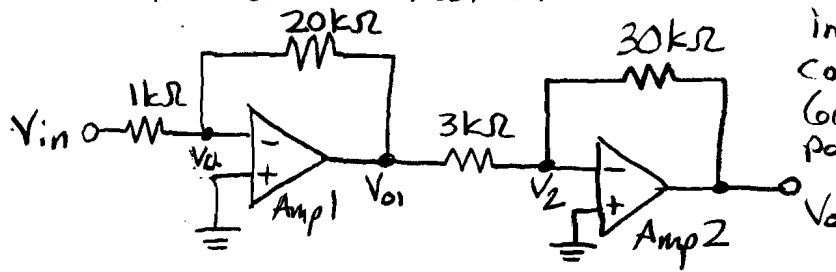


- 1) (a) An amplifier is a device whose output voltage is the same as its input voltage multiplied by some constant gain.
- (b) R_i is the input resistance, that is the resistance between the input terminals.
- (c) R_o is the output resistance, a resistor in series with the voltage output. It can load the circuit and reduce the gain of the amplifier.
- (d) Ideal Characteristics for an amplifier are $A_{vo} = \infty$, $R_i = \infty$, and $R_o = 0$.
- (e) A buffer amplifier is a voltage follower. It tracks the input voltage to the output terminals. They are used as impedance transformers or power amplifiers. It requires $A_{vo} = 1V/V$.
- (f) The gain-bandwidth product is the bandwidth achieved when a unity gain is desired. If we double the gain, we get half the bandwidth. The gain-bandwidth is specified on the op-amps' datasheets.

② Here is the circuit redrawn:



The two $10k\Omega$ resistors in series were combined. The two $60k\Omega$ resistors in parallel were combined

Amp1: Need to find the gain $\left(\frac{V_{01}}{V_{in}}\right)$

$$\frac{V_a - V_{in}}{1k\Omega} + \frac{V_a - V_{01}}{20k\Omega} = 0A$$

$$V_a = 0V \Rightarrow \frac{-V_{in}}{1k\Omega} - \frac{V_{01}}{20k\Omega} = 0A$$

$$\frac{V_{01}}{V_{in}} = \frac{-20k\Omega}{1k\Omega} = -20 \frac{V}{V}$$

Need to find f_{3dB}

From Datasheet: $f_T = 4.5 \text{ MHz}$ (Gain-Bandwidth Product)

$$\left| \frac{V_{01}}{V_{in}} \right| f_{3dB} = f_T \Rightarrow 20 f_{3dB} = 4.5 \text{ MHz}$$

$$f_{3dB} = 225 \text{ kHz}$$

Amp 2: $\frac{V_0}{V_{01}} = \frac{-30k\Omega}{3k\Omega} = -10 \frac{V}{V}$ (same algebra as above)

$$f_{3dB} = \frac{\text{gain} \times \text{bandwidth}}{\text{gain}} = \frac{100k \times 10 \leftarrow \text{graph. values from graph.}}{10 \leftarrow \left| \frac{V_0}{V_{01}} \right|} = 100 \text{ kHz}$$

Overall: Gain = $(-20)(-10) = 200 \frac{V}{V}$

$$\textcircled{a} \frac{V_{o1}}{V_{in}} = \frac{V_1}{V_{in}} = \frac{\text{Gain}}{\left(\frac{s}{f_{3dB}} + 1\right)} = \frac{-20}{\left(\frac{s}{2\pi \times 225k} + 1\right)}$$

$$\therefore \frac{V_1}{V_{in}} = \frac{-20}{\left(\frac{s}{2\pi \times 225k} + 1\right)}$$

$$\frac{V_o}{V_{o1}} = \frac{V_o}{V_1} = \frac{-10}{\left(\frac{s}{2\pi \times 100k} + 1\right)}$$

$$\therefore \frac{V_o}{V_1} = \frac{-10}{\left(\frac{s}{2\pi \times 100k} + 1\right)}$$

$$\textcircled{b} \frac{V_o}{V_{in}} = \frac{V_o}{V_1} \cdot \frac{V_1}{V_{in}} = \frac{-10}{\left(\frac{s}{2\pi \times 100k} + 1\right)} \cdot \frac{-20}{\left(\frac{s}{2\pi \times 225k} + 1\right)}$$

$$\therefore \frac{V_o}{V_{in}} = \frac{200}{\left(\frac{s}{200kr} + 1\right) \left(\frac{s}{450kr} + 1\right)}$$

(matlab assumes rad/sec.)

