

**TOOL:** The following identities generate basic Laplace transforms:

$$\mathcal{L}\left[t^n e^{-at} \cos(\omega t) u(t)\right] = \frac{n! \operatorname{Re}[(s+a+j\omega)^{n+1}]}{[(s+a)^2 + \omega^2]^{n+1}}$$

$$\mathcal{L}\left[t^n e^{-at} \sin(\omega t) u(t)\right] = \frac{n! \operatorname{Im}[(s+a+j\omega)^{n+1}]}{[(s+a)^2 + \omega^2]^{n+1}}$$

where  $n, a, \omega \geq 0$ ;  $\delta(t)$  is the impulse (or delta) function, and  $u(t)$  is the unit step function:

$$\delta(t) \equiv \begin{cases} 0 & t \neq 0 \\ \infty & t = 0 \end{cases} \quad \text{with} \quad \int_{-\infty}^{\infty} \delta(t) dt = 1, \quad u(t) \equiv \begin{cases} 0 & t < 0 \\ 1 & t \geq 0 \end{cases}$$

TABLE:	$v(t)$	$V(s)$	values in basic identity
	1 or $u(t)$	$\frac{1}{s}$	$n = 0, a = 0, \omega = 0$
	$t$	$\frac{1}{s^2}$	$n = 1, a = 0, \omega = 0$
	$t^n$	$\frac{n!}{s^{n+1}}$	$n \geq 0, a = 0, \omega = 0$
	$e^{-at}$	$\frac{1}{s+a}$	$n = 0, a \geq 0, \omega = 0$
	$te^{-at}$	$\frac{1}{(s+a)^2}$	$n = 1, a \geq 0, \omega = 0$
	$t^n e^{-at}$	$\frac{n!}{(s+a)^{n+1}}$	$n \geq 0, a \geq 0, \omega = 0$
	$\cos(\omega t)$	$\frac{s}{s^2 + \omega^2}$	$n = 0, a = 0, \omega \geq 0$
	$\sin(\omega t)$	$\frac{\omega}{s^2 + \omega^2}$	$n = 0, a = 0, \omega \geq 0$
	$Ae^{-at} \cos(\omega t)$	$A \frac{(s+a)}{(s+a)^2 + \omega^2}$	$n = 0, a \geq 0, \omega \geq 0$
	$Be^{-at} \sin(\omega t)$	$B \frac{\omega}{(s+a)^2 + \omega^2}$	$n = 0, a \geq 0, \omega \geq 0$

**REF:** James A. Nilsson, Susan A. Riedel, *Electric Circuits*, 8th Ed., Upper Saddle River, NJ: Prentice Hall, 2007.