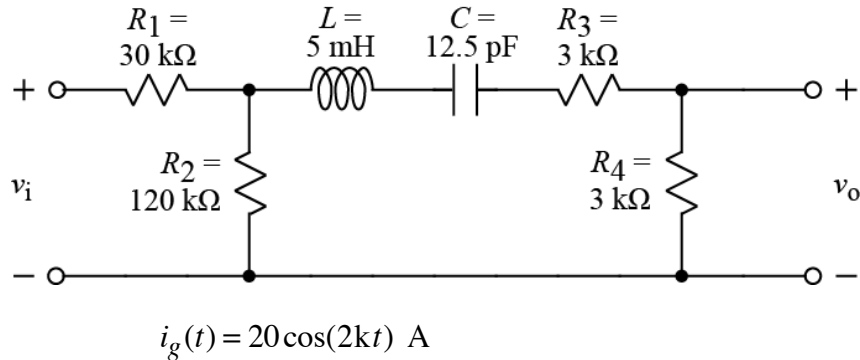


Ex:



- The above is what type of filter? (circle one of the following)
band-pass band-reject
- Find the center frequency, ω_o , of the above filter.
- Find the maximum value of the gain, $|H(j\omega)|$, of the above filter.
- Find the cutoff frequencies, ω_{C1} and ω_{C2} , of the above filter.

SOL'N: a) At resonance, see ω_o below, the L and C act like a wire. This reduces the impedance connecting the input signal to the output. Thus, the gain will be higher at resonance, and this is a **band-pass** filter.

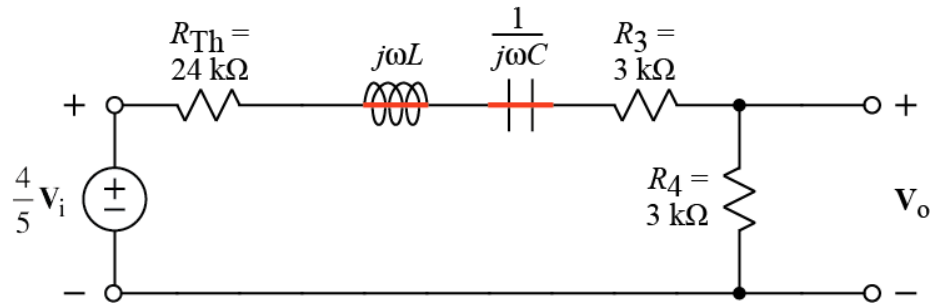
- b) The center frequency occurs when the impedances of the L and C cancel out. This occurs at the resonant frequency.

$$\omega_o = \frac{1}{\sqrt{LC}} = \frac{1}{\sqrt{5\text{m} \cdot 12.5\text{p}}} \text{ r/s} = \frac{1}{\sqrt{62.5\text{mp}}} \text{ r/s}$$

or

$$\omega_o = \frac{1}{\sqrt{62500\mu\text{p}}} \text{ r/s} = \frac{1}{250\mu\text{m}} \text{ r/s} = 4 \text{ Mr/s}$$

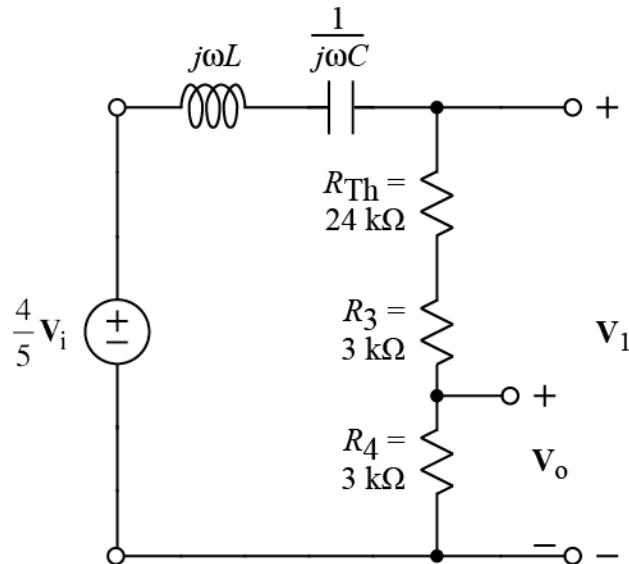
- c) The maximum gain occurs at the center frequency, when the L and C act like a wire. We may also convert v_i , R_1 , and R_2 to a Thevenin equivalent to simplify the calculation of the output voltage.



The transfer function is the ratio of the impedance across which V_o is measured.

$$|H(j\omega)| = \left| \frac{V_o}{V_i} \right| = \frac{4}{5} \frac{3\text{ k}\Omega}{|24\text{ k}\Omega + 3\text{ k}\Omega + 3\text{ k}\Omega|} = \frac{4}{50} = 0.08$$

- d) We put resistors together and compute the transfer function for the output taken across all three resistors.



We can express the transfer function in terms of the transfer function of V_1 relative to V_i .

$$H(j\omega) = \frac{V_o}{V_i} = \frac{V_o}{V_1} \frac{V_1}{V_i} = \frac{R_4}{R_{Th} + R_3 + R_4} \frac{V_1}{V_i} = \frac{1}{10} \frac{V_1}{V_i} = \frac{1}{10} H_1(j\omega)$$

The transfer function $H(j\omega)$ has the same cutoff frequencies as $H_1(j\omega)$, which is a standard RLC filter.

$$\omega_{C1,C2} = \pm \frac{R}{2L} + \sqrt{\left(\frac{R}{2L}\right)^2 + \frac{1}{LC}}$$

where

$$R = R_{Th} + R_3 + R_4$$

or

$$\omega_{C1,C2} = \pm \frac{30k}{2(5m)} + \sqrt{\left(\frac{30k}{2(5m)}\right)^2 + \frac{1}{5m(12.5p)}}$$

or

$$\omega_{C1,C2} = \pm 3M + \sqrt{(3M)^2 + \frac{1}{62500\mu p}}$$

or

$$\omega_{C1,C2} = \pm 3M + \sqrt{(3M)^2 + \left(\frac{1}{250m\mu}\right)^2} \text{ r/s}$$

or

$$\omega_{C1,C2} = \pm 3M + \sqrt{(3M)^2 + (4M)^2} \text{ r/s}$$

or

$$\omega_{C1,C2} = \pm 3 + 5 \text{ Mr/s}$$

or

$$\omega_{C1} = 2 \text{ Mr/s and } \omega_{C2} = 8 \text{ Mr/s}$$