
18 dB	$\begin{cases} C_p=0.31 \angle -36.3^\circ \\ r_p=0.234 \end{cases}$
21 dB	$\begin{cases} C_p=0.281 \angle -36.3^\circ \\ r_p=0.34 \end{cases}$
26 dB	$\begin{cases} C_p=0.266 \angle -36.3^\circ \\ r_p=0.39 \end{cases}$
36 dB	$\begin{cases} C_p=0.261 \angle -36.3^\circ \\ r_p=0.407 \end{cases}$

THE 26 dB GAIN CIRCLE, THE 36 dB GAIN CIRCLE, AND THE OUTPUT STABILITY CIRCLE ALMOST COINCIDE.



(f) INPUT STABILITY CIRCLE:  $C_2=0.102 \angle 107.4^\circ$ ,  $r_2=0.44$

FROM (3.6.5) (USING THE + SIGN):  $\Gamma_{M2}=0.127 \angle 107.44^\circ$

(g)  $(VSWR)_{in}=(VSWR)_{out}=1$ .

3.32) (a)  $K=1.17$ ,  $\Delta=0.368 \angle 27.9^\circ$  UNCONDITIONALLY STABLE

$G_{p,max}=9.24$  OR  $9.66$  dB,  $G_p=9.66-1=8.66$  dB

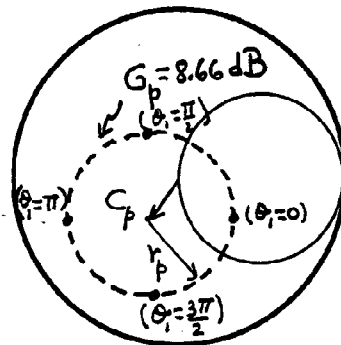
FOR THE  $G_p=8.66$  dB CIRCLE:  $g_p=1.388$ ,  $C_p=0.292 \angle -129.4^\circ$ ,  $r_p=0.466$

(b) THE VALUES OF  $\Gamma_L$  ON THE 8.66 dB CIRCLE ARE:

$$\Gamma_L = C_p + r_p e^{j\theta_1} = 0.292 \angle -129.4^\circ + 0.466 e^{j\theta_1}$$

LETTING  $\theta_1=0, \pi, \pi$ , AND  $\frac{3\pi}{2}$  WE OBTAIN THE VALUES OF  $\Gamma_L$  SHOWN IN THE TABLE. THE ASSOCIATED VALUES OF  $\Gamma_{IN}$  ARE ALSO SHOWN.

FOR  $(VSWR)_{in}=1.5$  (OR  $|\Gamma_{in}|=0.2$ ), USING (3.8.3) AND (3.8.4), THE CENTER AND RADIUS OF THE  $(VSWR)_{in}=1.5$  CIRCLE ARE CALCULATED.



(c) THE VALUES OF  $\Gamma_L$  ON THE  $(VSWR)_{in} = 1.5$  CIRCLE ARE GIVEN BY  $\Gamma_L = C_{V_i} + \gamma_i e^{j\theta_2}$ . LETTING  $\theta_2 = 0$  AND  $\pi$ , TWO VALUES OF  $\Gamma_L$  ON THE  $(VSWR)_{in} = 1.5$  CIRCLE ARE CALCULATED (SEE THE TABLE). THE ASSOCIATED VALUES OF  $\Gamma_{OUT}$ ,  $|\Gamma_b|$ , AND  $(VSWR)_{OUT}$  ARE ALSO SHOWN

