

**TOOLS:** The table below summarizes variances of combinations of random variables.

**VARIANCE (OR SQUARE OF STANDARD DEVIATION), 1 RANDOM VAR**

$$\sigma_X^2 = E\left((X - \mu_X)^2\right) = \int_{-\infty}^{\infty} (x - \mu_X)^2 f_X(x) dx = E(X^2) - (\mu_X)^2$$

$$\sigma_{aX+b}^2 = a^2 \sigma_X^2 \qquad \sigma_{aX+b} = a \sigma_X$$

**VARIANCE (OR SQUARE OF STANDARD DEVIATION), ANY 2 RAND VARS**

$$\sigma_{aX+bY}^2 = a^2 \sigma_X^2 + b^2 \sigma_Y^2 + 2ab \sigma_{XY} \text{ (see covariance below)}$$

**VARIANCE (OR SQUARE OF STAND DEV), 2 INDEPENDENT RAND VARS**

$$\sigma_{aX+bY}^2 = a^2 \sigma_X^2 + b^2 \sigma_Y^2$$

**COVARIANCE, ANY 2 RANDOM VARIABLES**

$$\sigma_{XY} = E(XY) - \mu_X \mu_Y = E((X - \mu_X)(Y - \mu_Y)) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} xyf(x, y) dy dx - \mu_X \mu_Y$$

$$\sigma_{aXbY} = ab \sigma_{XY}$$

**COVARIANCE, 2 INDEPENDENT RANDOM VARIABLES**

$$\sigma_{XY} = 0$$

**CORRELATION, ANY 2 RANDOM VARIABLES**

$$\rho_{XY} = \frac{\sigma_{XY}}{\sigma_X \sigma_Y} = \frac{\sigma_{XY}}{\sqrt{\sigma_X^2 \sigma_Y^2}}$$

$$\rho_{aXbY} = \rho_{XY}$$

**CORRELATION, 2 INDEPENDENT RANDOM VARIABLES**

$$\rho_{XY} = 0$$