1. (24 pts) a) Draw the asymptotic Bode plot (the straight-line approximation) of the transfer function below. Accurately draw it on the graph provided. You must show the steps you use to get the Bode plot. That is, show things like the corner frequency(ies), the approximations of the transfer function in each frequency region, calculations of dB, etc.

\[ H(f) = \frac{1 \cdot 10^6 \cdot (3 \cdot 10^3 + 0.1 \cdot f)}{f \cdot (40 \cdot 10^3 + 2 \cdot f)} \]

b) The asymptotic Bode plot is not exact. Using a dotted line, sketch the actual magnitude of the transfer function \(|H(f)|\) on the plot above. Indicate the point(s) where the difference between the two lines is the biggest (draw arrow(s)) and write down the actual magnitude(s) at that (those) point(s).

c) If there are any corners in the Bode plot associated with poles in the transfer function, list that/those corner frequency(ies) here \(f_p\).

d) If there are any corners in the Bode plot associated with zeroes in the transfer function, list that/those corner frequency(ies) here \(f_z\).

2. (18 pts) a) A feedback system is shown in the figure. What is the transfer function of the whole system, with feedback.

\[ H(s) = \frac{X_{out}(s)}{X_{in}(s)} = ? \]

SHOW YOUR WORK
Simplify your expression for \(H(s)\) so that the denominator is a simple polynomial.

Be clear about your signs, so I can tell you what you’re doing.

b) Find the value of \(K\) to make the transfer function critically damped.

c) If \(K\) is Greater than this value the system will be: underdamped or overdamped Circle one

d) Does the transfer function have a zero?  
Answer no or find the \(s\) value of that zero.
3. (32 pts) The switch has been down for a long time and is switched up (as shown) at time $t = 0$.

a) What are the final conditions of $i_L$ and the $v_C$?
   
   $i_L(\infty) = ?$  
   $v_C(\infty) = ?$  

b) Find the initial condition and initial slope of $i_L$ that you would need to have in order to find all the constants in $i_L(t)$. Don't find $i_L(t)$ or it's constants, just the initial conditions.

c) Find the initial condition and initial slope of $v_C$ that you would need to have in order to find all the constants in $v_C(t)$. Don't find $v_C(t)$ or it's constants, just the initial conditions.

4. (26 pts) R, L, & C together are the load in the circuit shown. Find the following for the load (in dotted box):
   
   Be sure to show the correct units for each value.

a) The real power. $P = ?$

b) The reactive power. $Q = ?$

c) The complex power. $S = ?$

d) The apparent power. $|S| = ?$

e) The power factor. $\text{pf} = ?$

f) The power factor is: i) leading ii) lagging

(g) The magnitudes of the three currents. $|I_S| = ?$  
 $|I_R| = ?$  
 $|I_L| = ?$

h) Is there something weird about these currents? If so, what?

Answers

1. a), b)

2. a) $\frac{3}{6(s+6)}$  
 b) $\frac{1}{s^2} + 10s + 16 + \frac{30}{K}$  
 c) overdamped  
 d) - 6

3. a) 30 mA  
 b) 30 mA  
 c) 9 V  
 d) 432 VAR  
 e) (864 - 432 j) VA  
 f) 0.894  
 g) 8.05 A  
 h) $|I_S|$ is much less than $|I_R| + |I_C|$ because $I_R$ and $I_L$ are badly out of phase