$$\textcircled{3} \text{ Overall } f_{3dB} \approx 800k \text{ rad/s or } 127kHz$$

See attached plot with code

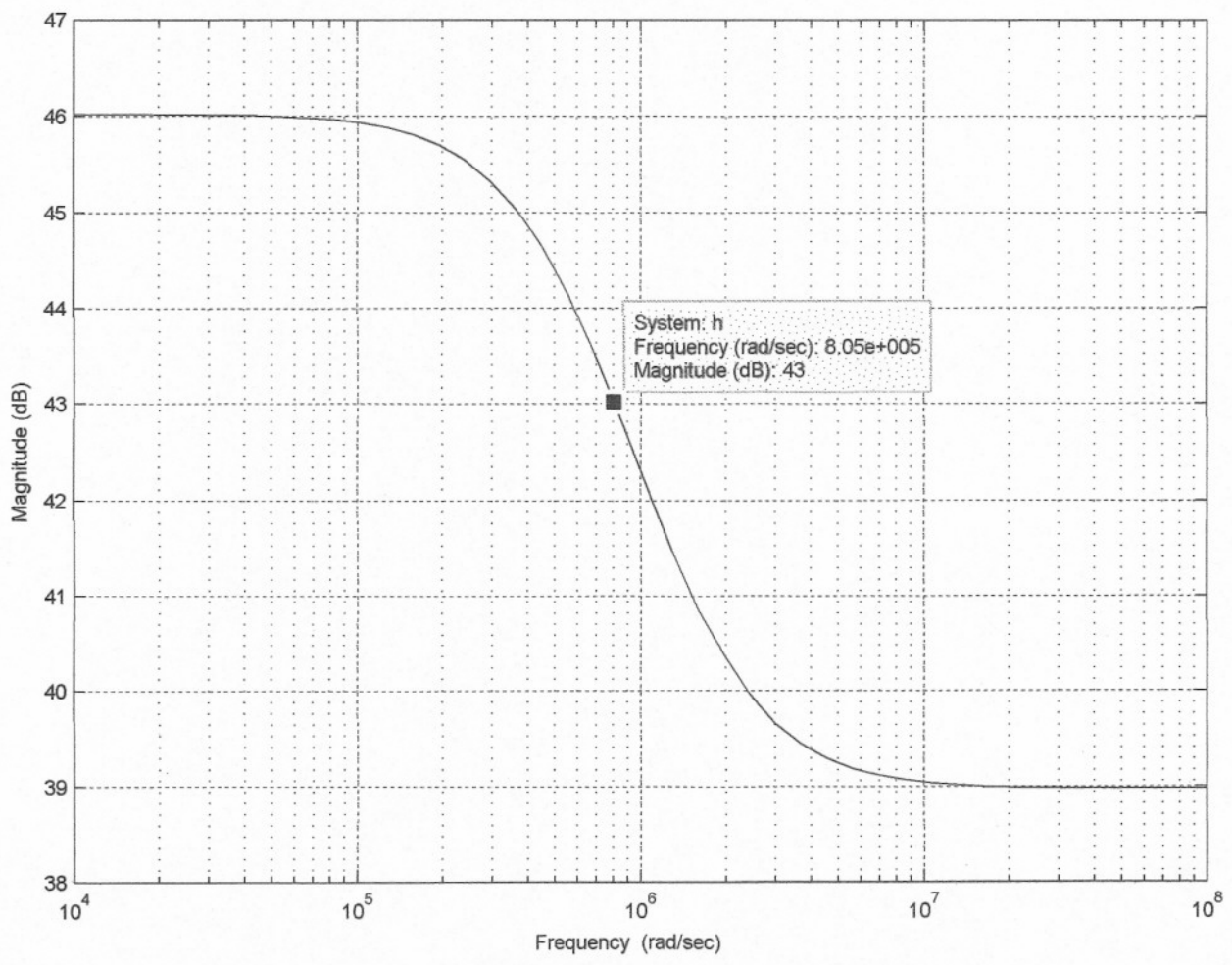
$$200 \text{ V/V} \Rightarrow 46dB$$

$$\therefore 43dB$$

$$43 \Rightarrow 10^{43/20} \approx 141 \text{ V/V}$$

$$h=200/((s/(2\pi*100e3))+1)*((s/(2\pi*225e3))+1)$$

Bode Diagram

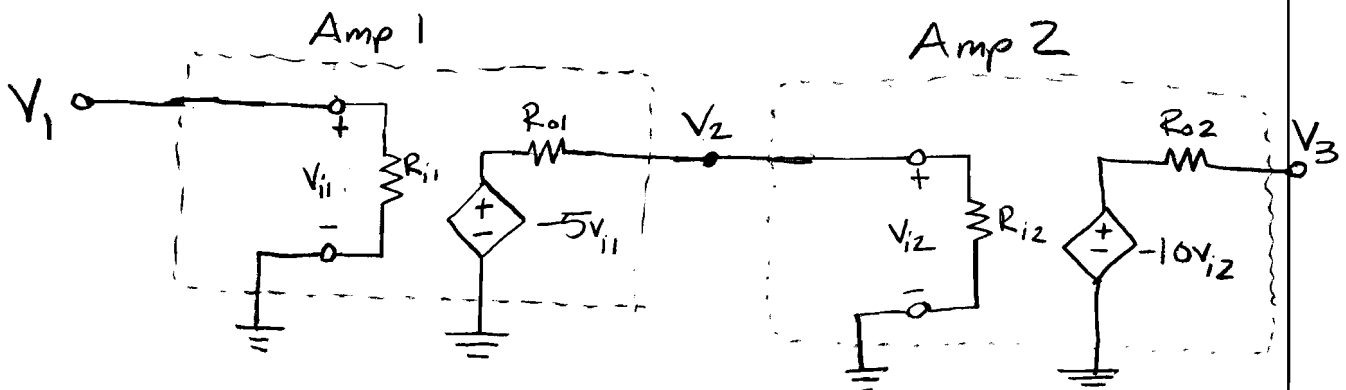


- ④ a) The algebra to find the gain for each amplifier is identical to the algebra used in 2a the gain was found to be $A_{vo} = -\frac{R_2}{R_1}$ where R_2 is the feedback resistor and R_1 is the resistor connected to the input voltage.

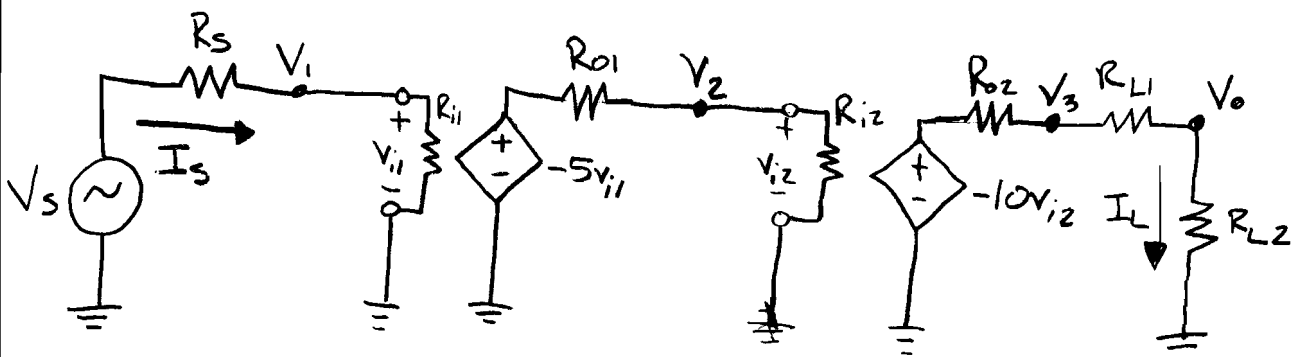
$$\frac{V_2}{V_1} = \frac{-10\text{k}\Omega}{2\text{k}\Omega} = -5\text{V/V} \quad (\text{Amp 1})$$

$$\frac{V_3}{V_2} = \frac{-20\text{k}\Omega}{2\text{k}\Omega} = -10\text{V/V} \quad (\text{Amp 2})$$

- ⑤ Redraw the two-stage amplifier



Note: $R_{11} = R_{12} = 100\text{k}\Omega$ $R_{01} = R_{02} = 5\text{k}\Omega$ Clips at $\pm 12\text{V}$



⑤ Find overall gain for circuit from #4.