$\Gamma_L$	$\Gamma_{IN}$	$(VSWR)_{in} = 1.5$ CIRCLE	$\Gamma_L$	$\Gamma_{OUT}$	$ \Gamma_b $	$(VSWR)_{out}$
$(\theta_1 = 0)$ $0.36 \angle -38.8^\circ$	$0.548 \angle 47.1^\circ$	$C_{V_i} = 0.532 \angle -47.1^\circ$ $\gamma_i = 0.142$	$0.637 \angle -37.7^\circ (\theta_2 = 0)$ $0.448 \angle -60.5^\circ (\theta_2 = \pi)$	$0.311 \angle 129.5^\circ$ $0.259 \angle 91.2^\circ$	$0.475$ $0.304$	$2.8$ $1.875$
$(\theta_1 = \pi/2)$ $0.304 \angle 127.6^\circ$	$0.634 \angle 27.9^\circ$	$C_{V_i} = 0.619 \angle -27.9^\circ$ $\gamma_i = 0.122$	$0.729 \angle -23.4^\circ (\theta_2 = 0)$ $0.514 \angle -34.3^\circ (\theta_2 = \pi)$	$0.314 \angle 161.7^\circ$ $0.219 \angle 123.5^\circ$	$0.368$ $0.419$	$2.16$ $2.44$
$(\theta_1 = \pi)$ $0.689 \angle -160.9^\circ$	$0.81 \angle 34.2^\circ$	$C_{V_i} = 0.799 \angle -34.2^\circ$ $\gamma_i = 0.071$	$0.859 \angle -31.5^\circ (\theta_2 = 0)$ $0.741 \angle -37.3^\circ (\theta_2 = \pi)$	$0.501 \angle 153.7^\circ$ $0.399 \angle 136.2^\circ$	$0.306$ $0.483$	$1.88$ $2.87$
$(\theta_1 = 3\pi/2)$ $0.716 \angle -105^\circ$	$0.782 \angle 49.4^\circ$	$C_{V_i} = 0.77 \angle -49.4^\circ$ $\gamma_i = 0.08$	$0.824 \angle -45.2^\circ (\theta_2 = 0)$ $0.721 \angle -54.2^\circ (\theta_2 = \pi)$	$0.518 \angle 124.3^\circ$ $0.429 \angle 107.5^\circ$	$0.430$ $0.415$	$2.51$ $2.42$

FROM THESE CALCULATIONS IT IS SEEN THAT A DESIGN WITH  $\Gamma_L = 0.689 \angle -160.9^\circ$  AND  $\Gamma_A = 0.859 \angle -31.5^\circ$  GIVES:  $G_p = 8.66$  dB,  $(VSWR)_{in} = 1.88$ ,  $(VSWR)_{out} = 1.5$ .

3.33) (a) FROM EXAMPLE 3.7.2, FOR THE  $G_p = 10$  dB CIRCLE:  $C_p = 0.572 \angle 97.2^\circ$ ,  $\gamma_p = 0.473$   
FROM (3.8.9) AND (3.8.10), WITH  $C_{oo} = C_p$  AND  $\gamma_{oo} = \gamma_p$ , WE OBTAIN:  
 $C_i = 1.131 \angle 170.6^\circ$  AND  $\gamma_i = 0.622$

(b) FOR  $\Gamma_L = 0.1 \angle 97^\circ$ ,  $\Gamma_{IN}^* = 0.52 \angle 179.32^\circ$

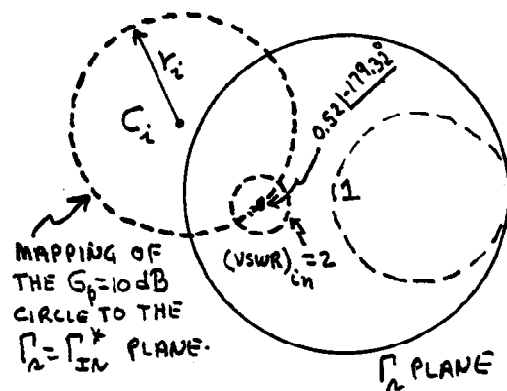
$$\Gamma_A = \Gamma_{IN}^* = 0.52 \angle -179.32^\circ$$

THEN  $(VSWR)_{in} = 1$

FOR  $(VSWR)_{in} = 2$  (OR  $|\Gamma_A| = 0.333$ ),

WE OBTAIN FROM (3.8.3) AND (3.8.4):

$$C_{V_i} = 0.477 \angle 179.32^\circ, \gamma_i = 0.251$$



3.34)  $K=0.924$ ,  $\Delta=0.137 \angle -139^\circ$   $\therefore$  POTENTIALLY UNSTABLE

$$G_{MSG} = \frac{|S_{21}|}{|S_{12}|} = \frac{8}{0.03} = 266.6 \text{ OR } 24.3 \text{ dB}$$

DESIGN FOR  $G_p=20 \text{ dB}$  (i.e., 4.3 dB LESS THAN  $G_{MSG}$ ).

