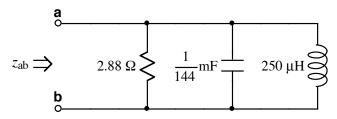
U

Ex:



Find a frequency,  $\omega$ , that causes  $z_{ab}$  to have a phase angle of  $-45^{\circ}$ , (i.e., imaginary part is the negative of the real part). Hint: use admittance, (the reciprocal of impedance).

sol'n: For single components in parallel, using admittance = 1/2 is helpful.

$$\frac{1}{z_{ab}} = \frac{1}{z_{R}} + \frac{1}{z_{d}} + \frac{1}{z_{d}}$$

Here, we have 
$$\frac{1}{2a} = \frac{1}{2\omega c} = -\frac{1}{2\omega c}$$

$$= \frac{1}{2\omega c} = -\frac{1}{2\omega c} = -\frac{1}{2\omega c} = -\frac{1}{2\omega c}$$
144m

If  $\angle Z_{ab} = -45^\circ$ , then  $Z_{ab} = k(1-j)$  where k is a positive real number.

Then 
$$\frac{1}{z_{ijb}} = \frac{1}{k(1-j)} = \frac{1+j}{k(1-j)(1+j)} = \frac{1+j}{2k}$$
.

Thus, 
$$\angle \frac{1}{2ab} = 45^{\circ}$$
 and  $Re\left[\frac{1}{2ab}\right] = Im\left[\frac{1}{2ab}\right]$ .

We observe that the values of i and i are pure imaginary

and constitute the entire imaginary part of 1/2 :

$$Im \left[ \frac{1}{2ab} \right] = Im \left[ \frac{1}{2a} + \frac{1}{2a} \right]$$

$$= Im \left[ j\omega C + \frac{1}{j\omega L} \right]$$

$$= Im \left[ j\omega C - \frac{j}{\omega L} \right]$$

$$= \omega C - \frac{1}{ab}$$

Note: Im [] has a real value. Im [a+jb] = b rather than jb.

The real part of Zab consists entirely of L:

$$Re\left[\frac{1}{R_{q}}\right] = Re\left[\frac{1}{R}\right] = \frac{1}{R}$$

Now we solve 
$$Re\left[\frac{1}{2ab}\right] = Im\left[\frac{1}{2ab}\right]$$
  
or  $\frac{1}{R} = \omega C - \frac{1}{\omega L}$ .

or 
$$\frac{1}{RC}\omega \simeq \omega^2 \sim \frac{1}{LC}$$

or 
$$\omega^2 - \frac{1}{RC} \omega - \frac{1}{LC} = 0$$

or 
$$\omega = \frac{1}{2RC} \frac{\pm}{\sqrt{\left(\frac{1}{2RC}\right)^2 + \frac{1}{LC}}}$$

Note: since  $\omega > 0$ , we use only  $+\sqrt{-1}$ .

$$\omega = \frac{1}{2RC} + \sqrt{\left(\frac{1}{2RC}\right)^2 + \frac{1}{LC}}$$

Now we calculate values.

$$\frac{1}{2RC} = \frac{1}{2(2.88)} \frac{1}{1} \frac{m}{1} \frac{g}{2(2.88k)} \frac{g}{g}$$

$$\frac{1}{1} = \frac{1M}{40g} = \frac{25k}{9} \frac{g}{1}$$

$$\frac{1}{1} = \frac{1}{250} \frac{1}{144} \frac{m}{1} \frac{g^{2}}{1}$$

$$\frac{1}{1} = \frac{144}{250} \frac{g}{1} \frac{g}{1} \frac{g}{1}$$

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Using values, we have the following:

$$\omega = 25 k/5 + \sqrt{(25k/5)^2 + (24k/5)^2}$$