Ex: $\quad$ Sketch each of the following functions and then express each of them as a summation of products of common functions and step functions.
a) $\quad f(t)=\left\{\begin{array}{cc}0 & t \leq 1 \\ 2(t-1)^{2} & 1 \leq t \leq 2 \\ 2 & 2 \leq t \leq 5 \\ 2 e^{5-t} & 5 \leq t \leq 8 \\ 0 & 8<t\end{array}\right.$
b) $f(t)=\left\{\begin{array}{cc}0 & t<1 \\ 4 e^{-t / 3} \cos (\pi t) & 1 \leq t \leq 4 \\ 0 & 4<t\end{array}\right.$

Sol'N: a)


We use the pulses, shown in color, to turn on the three nonzero segments of $f(t)$.

$$
\begin{aligned}
f(t)= & 2(t-1)^{2}[u(t-1)-u(t-2)] \\
& +2[u(t-2)-u(t-5)] \\
& +2 e^{5-t}[u(t-5)-u(t-8)]
\end{aligned}
$$

b)


We use a single pulse from 1 to 4 .

$$
f(t)=4 e^{-t / 3} \cos (\pi t)[u(t-1)-u(t-4)]
$$