$$V_o = -10V_{i2} \frac{R_{L2}}{R_{L1} + R_{L2} + R_{o2}} \quad \text{Voltage Divider}$$

$$V_{i2} = -5V_{i1} \frac{R_{i2}}{R_{i2} + R_{o1}}$$

$$V_{i1} = V_s \frac{R_{i1}}{R_s + R_{i1}}$$

$$V_o = (-10)(-5)V_s \frac{R_{i1} R_{i2} R_{L2}}{(R_s + R_{i1})(R_{i2} + R_{o1})(R_{L1} + R_{L2} + R_{o2})}$$

$$V_o = 50V_s \frac{(100\text{k}\Omega)(100\text{k}\Omega)(2\text{k}\Omega)}{(100.1\text{k}\Omega)(105\text{k}\Omega)(9\text{k}\Omega)} = 10.57V_s$$

$$\therefore \frac{V_o}{V_s} = \parallel \frac{V}{V} \quad \text{or } 20\text{ dB}$$

⑥ Find $\frac{I_L}{I_s}$

$$I_L = \frac{V_o}{R_{L2}} \quad I_s = \frac{V_s}{R_s + R_{i1}}$$

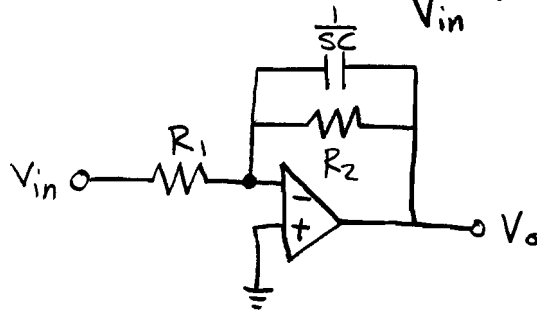
$$\frac{I_L}{V_o} = \frac{1}{R_{L2}} = \frac{1}{2\text{k}\Omega}$$

$$\frac{V_s}{I_s} = R_s + R_{i1} = 100\Omega + 100\text{k}\Omega = 100.1\text{k}\Omega$$

$$\frac{V_o}{V_s} = \parallel \frac{V}{V} \Rightarrow \frac{I_L}{I_s} = \frac{I_L}{V_o} \cdot \frac{V_s}{I_s} \cdot \frac{V_o}{V_s} = \frac{100.1\text{k}\Omega}{2\text{k}\Omega} \text{ (11)} = 550.55$$

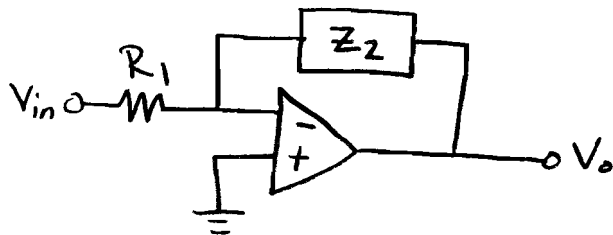
$$\therefore \frac{I_L}{I_s} = 551 \frac{\text{A}}{\text{A}} \quad \text{or } 55\text{ dB}$$

- 6) Analyze the circuit to obtain $\frac{V_o}{V_{in}}$, assuming an ideal op-amp.



Notice the feedback element can be rewritten as

$$Z_2 = \frac{1}{sC} \parallel R_2 = \frac{R_2/sC}{R_2 + \frac{1}{sC}} = \frac{R_2}{sCR_2 + 1}$$

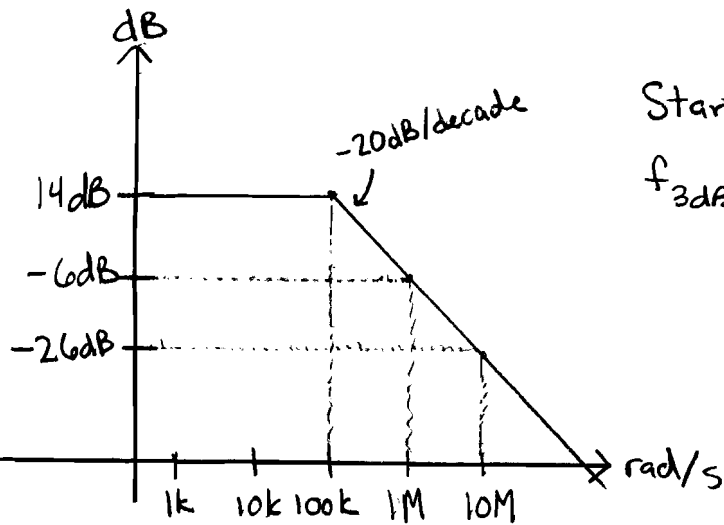


Now the algebra is identical to problem 2a.

