
(a) Sum-of-products implementation

(b) NAND gate implementation

(c) Optimal NAND gate implementation

Figure 8.9. Implementation of XOR.

(a) Circuit with AND and OR gates

(b) Inversions needed to convert to NANDs

(c) NAND-gate circuit

Figure 8.10. Conversion to a NAND-gate circuit.

(a) Inversions needed to convert to NORs

(b) NOR-gate circuit

Figure 8.11. Conversion to a NOR-gate circuit.

(a) NAND-gate circuit

(b) Moving bubbles to convert to ANDs and ORs

(c) Circuit with AND and OR gates

Figure 8.14. Circuit for Example 8.8.

| Prime implicant | Minterm |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0 | 4 | 8 | 10 | 11 | 12 | 13 | 15 |
| $p_{1}=10 \times 0$ |  |  | $\checkmark$ | $\checkmark$ |  |  |  |  |
| $p_{2}=1011 \mathrm{x}$ |  |  |  | $\checkmark$ | $\checkmark$ |  |  |  |
| $p_{3}=110 \mathrm{x}$ |  |  |  |  |  | $\checkmark$ | $\checkmark$ |  |
| $p_{4}=1 \mathrm{x} 111$ |  |  |  |  | $\checkmark$ |  |  | $\checkmark$ |
| $p_{5}=11 \times 1$ |  |  |  |  |  |  | $\checkmark$ | $\checkmark$ |
| $p_{6}=\mathrm{x} \times 00$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |  | $\checkmark$ |  |  |

(a) Initial prime implicant cover table

| Prime <br> implicant | Minterm |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| $p_{1}$ | $\checkmark$ | 11 | 13 | 15 |
| $p_{2}$ | $\checkmark$ | $\checkmark$ |  |  |
| $p_{3}$ |  |  | $\checkmark$ |  |
| $p_{4}$ |  | $\checkmark$ |  | $\checkmark$ |
| $p_{5}$ |  |  | $\checkmark$ | $\checkmark$ |

(b) After the removal of essential prime implicants

| Prime <br> implicant | Minterm |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\checkmark$ | $\checkmark$ |  |  |
| $p_{4}$ |  | $\checkmark$ |  | $\checkmark$ |
| $p_{5}$ |  |  | $\checkmark$ | $\checkmark$ |

(c) After the removal of dominated rows

Figure 8.26. Selection of a cover for the function in Figure 2.58.

(a) Initial prime implicant cover table

| Prime implicant | Minterm |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0 | 2 | 5 | 6 | 7 | 8 |
| $p_{1}=00 \times 0$ | $\checkmark$ | $\checkmark$ |  |  |  |  |
| $p_{2}=0 \times 10$ |  | $\checkmark$ |  | $\checkmark$ |  |  |
| $p_{3}=0 \begin{array}{llll}1 & 1\end{array}$ |  |  |  | $\checkmark$ | $\checkmark$ |  |
| $p_{4}=\mathrm{x} 000 \mathrm{x}$ | $\checkmark$ |  |  |  |  | $\checkmark$ |
| $p_{5}=\mathrm{x} \times 01$ |  |  | $\checkmark$ |  |  |  |
| $p_{6}=1 \times 0 \times \mathrm{l}$ |  |  |  |  |  | $\checkmark$ |
| $p_{7}=\mathrm{x} 11 \times 1$ |  |  | $\checkmark$ |  | $\checkmark$ |  |

(b) After the removal of columns 9 and 13

| Prime | Minterm |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| implicant | 0 | 2 | 5 | 6 | 7 | 8 |
| $p_{1}$ | $\checkmark$ | $\checkmark$ |  |  |  |  |
| $p_{2}$ |  | $\checkmark$ |  | $\checkmark$ |  |  |
| $p_{3}$ |  |  |  | $\checkmark$ | $\checkmark$ |  |
| $p_{4}$ | $\checkmark$ |  |  |  |  | $\checkmark$ |
| $p_{7}$ |  |  | $\checkmark$ |  | $\checkmark$ |  |

(c) After the removal of rows $p_{5}$ and $p_{6}$

| Prime | Minterm |  |
| :--- | :---: | :---: |
| implicant | 2 | 6 |
| $p_{1}$ | $\checkmark$ |  |
| $p_{2}$ | $\checkmark$ | $\checkmark$ |
| $p_{3}$ |  | $\checkmark$ |

(d) After including $p_{4}$ and $p_{7}$ in the cover

Figure 8.28. Selection of a cover for the function in Example 8.12.

| Prime implicant | Minterm |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | 0 | 3 | 10 | 15 |
| $p_{1}=00 \times \mathrm{x}$ | $\checkmark$ | $\checkmark$ |  |  |
| $p_{2}=\mathrm{x} 0 \times 0$ | $\checkmark$ |  | $\checkmark$ |  |
| $p_{3}=\times 01 \times$ |  | $\checkmark$ | $\checkmark$ |  |
| $p_{4}=\mathrm{x} \times 11$ |  | $\checkmark$ |  | $\checkmark$ |
| $p_{5}=1 \times 1 \times$ |  |  | $\checkmark$ | $\checkmark$ |

(a) Initial prime implicant cover table

| Prime <br> implicant | Minterm <br> 0 |  |
| :---: | :---: | :---: |
| $p_{1}$ | $\checkmark$ |  |
| $p_{2}$ | $\checkmark$ |  |
| $p_{4}$ |  | $\checkmark$ |
| $p_{5}$ |  | $\checkmark$ |

(b) After including $p_{3}$ in the cover

| Prime | Minterm |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| implicant | 0 | 3 | 10 | 15 |
| $p_{1}$ | $\checkmark$ | $\checkmark$ |  |  |
| $p_{2}$ | $\checkmark$ |  | $\checkmark$ |  |
| $p_{4}$ |  | $\checkmark$ |  | $\checkmark$ |
| $p_{5}$ |  |  | $\checkmark$ | $\checkmark$ |

(c) After excluding $p_{3}$ from the cover

Figure 8.29. Selection of a cover for the function in Example 8.13.

