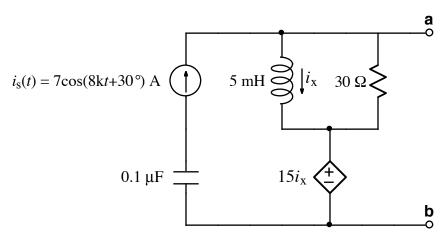
U

Ex:



- a) Draw a frequency-domain equivalent of the above circuit. Show a numerical phasor value for $i_s(t)$, and show numerical impedance values for R, L, and C. Label the dependent source appropriately.
- b) Find the Thevenin equivalent (in the frequency domain) for the above circuit. Give the numerical phasor value for V_{Th} and the numerical <u>rectangular form</u> for the impedance value of z_{Th} .

soln: a) We compute phasors and impedances.

$$P[is(t)] = P[7\cos(8kt+30^{\circ})A]$$
or $Is = 7230^{\circ}A$

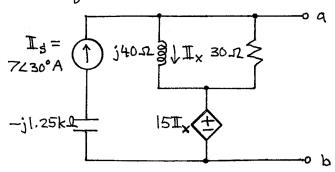
$$-j = -j \quad \Omega = -j \quad |k\Omega = -j|.25k\Omega$$

$$\overline{wC} = \frac{3k \cdot 0.|\mu}{8k \cdot 0.|\mu} \quad 0.8$$

$$j\omega L = j8k \cdot 5m \Omega = j40\Omega$$

$$I_{x} = P[i_{x}]$$

Frequency- or s-domain model:



b) The -j 1.2ks is in series with a current source and may be ignored.

Also, with no load connected across a and b, (the condition under which we measure V_{Th} across a and b), the j40-s and 30-s form a current divider.

$$I_{\times} = I_{5} \cdot \frac{30 \Omega}{30 \Omega + 1 0 \Omega}$$

$$= 7 \angle 30^{\circ} A \cdot \frac{30}{30 + 1 0}$$

$$= 7 \angle 30^{\circ} A \cdot \frac{30}{50 \angle 53.1^{\circ}}$$

$$= \frac{21}{5} \angle 30^{\circ} - 53.1^{\circ}$$

$$= \frac{21}{5} \angle -23.1^{\circ}$$

To obtain an exact expression for Ix, we may use the following alternative calculation:

$$I_{x} = I_{5} \cdot 30\Omega$$

$$30\Omega + j + 0\Omega$$

where
$$I_{3} = 7230^{\circ} A = 7\sqrt{3} + j\frac{7}{2}$$

$$I_{X} = 7 \cdot \left(\sqrt{3} + j\frac{1}{2}\right) \cdot \frac{36\Omega}{36\Omega + j46\Omega} \frac{36\Omega - j46\Omega}{36\Omega - j46\Omega} A$$

$$= \frac{2!}{2!} \frac{(\sqrt{3} + j \cdot 1)(3 - j \cdot 4)}{3^{2} + 4^{2}} A$$

$$= \frac{2!}{25} \cdot \frac{1}{2} \left(3\sqrt{3} + 4 - j4\sqrt{3} + j3\right) A$$

$$I_{X} = \frac{2!}{50} \left[3\sqrt{3} + 4 + j(3 - j4\sqrt{3})\right] A$$

$$V_{Th} = 15 I_{x} + I_{3} j40 \Omega | 30 \Omega$$
or
$$V_{Th} = 15 I_{x} + j40 \Omega I_{x}$$

$$= (15 + j40 \Omega) \frac{21}{50} [313 + 4 + j(3 - j413)] V$$

$$= \frac{21}{50} (4513 + 60 - 120 + 16013 + j160) V$$

$$V_{Th} = \frac{21}{50} \left[205\sqrt{3} - 60 + j(60\sqrt{3} + 205) \right] V$$

$$V_{Th} = \frac{21}{10} \left[41\sqrt{3} - 12 + j(12\sqrt{3} + 41) \right] = 21\sqrt{73} \ \angle 46.3^{\circ} \ V$$

If we opt form and an approximate answer, we have the following result:

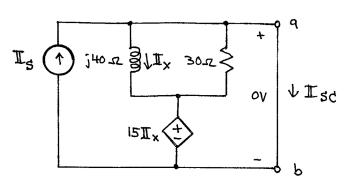
$$V_{Th} = (15+j40.52) I_{x}$$

$$= 5(3+j8) \cdot 21 \angle -23.1^{\circ} \lor$$

$$= 21 \cdot 173^{\circ} \angle 69.4^{\circ} - 23.1^{\circ} \lor$$

$$V_{Th} = 21\sqrt{73^{\circ}} \angle 46.3^{\circ} \lor$$

Now we find z_{Th} using $\overline{z}_{Th} = \frac{V_{Th}}{I_{sc}}$.



We observe that shorting a to b gives ov across the components in the middle. We suspect all of Is flows in the wire from a to b, meaning $I_{\times}=0$ and $15I_{\times}=0$ v.

We check whether $I_x = 0$ and $15I_x = 0V$ is plausible. It does because if $15I_x = 0V$, then we have 0V - 0V = 0V across the j 40s and 30s. Thus, $I_x = 0V = 0.V$ j40s

So $I_{\times} = 0$ is consistent, and $I_{SC} = I_{S}$.

$$\therefore \ \, \boldsymbol{\Xi}_{\mathsf{Th}} = \ \, \frac{\mathsf{V}_{\mathsf{Th}}}{\mathbb{I}_{\mathsf{5C}}} = \ \, \frac{\mathsf{V}_{\mathsf{Th}}}{\mathbb{I}_{\mathsf{5}}}$$