OUTPUT STABILITY CIRCLE:

$$C_L = 2.26 \angle 40.1^\circ, \quad \gamma_L = 1.307$$

$G_p=20 \text{ dB}$  CONSTANT-GAIN CIRCLE: ( $g_p=1.563$ )

$$C_p = 0.505 \angle 40.1^\circ, \quad \gamma_p = 0.519$$

VALUES OF  $\Gamma_L$  ON  $G_p=20 \text{ dB}$  CIRCLE:

$$\Gamma_L = C_p + \gamma_p e^{j\theta} = 0.505 \angle 40.1^\circ + 0.519 e^{j\theta}$$

THE TABLE SHOWS TWO VALUES OF  $\Gamma_L$  (i.e., for  $\theta_1 = \pi$  AND  $\theta_2 = \frac{3\pi}{2}$ ), THE ASSOCIATED VALUES OF  $\Gamma_{in}^*$ ,  $\Gamma_{out}$ ,  $|\Gamma_b|$ , AND  $(VSWR)_{out}$ .

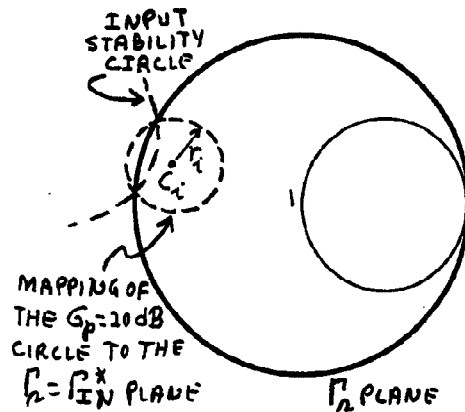
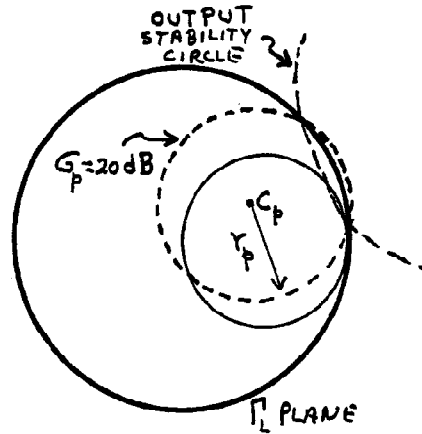
$\Gamma_L$	$\Gamma_{in}^*$	$(VSWR)_{in}$	$\Gamma_{out}$	$ \Gamma_b $	$(VSWR)_{out}$
( $\theta_1 = \pi$ ) $0.352 \angle 112.2^\circ$	$0.655 \angle 163.4^\circ$	1	$0.668 \angle -44.8^\circ$	0.667	30.25
( $\theta_2 = \frac{3\pi}{2}$ ) $0.432 \angle -26.6^\circ$	$0.607 \angle -179.2^\circ$	1	$0.674 \angle -34.3^\circ$	0.668	30.25

MAPPING OF THE  $G_p=20 \text{ dB}$  CIRCLE TO THE  $\Gamma_{in}^*$  PLANE:

$$C_i = 0.823 \angle 175.3^\circ, \quad \gamma_i = 0.227$$

INPUT STABILITY CIRCLE:  $C_{in} = 1.65 \angle 175.3^\circ, \quad \gamma_{in} = 0.679$

THE VALUES OF  $(VSWR)_{out} = 30.25$  SHOW THAT THE OUTPUT HAS TO BE MISMATCHED IN ORDER TO REDUCE THE GAIN TO 20 dB. THE DESIGNER CAN TRY TO REDUCE  $(VSWR)_{out}$  BY RELAXING THE INPUT VSWR VALUE (SAY, LET  $(VSWR)_{in} \leq 1.5$ ), AS DISCUSSED IN EXAMPLE 3.8.2.



3.35)  $K = 0.875$ ,  $\Delta = 0.445 \angle 160.4^\circ$   $\therefore$  POTENTIALLY UNSTABLE

$$G_{MSG} = \frac{|S_{21}|}{|S_{12}|} = \frac{3.1}{0.125} = 24.8 \text{ OR } 13.9 \text{ dB}$$

DESIGN FOR  $G_A = 10 \text{ dB}$  (i.e, 3.9 dB LESS THAN  $G_{MSG}$ )

INPUT STABILITY CIRCLE:

$$C_A = 3.303 \angle -173.2^\circ, \quad r_A = 2.392$$

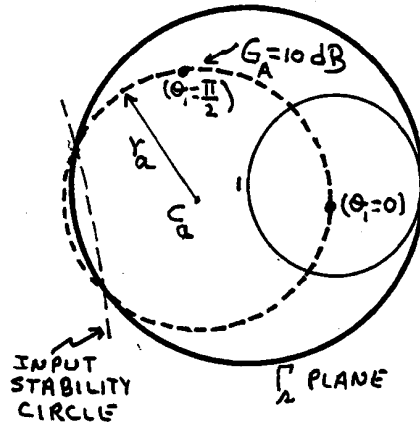
$G_A = 10 \text{ dB}$  CONSTANT-GAIN CIRCLE: ( $g_A = 1.041$ )

$$C_a = 0.296 \angle -173.2^\circ, \quad r_a = 0.73$$

VALUES OF  $\Gamma_L$  ON THE  $G_A = 10 \text{ dB}$  CIRCLE:

$$\Gamma_L = C_a + r_a e^{j\theta_1} = 0.296 \angle -173.2^\circ + 0.73 e^{j\theta_1}$$

THE TABLE SHOWS TWO VALUES OF  $\Gamma_L$  (i.e, for  $\theta_1 = 0$  AND  $\theta_1 = \pi/2$ ), THE ASSOCIATED VALUES OF  $\Gamma_L = \Gamma_{OUT}^*$ ,  $\Gamma_{IN}$ ,  $|\Gamma_a|$ , AND  $(VSWR)_{in}$ .



$\Gamma_L$	$\Gamma_L = \Gamma_{OUT}^*$	$(VSWR)_{OUT}$	$\Gamma_{IN}$	$ \Gamma_a $	$(VSWR)_{in}$
$(\theta_1 = 0)$ $0.437 \angle -4.6^\circ$	$0.405 \angle 70.8^\circ$	1	$0.565 \angle 172^\circ$	0.802	9.1
$(\theta_1 = \pi/2)$ $0.755 \angle 112.9^\circ$	$0.08 \angle 133.5^\circ$	1	$0.624 \angle -171.9^\circ$	0.802	9.1

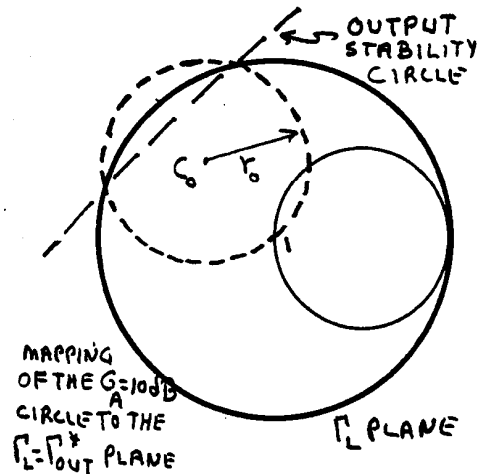
MAPPING OF THE  $G_A = 10 \text{ dB}$  CIRCLE TO THE  $\Gamma_L = \Gamma_{OUT}^*$  PLANE:

$$C_o = 0.646 \angle 130.9^\circ \text{ AND } r_o = 0.566$$

OUTPUT STABILITY CIRCLE:

$$C_L = 9.33 \angle -49.1^\circ, \quad r_L = 10.19$$

THE VALUES OF  $(VSWR)_{in} = 9.1$  SHOW THAT THE INPUT HAS TO BE MISMATCHED IN ORDER TO REDUCE THE GAIN TO  $10 \text{ dB}$ . (i.e,  $G_A = 10 \text{ dB}$ ). THE DESIGNER CAN TRY TO REDUCE  $(VSWR)_{in}$  BY RELAXING THE OUTPUT VSWR.