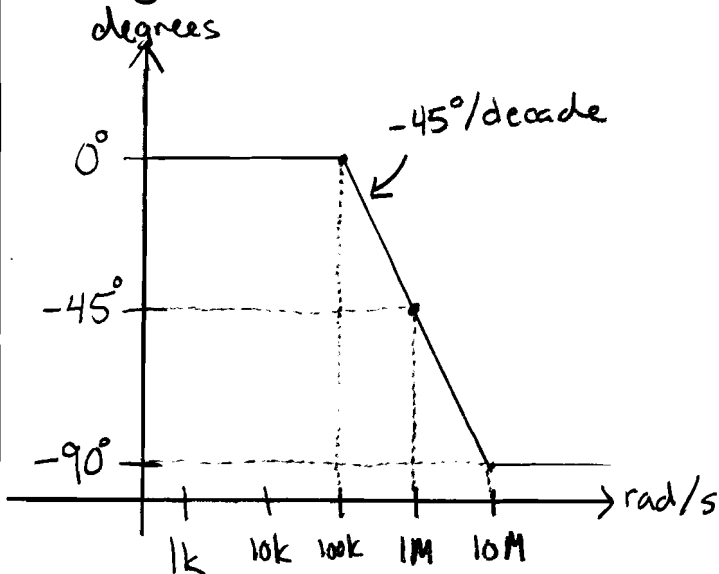
$$\frac{V_o}{V_{in}} = \frac{-Z_2}{R_1} = \frac{R_2/R_1}{sCR_2 + 1} = \frac{5}{10\mu s + 1}$$

$$\therefore \frac{V_o}{V_{in}} = \frac{5}{\frac{s}{100k} + 1}$$

⑦ Sketch the Straight Line Approx. for the Bode Plots from #6.

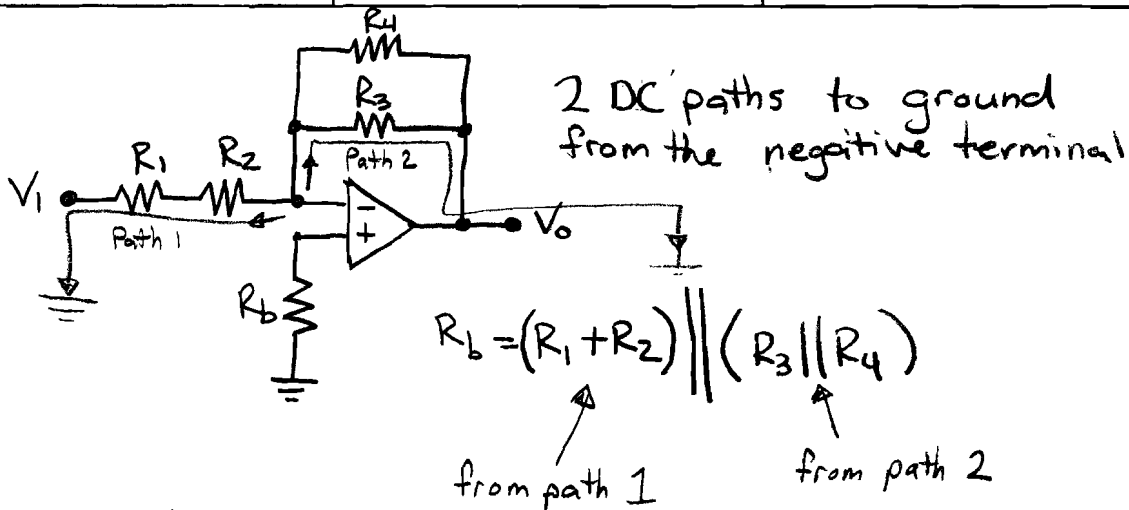


Magnitude Plot

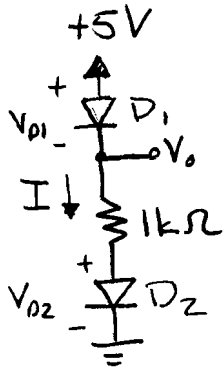


Phase Plot

8



9

ASSUME D_1, D_2 both on.

$$V_{D1} = 0.7$$

$$V_{D2} = 0.7$$

$$V_o = 5V - V_{D1} = 4.3V \quad (\text{K's V Law})$$

$$I = \frac{V_o - V_{D2}}{1k\Omega} = \frac{3.6V}{1k\Omega} \quad (\text{Ohm's Law})$$

$$I = 3.6 \text{ mA}$$

$$\therefore V_o = 4.3V \text{ and } I = 3.6 \text{ mA}$$

Check: Current is flowing the correct direction in both diodes, and the voltage drops were defined in the correct direction.