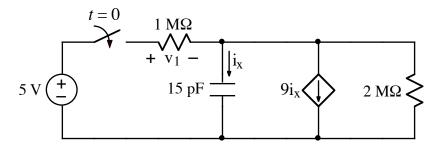
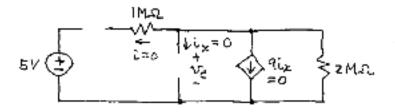


Ex:



After being open for a long time, the switch closes at t = 0. Find  $v_1(t)$  for t > 0.

solin: t=0 model: (to find  $v_c(o^2)$ ) C=open circuit



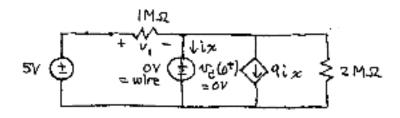
The total current flowing cut of top node equals zero, and there is no current flowing in the  $1M_{\rm R}$ , the C, and the dependent source. It follows that the current in the  $2M_{\rm R}$  is OA. By Ohm's law, the voltage drop across the  $2M_{\rm R}$  is  $0.2M_{\rm R} = 0.7$ . This is also the voltage across the C.

∴ v<sub>c</sub> (0<sup>-</sup>) = 0V

and

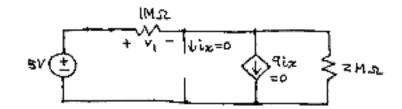
$$v_c(o^+) = v_c(o^-) = oV$$

We use this value of  $v_2(t=0^+)$  as a voltage source in the  $t=0^+$  model to find  $v_1(0^+)$ .



From a voltage loop on the left side, we have  $v_1(0^+) = 5V$ . Note: the components to the right of C are in parallel with the circuitry on the left and directly across the same voltage source, (namely OV).

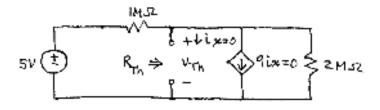
t > ∞ model: (to find v, (t > ∞)) C= open circle



The dependent src is off and effectively disappears. This leaves a voltage divider:

 $V_1(t \rightarrow \infty) = 5V \cdot 1M\Omega = 5V$  $1MQ + 2M\Omega = 3$ 

Finally, we have  $T = R_{Th} C$  where  $R_{Th}$  is the Therenin equivalent resistance seen looking into the terminals where C is connected.



Because there is a dependent source, we sind  $R_{Th}$  from  $R_{Th} = \frac{V_{Th}}{i_{SC}}$ .

 $V_{Th}$ ; as always, equals the voltage across the output terminals when nothing is connected across them. Since  $i_X = 0$  and  $9i_X = 0$ ,  $V_{Th}$  is given by a voitage divider formula:

$$V_{Th} = SV \cdot 2M.\Omega = \frac{10}{3}V$$

$$+ \frac{SV}{1M.\Omega} - \frac{10}{1M.\Omega} + 2M.\Omega = \frac{10}{3}V$$

$$+ \frac{SV}{1M.\Omega} - \frac{10}{1M.\Omega} + 2M.\Omega = \frac{10}{3}V$$

$$+ \frac{10}{10}\sqrt{2}V + \frac{10}{1$$

If we short out the output terminals, we have OV across the 2MD2 resistor. Thus, there is no current in the 2MD2 R.

A current summation for the top node reveals that the current in the IMSZ must be  $10i_X$ . From a V-loop on the left side, we also have SV across the IMSZ R. Thus, the current in the IMSZ R is  $5V/IMSZ = 5\mu A$ . Thus, we have

5, uA = 102x or 2x = 0,5 MA

From the schematic diagram, we see that

 $R_{Th} = \frac{V_{Th}}{\frac{1}{1}} = \frac{10}{3}V = \frac{20}{3}M_{SL}$ 

 $i_{sc} = i_{2} = 0.5 \,\mu A.$ 

Thus,  $\mathcal{C} = R_{Th}C = \frac{20}{3}$  MQ·15pF = 100 MS. Using the general form of solution, we have  $v_{\mathbf{f}}(t) = v_{\mathbf{i}}(t \rightarrow \infty) + [v_{\mathbf{i}}(t = 0^{\dagger}) - v_{\mathbf{i}}(t \rightarrow \infty)] e^{-t/t}$  $v_{\mathbf{i}}(t) = \frac{5}{3}v + [5v - \frac{5}{3}v] e^{-t/100} MS$ , t > 0

or 
$$v_1(t) = \frac{5}{3}V + \frac{10}{3}Ve$$
,  $t > 0$ 

Note: A much simpler way to solve that this problem is to observenthe 9ix dependent source acts like a capacitor that is 9 times C. Since the C and 9C are in parallel, we have an equivalent capacitance of 10C = 10.15 pF = 150 pF. The dependent source is now gone, and the solv is easier to find. The solution, of course is the same as above. R<sub>Th</sub> C is the same, but R<sub>Th</sub> = 1Ms2||2Ms and C=150 pF. v<sub>1</sub>(0<sup>+</sup>) and v<sub>1</sub>(t+m) are the same as before.