3.36) (a) dc MODEL

$$(b) V_{TH} = \frac{24(4k)}{4k+16k} = 4.8V$$

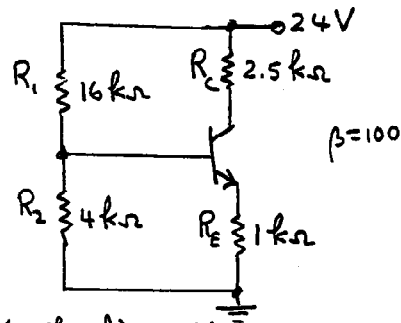
$$R_{TH} = 4k \parallel 16k = 3.2k\Omega$$

$$V_{TH} = I_B R_{TH} + 0.7 + I_C R_E \quad (I_C \approx I_E)$$

$$\therefore I_B = \frac{V_{TH} - 0.7}{R_{TH} + \beta R_E} = 40\mu A$$

$$I_C = \beta I_B = 4mA$$

$$V_{CE} = V_{CC} - I_C (R_C + R_E) = 24 - 4m(2.5k + 1k) = 10V$$



(c) AT 500MHz THE 0.1μF ( $Z_C = -j0.003\Omega$ ) ACT AS SHORT CIRCUITS TO THE AC SIGNAL. THUS, RFL ARE NOT NEEDED IN SERIES WITH THE 16kΩ AND 2.5kΩ RESISTORS.

THE 100nH INDUCTOR ( $Z_L = j314\Omega$ ) IMPEDANCE IS ABOUT 10% OF THE RESISTANCE OF  $R_2 = 4k\Omega$ . THUS, A RFL SHOULD BE USED IN SERIES WITH THE 4kΩ RESISTOR.

(d) ac MODEL

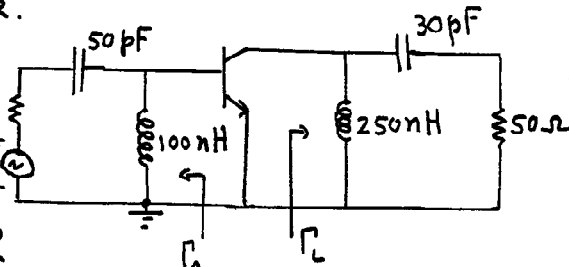
$$(e) Z = \frac{1}{50pF \cdot j2\pi 500 \cdot 10^6 \cdot 50 \cdot 10^{-12}} = -j6.37\Omega \quad 50\Omega$$

$$Z_{100nH} = j2\pi 500 \cdot 10^6 \cdot 100 \cdot 10^{-9} = j314.2\Omega \quad 50\Omega$$

USING THE ZY CHART IT IS SIMPLE TO

CALCULATE:  $\Gamma_{in} = 1.015 + j0.035$

$$\text{AND } \Gamma_{in} = 0.02 \angle 65.8^\circ$$



$$\text{SIMILARLY: } \Gamma_L = 1.05 - j0.11$$

$$\text{AND } \Gamma_L = 0.06 \angle -61^\circ$$

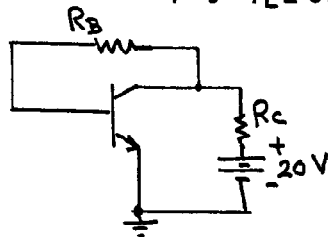
3.37) (a) dc MODEL

$$(b) 20 = I_C R_C + V_{CE}$$

$$\text{OR } R_C = \frac{20 - 10}{5m} = 2k\Omega$$

$$V_{CE} = I_B R_B + 0.7$$

$$R_B = \frac{10 - 0.7}{\left(\frac{5m}{100}\right)} = 186k\Omega$$



THIS TYPE OF DC BIAS RESULTS IN A LARGE VALUE FOR  $R_B$ .

