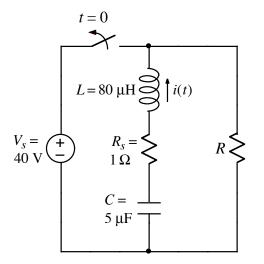


Ex:



or

After being closed for a long time, the switch opens at t = 0.

The above circuit is an analog "one-shot" circuit that, once charged, produces a short, rounded current-pulse resembling the current that flows in a synapse of a neuron. The circuit is critically damped.

- a) Find the value of *R* that makes the circuit critically-damped.
- b) Using the *R* value from (a), find a numerical expression for the inductor current, i(t), for t > 0.
- soln: a) After t=0, the switch is open, and the circuit becomes a series RLC with resistance R+Rs.

Characteristic roots are (always)

$$\sharp_{1,2} = -\alpha \pm \sqrt{\alpha^2 - \omega_0^2}$$

where $\alpha = \frac{R}{2L}$ for series RLC $w_0^2 = \frac{1}{LC}$ for series or parallel RLC

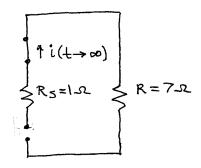
For critically-damped, we have

$$\beta_1 = \beta_2 \Rightarrow \alpha = \omega_0 \quad \text{or} \quad \alpha^2 = \omega_0^2$$

$$\begin{pmatrix} \underline{Reg} \\ 2L \end{pmatrix}^{2} = \frac{1}{LC} \quad \text{with} \quad \underline{Reg} = R_{3} + R$$
or
$$Reg = \frac{2}{L}$$
or
$$Reg = 2\sqrt{\frac{L}{C}} = 2\sqrt{\frac{80\mu}{5\mu}} \cdot n = 8.\Omega$$
or
$$1.52 + R = 8.\Omega$$
or
$$R = 7.\Omega$$
b) We use the general form of solv for
critically damped:

$$i(t>0) = A_1e^{st} + A_2te^{st} + A_3$$

We find A_3 from $i(t \rightarrow \infty)$. $t \rightarrow \infty$: C = open, L = wire, switch open



Since there is no pur source, $A_3 = i(t \rightarrow \infty) = 0 A$

We find A, and Az from initial cond's:

t=0: C=open, L=wire, switch closed i (0-) = 0 A (no path for current) Ve(0-) = 401 since no current in Rg means OV across Ry and v-loop on left must sum to zero volts, We find $i(o^{+})$ and $\frac{di(t)}{dt}\Big|_{t=0^{+}}$. $t=0^{+}: i_{L}(o^{+})=i_{L}(o^{-})=0A, v_{c}(o^{+})=v_{c}(o^{-})=40V$ $V_{L}(0^{+}) \stackrel{OA}{(open)} \stackrel{\uparrow}{(open)} \stackrel{\uparrow}{(open)} \stackrel{\uparrow}{(open)} \stackrel{\uparrow}{(open)} \stackrel{\uparrow}{(over} \stackrel{R=}{(over r_{-R})} \stackrel{\downarrow}{(over r$ $i(0^+) = i_1(0^+) = 0A$ For the symbolic soln we have

 $i(o^+) = A_1$

Equating the circuit value and symbolic solin form, we have $A_1 = 0A$. For the derivative, we have $\frac{di(t)}{dt} \Big|_{t=0^{+}} = \frac{V_{\perp}(0^{+})}{L}$ Using a v-loop, we have $V_{\perp}(0^{+}) = 40V$. For the symbolic solin we have $\frac{di(t)}{dt} \Big|_{t=0^{+}} = A_1^{\circ}s + A_2 = A_2 = \frac{40V}{80\mu}$ Thus, $i(t>0) = 500K + e^{St}A$

where
$$s = \frac{Reg}{2L} = \frac{8}{2(eo\mu)} = 50 \text{ K r/s}$$
.