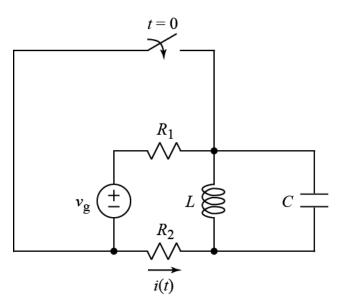


Ex:



After being open for a long time, the switch closes at t = 0.

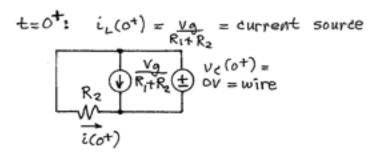
a) Give expressions for the following in terms of no more than v_g , R_1 , R_2 L, and C:

$$i(t=0^+)$$
 and $\frac{di(t)}{dt}\Big|_{t=0^-}$

b) Find the numerical value of R_2 given the following information:

At $t=0^+$, the switch is closed and $i_L(0^+)=i_L(0^-)$ and $v_C(0^+)=v_C(0^-)$.

Vg and R1 are shorted out by the switch. This short divides the circuit into two halves that we may solve independently. The one we are interested in consists of R2, L, and C.



Because the C acts like a wire, all the current from the L will flow thru the C. So the current in R_2 is zero. (Another way to see this is to observe that R_2 has $ov = v_C$ across it, and by Ohm's (aw $i(O^{\dagger}) = OV/R_2 = OA$.)

So i(0+) = 0 A.

For di | we first write i(+)

in terms of it and/or ve.

We observe that ve is across Rz:

Now we differentiate the entire egh:

$$\frac{di(t)}{dt} = \frac{1}{R_2} \frac{dv_c}{dt} = \frac{1}{R_2} \frac{ic}{c}$$

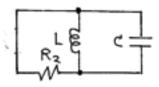
(we have used $id = C \frac{dv_c}{dt}$ rearranged.)

We evaluate it at t=0t. We noted earlier that all the current from the L goes thru C. If we follow the direction of the current arrow for the L down, over, and up thru the C, we see that

$$i_c(o^+) = -i_L(o^+) = -\frac{v_g}{R_1 + R_2}$$

Thus,
$$\frac{di(t)}{dt}\Big|_{t=0}^{t} = \frac{1}{R_zC} i_c(o^+)$$
or
$$\frac{di(t)}{dt}\Big|_{t=0}^{t} = \frac{-Vg}{R_zC(R_1+R_z)}.$$

b) We use the circuit for t>0.



We have a parallel RLC.

$$\alpha = \frac{1}{2R_2C}$$
, $\omega_0 = \sqrt{\omega_0^2 - \alpha^2}$, $\omega_0^2 = \frac{1}{LC}$