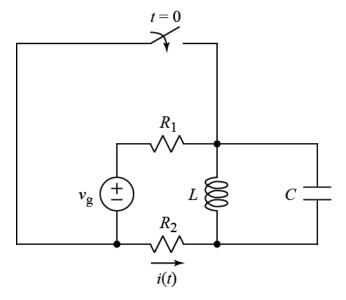


## Ex:



After being open for a long time, the switch closes at t = 0.

a) Give expressions for the following in terms of no more than  $v_g$ ,  $R_1$ ,  $R_2 L$ , and C:

$$i(t=0^+)$$
 and  $\frac{di(t)}{dt}\Big|_{t=0^-}$ 

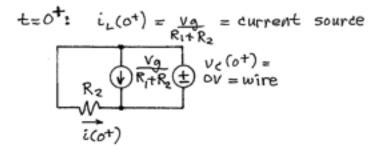
b) Find the numerical value of  $R_2$  given the following information:

$$R_1 = 150 \Omega$$
  $L = 40 \text{ mH}$   $C = 3.2 \,\mu\text{F}$   
 $\alpha = 1250 \text{ r/s}$   $\omega_d = 2500 \,\text{r/s}$ 

SOL'N: a) We start with the circuit at  $t=0^{-1}$ to determine the state of the L and C. At  $t=0^{-1}$ , L=wire, C=open $R_1$  $V_C(0^{-1})=OV$  (shorted by L)  $V_g = R_2$  $V_L = \frac{V_C}{L_1} = \frac{V_C}{R_1 + R_2}$ 

At 
$$t=0^+$$
, the switch is closed and  $i_{\perp}(0^+) = i_{\perp}(0^-)$  and  $v_{\perp}(0^+) = v_{\perp}(0^-)$ .

Vg and R1 are shorted out by the switch. This short divides the circuit into two halves that we may solve independently. The one we are interested in consists of R2, L, and C.



Because the C acts like a wire, all the current from the L will flow thru the C. So the current in  $R_2$  is zero. (Another way to see this is to observe that  $R_2$  has  $OV = V_C$  across it, and by Ohm's (aw  $i(O^{+}) = OV/R_2 = OA$ .)

\$0 i(0+)=0A.

For di , we first write i(+)

in terms of it and for ve.

We observe that ve is across R2:

i(t) = Ve/R2

Now we differentiate the entire egn:  $\frac{di(t)}{dt} = \frac{1}{R_2} \frac{dv_e}{dt} = \frac{1}{R_2} \frac{ie}{dt}$ (we have used  $id = C \frac{dv_d}{dt}$  rearranged.) We evaluate is at t=0t. We noted earlier that all the current from the L goes thru C. If we follow the direction of the current arrow for the L down, over, and up thru the C, we see that  $i_{c}(o^{+}) = -i_{L}(o^{+}) = -v_{g}$ . Thus,  $\frac{di(t)}{dt} = 1$  is  $(0^+)$ or  $\frac{di(t)}{dt} = \frac{-V_g}{R_2 C (R_1 + R_2)}.$ b) we use the circuit for t>0. We have a parallel RLC.  $\alpha = \frac{1}{2R_{1}C}, \quad \omega_{d} = \sqrt{\omega_{0}^{2} - \alpha^{2}}, \quad \omega_{0}^{2} = \frac{1}{LC}$ 

Use  $\alpha$ ;  $R_2 = \frac{1}{2\alpha C} = \frac{1}{2(1250)} \frac{\alpha}{3.2\mu} = 125 \Omega$