

Ex: Find $v(t)$ if $V(s) = \frac{18s+148}{s^2+12s+11}$.

SOL'N: We have two real roots:

$$\mathcal{L}^{-1}\left\{\frac{18s+148}{s^2+12s+11}\right\} = \mathcal{L}^{-1}\left\{\frac{18s+148}{(s+1)(s+11)}\right\} = \mathcal{L}^{-1}\left\{\frac{A}{s+1} + \frac{B}{s+11}\right\}$$

We find A and B by the usual method of removing the pole and evaluating at the pole value:

$$A = (s+1)V(s)\Big|_{s=-1} = \frac{18s+148}{s+11}\Big|_{s=-1} = \frac{130}{10} = 13$$

$$B = (s+11)V(s)\Big|_{s=-11} = \frac{18s+148}{s+1}\Big|_{s=-11} = \frac{-50}{-10} = 5$$

Before proceeding, we check our result:

$$\frac{13}{s+1} + \frac{5}{s+11} = \frac{13(s+11) + 5(s+1)}{s^2+12s+11} = \frac{18s+143+5}{s^2+12s+11} \quad \checkmark$$

The inverse transform follows immediately:

$$\mathcal{L}^{-1}\left\{\frac{13}{s+1} + \frac{5}{s+11}\right\} = [13e^{-t} + 5e^{-11t}]u(t)$$