(c) ac MODEL

$$\text{AT } f = 300MHz: Z_{30pF} = -j17.68\Omega,$$

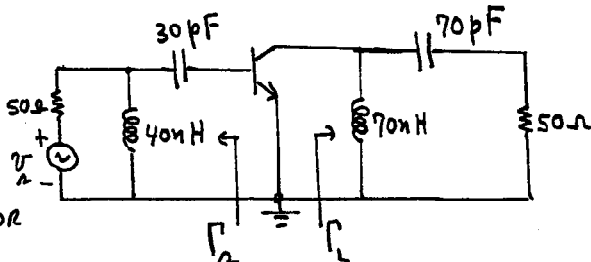
$$Z_{70pF} = -j7.58\Omega, Z_{40nH} = j75.4\Omega$$

$$Z_{70nH} = j131.9\Omega$$

USING THE ZY SMITH CHART OR

SIMPLE CALCULATIONS, WE OBTAIN:

$$Z_{in} = 35\Omega + j5.2\Omega \text{ OR } \Gamma_{in} = 0.185 \angle 157.3^\circ; Z_L = 49.9 + j1.25\Omega \text{ OR } \Gamma_L = 0.96 \angle 10^\circ.$$



$$3.38) \text{ LET } V_{CC} = 20 \text{ V}, R_E = \frac{10\% V_{CC}}{I_C} = \frac{0.1(20)}{10 \text{ m}} = 200 \Omega$$

$$V_{CC} = V_{CE} + I_C(R_C + R_E) \Rightarrow R_C + 200 = \frac{20 - 10}{4 \text{ m}} = 2.5 \text{ k}, \text{ OR } R_C = 2.3 \text{ k}\Omega$$

$$\text{FOR GOOD } \beta \text{ STABILITY LET } R_{TH} = \frac{\beta R_E}{10} = \frac{100(200)}{10} = 2 \text{ k}\Omega$$

$$V_{TH} = I_B R_{TH} + 0.75 + I_C R_E = \frac{4 \text{ m}}{100} (2 \text{ k}) + 0.75 + 4 \text{ m}(200) = 1.63 \text{ V}$$

$$R_1 = R_{TH} \frac{V_{CC}}{V_{TH}} = 2.3 \text{ k} \frac{20}{1.63} = 28.22 \text{ k}\Omega$$

$$R_2 = \frac{R_{TH}}{1 - V_{TH}/V_{CC}} = \frac{2.3 \text{ k}}{1 - (1.63/20)} = 2.5 \text{ k}\Omega$$

$$3.39) I_{C2} = 10 \text{ mA}. \text{ LET } I_3 = 20 \text{ mA}, \text{ THEN } I_{C1} = I_3 - I_{C2} = 20 \text{ m} - 10 \text{ m} = 10 \text{ mA}$$

$$\therefore R_4 = \frac{0.75}{I_{C1}} = \frac{0.75}{10 \text{ m}} = 75 \Omega. \text{ LET } V_{CC} = 20 \text{ V}$$

$$R_3 = \frac{V_{CC} - V_{CE,2}}{I_3} = \frac{20 - 10}{20 \text{ m}} = 500 \Omega$$

$$\text{FOR GOOD } \beta \text{ STABILITY LET } I_{R1} \approx I_{R2} = 20 I_{B1} = 20 \frac{10 \text{ m}}{100} = 2 \text{ mA},$$

$$V_{B,1} = V_{CE,2} - 0.75 = 9.25 \text{ V}$$

$$R_1 = \frac{V_{CC} - V_{B,1}}{I_{R1}} = \frac{20 - 9.25}{2 \text{ m}} = 5.37 \text{ k}\Omega$$

$$R_2 = \frac{V_{B,1}}{I_{R2}} = \frac{9.25}{2 \text{ m}} = 4.63 \text{ k}\Omega$$