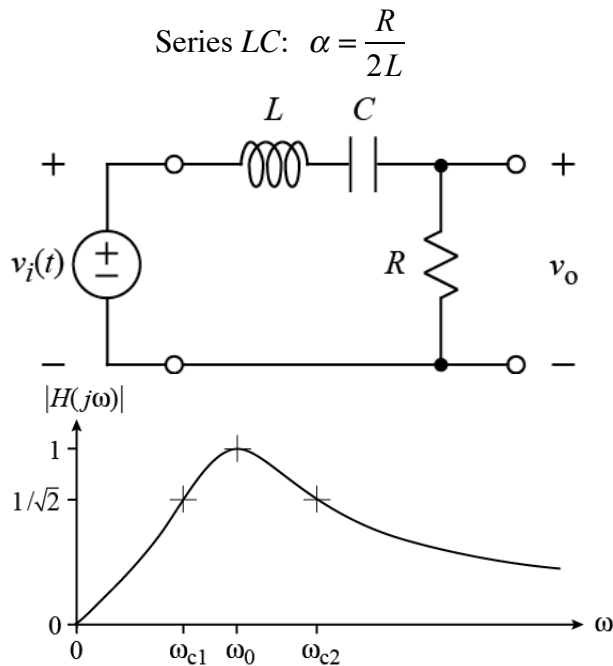


**TOOL:** The *RLC* circuits shown below act as two-pole band-pass filters.

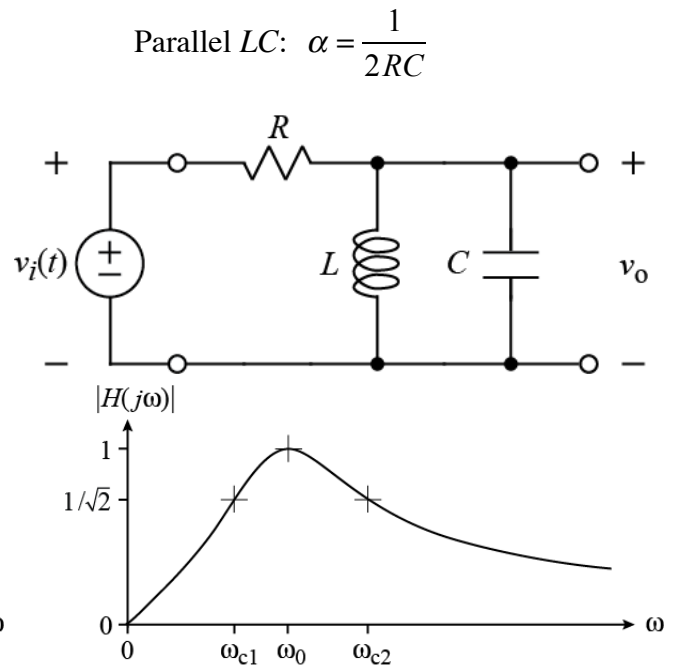
Series or parallel *LC*:  $\omega_0^2 = \frac{1}{LC}$  (resonant frequency;  $z_L = -z_C$ )  
 $\omega_{c1} = -\alpha + \sqrt{\alpha^2 + \omega_0^2}$  (lower cutoff frequency)  
 $\omega_{c2} = \alpha + \sqrt{\alpha^2 + \omega_0^2}$  (higher cutoff frequency)



$$H(j\omega) = \frac{R}{R + j\left(\omega L - \frac{1}{\omega C}\right)}$$

$$= \frac{1}{1 + j\frac{1}{R}\left(\omega L - \frac{1}{\omega C}\right)}$$

Fig. 1. Series *LC* band-pass filter.



$$H(j\omega) = \frac{j\omega L \parallel \frac{1}{j\omega C}}{R + j\omega L \parallel \frac{1}{j\omega C}}$$

$$= \frac{1}{1 + jR\left(\omega C - \frac{1}{\omega L}\right)}$$

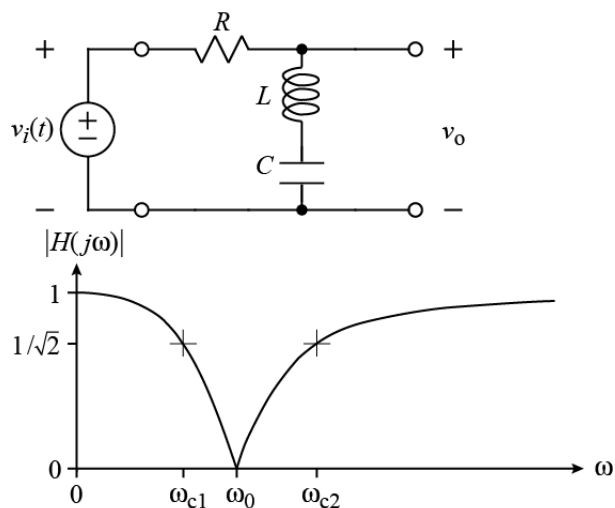
Fig. 2. Parallel *LC* band-pass filter.

**TOOL:** The *RLC* circuits shown below act as two-pole band-reject filters.

Series or parallel *LC*:  $\omega_0^2 = \frac{1}{LC}$  (resonant frequency;  $z_L = -z_C$ )  
 $\omega_{c1} = -\alpha + \sqrt{\alpha^2 + \omega_0^2}$  (lower cutoff frequency)  
 $\omega_{c2} = \alpha + \sqrt{\alpha^2 + \omega_0^2}$  (higher cutoff frequency)

Series *LC*:  $\alpha = \frac{R}{2L}$

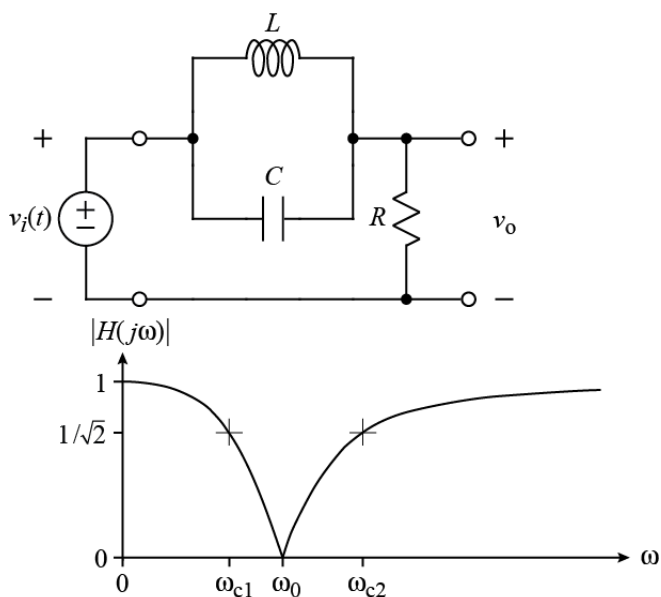
Parallel *LC*:  $\alpha = \frac{1}{2RC}$



$$H(j\omega) = \frac{j\omega L + \frac{1}{j\omega C}}{R + j\omega L + \frac{1}{j\omega C}}$$

$$= \frac{1}{1 - jR \left( \frac{1}{\omega L} - \frac{1}{\omega C} \right)}$$

Fig. 1. Series *LC* band-reject filter.



$$H(j\omega) = \frac{R}{R + j\omega L \parallel \frac{1}{j\omega C}}$$

$$= \frac{1}{1 - j\frac{1}{R} \left( \frac{1}{\omega C} - \frac{1}{\omega L} \right)}$$

Fig. 2. Parallel *LC* band-reject filter.