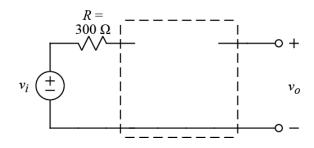
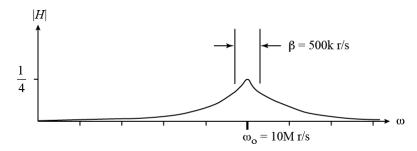
U

Ex:





Given the resistor connected as shown and using not more than one each R, L, and C in the dashed-line box, design a circuit to go in the dashed-line box that will produce the **band-pass**  $|H(j\omega)|$  vs.  $\omega$  shown above. That is:

$$\max_{\omega} |H(j\omega)| = \frac{1}{4}$$
 and occurs at  $\omega_0 = 10$  M r/s

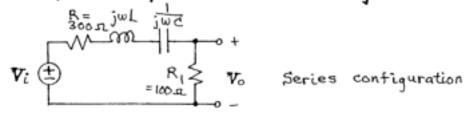
The bandwidth,  $\beta$ , of the filter is 500k r/s.

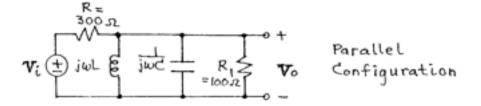
$$|H(j\omega)| = 0$$
 at  $\omega = 0$  and  $\lim_{\omega \to \infty} |H(j\omega)| = 0$ 

SOL'N: To achieve the peak at wo, we may use a series LC in the top rail or a parallel LC from the top to bottom rail. To achieve a gain of 1/4 at wo, we must use a vertical resistance to form a V-divider with R.

$$v_{i} + R_{i} = \frac{1}{4}$$
,  $3R_{i} = R = 300\Omega$ 

We have two possible circuit configurations:





Note: R, must be to the right of L and C in order to have any effect from the L and C in the series configuration.

For the series configuration, the Land C are to act like a wire at wo=10 M r/s.

The bandwidth when using a series L and C is

$$\beta = \frac{Reg}{L} = 500 \text{ kr/d}$$

to determine the value of Reg, we view the filter and a V-divider.

$$V_{i} \stackrel{\text{find}}{=} V_{o} \stackrel{\text{find}}{=} V_{o$$

The cutoff frequencies for  $H(j\omega)$  are the same as the cutoff frequencies for  $H'(j\omega)$ :

$$\omega_{cl,2} = \frac{\pm}{2L} \frac{Reg}{2L} + \sqrt{\left(\frac{Reg}{2L}\right)^2 + \omega_o^{2l}}, \beta = \frac{Reg}{L}$$

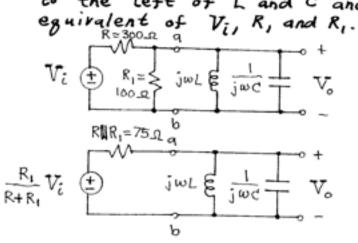
where Reg = R+R, = 400.12

Using  $\beta = \text{Reg}/L$ , we find L:

Using  $w_0^2 = \frac{1}{LC}$  and  $L = 800 \mu H$ , we find C:

Summary of series RLC: R,=100 R, L=800,4H, C=12.5 F

For the parallel configuration, we move  $R_1$  to the left of L and C and use a Therenin equivalent of  $V_i$ ,  $R_i$  and  $R_i$ .



To find the Therenin equivalent, we find V<sub>Th</sub> by finding the open-circuit, of the Vi, R, and R, directit

$$R_{i}$$
 directly the  $V_{i}$ ,  $R_{i}$  directly  $R_{i}$  d

To find RTh, we turn off Vi and look in from terminals a and b. The resistance seen is

Using the filter with the Thevenin equivalent, we have

$$H(j\omega) = \frac{V_0}{V_i} = \frac{R_1}{R+R_1} \frac{V_0}{V_i} = \frac{1}{4} H'(j\omega)$$

where 
$$H'(j\omega) = \frac{V_0}{V_i}$$
 where  $V_i = \frac{R_1}{R + R_1} V_i$ 

The cutoff frequencies of H'(jw) are the same as the cutoff frequencies of H(jw).

$$\omega_{cl,2} = \pm \frac{1}{2RC} + \sqrt{\left(\frac{1}{2RC}\right)^2 + \omega_o^2}, \quad \beta = \frac{1}{RC}$$

$$\omega_o^2 = \frac{Th}{LC}$$

Using Rin and B, we find C:

$$C = \frac{1}{RB} = \frac{1}{75 \cdot 2.500 \, k \, r/s} = 26.6 \, nF$$

Using L and wo, we find L: