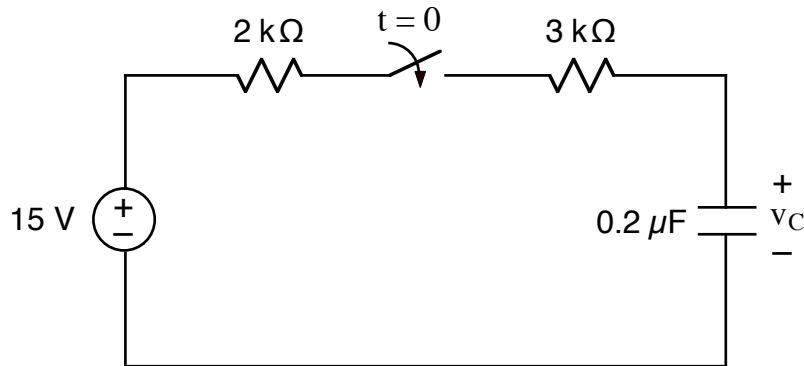


Ex:



After being open for a long time, the switch closes at $t = 0$. $v_C(t = 0^-) = 0V$. Find $v_C(t)$ for $t > 0$.

sol'n: Use the general form of solution for RC problems.

$$v_C(t > 0) = v_C(t \rightarrow \infty) + [v_C(0^+) - v_C(t \rightarrow \infty)] e^{-t/R_{Th}C}$$

We now proceed to find the following values:

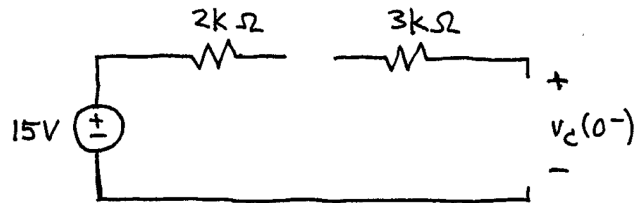
$$v_C(0^+), v_C(t \rightarrow \infty), \text{ and } R_{Th}$$

To find $v_C(0^+)$, we consider $t=0^-$ and find $v_C(0^-)$. Since v_C is an energy variable that cannot change instantly, we have $v_C(0^+) = v_C(0^-)$.

At $t=0^-$, currents and voltages have stabilized, and all time derivatives of currents and voltages are zero.

$$\text{Thus, } i_C = C \frac{dv_C}{dt} = C \cdot 0 = 0. \text{ } C \text{ looks like } \underline{\text{open}}.$$

$t = 0^-$: $C = \text{open}$, switch open



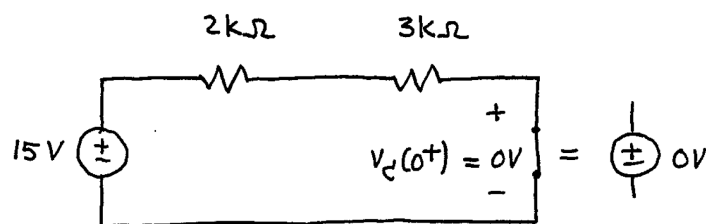
From the circuit diagram, we cannot determine $v_c(0^-)$. The C could be charged to some voltage, and it would remain at that voltage forever.

Fortunately, the problem states that $v_c(0^-) = 0V$.

$t = 0^+$: v_c cannot change instantly, so

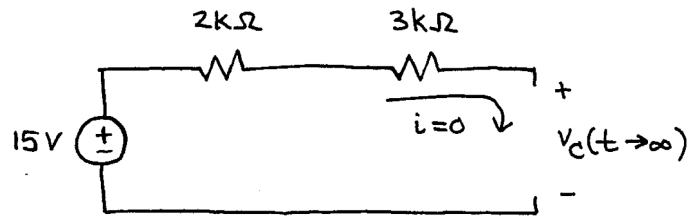
$$v_c(0^+) = v_c(0^-) = 0V$$

If needed a circuit model at $t = 0^+$, we would model the C as a v src with value $0V$. In other words, $C = \text{wire}$ at $t = 0^+$.



To find $v_c(t \rightarrow \infty)$, we again use the idea that currents and voltages are stable and $C = \text{open}$.

$t \rightarrow \infty$: $C =$ open, switch closed



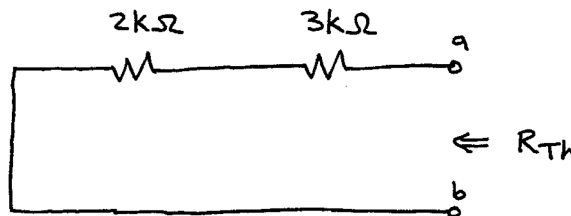
Since no current flows, the voltage drop across the $2k\Omega$ and $3k\Omega$ R's is $0V$.

Thus, we have $15V$ across C :

$$v_c(t \rightarrow \infty) = 15V$$

To find R_{Th} , we remove C and find the Thevenin equivalent resistance seen looking into the terminals where C was connected.

For the circuit we are using here, we can find R_{Th} by turning off the independent $15V$ source:



$$R_{Th} = 2k\Omega + 3k\Omega = 5k\Omega \quad R_{Th}C = 5k\Omega \cdot 0.2\mu F = 1ms$$

$$\therefore v_c(t > 0) = 15V + (0V - 15V)e^{-t/1ms}$$

\uparrow \uparrow \uparrow
 $v_c(t \rightarrow \infty)$ $v_c(0^-)$ $v_c(t \rightarrow \infty)$