

## ECE 3510 homework # 10

- Draw a basic control system loop such as that shown in Fig 4.7 (Bodson), show all the items listed on p. 59 plus a feedback sensor labeled  $F(s)$  and a disturbance input.
- Add  $F(s)$  or  $n_f(s)$  and  $d_f(s)$  into the following equations: full  $Y(s) =$   
 With disturbance as zero: Eq. 4.5      Eq. 4.7      Eq. 4.10  
 With input ( $R(s)$ ) as zero: Eq. 4.13      Eq. 4.15
- List 5 measures of a control system's quality (see p. 59-60) and list one or two things that can be done to achieve each.
- The transfer functions of  $C(s)$  and  $P(s)$  are given below. In each case determine if the steady-state error will go to zero and whether disturbances will be completely rejected. Be sure to check for closed-loop stability when needed.
 

|                                     |                                |                                      |                               |
|-------------------------------------|--------------------------------|--------------------------------------|-------------------------------|
| a) $C(s) = \frac{s+4}{s^2+3s+2}$    | P(s) = $\frac{s+1}{s^2+3s}$    | b) $C(s) = \frac{s+1}{s^2+3s}$       | P(s) = $\frac{s+4}{s^2+3s+2}$ |
| c) $C(s) = \frac{s(s+6)}{s^2+3s+2}$ | P(s) = $\frac{s+8}{s^2+12s}$   | d) $C(s) = \frac{s+9}{s^2+3s+2}$     | P(s) = $\frac{s}{s+16}$       |
| e) $C(s) = \frac{s+1}{s^2+5s+6}$    | P(s) = $\frac{s+1}{s^2+8s+15}$ | f) $C(s) = \frac{s+1}{s^3+7s^2+12s}$ | P(s) = $\frac{s+1}{s+3}$      |
- Problem 4.2 (p.98) in the text. Use your calculator or Matlab to find the actual roots, or use the Routh-Hurwitz method.
- EXTRA CREDIT  
 Characteristic equations of feedback systems are shown below. In each case, use the Routh-Hurwitz method to determine the value range of  $K$  that will produce a stable system. You must show your work.
 

|                                      |                                      |
|--------------------------------------|--------------------------------------|
| a) $0 = s^4 + 20s^3 + 10s^2 + s + K$ | b) $0 = s^4 + 2Ks^3 + 5s^2 + Ks + K$ |
|--------------------------------------|--------------------------------------|

### Answers

- 1., 2., 3. Read sections 4.1 - 4.2 in text (Bodson).  $Y(s) = \frac{P \cdot C \cdot R + P \cdot D}{1 + P \cdot C \cdot F}$
4. a) Yes No      b) Yes Yes  
 c) No No      d) No Yes  
 e) No No      f) Yes Yes
5. a) Yes      b) No      c) No
6. EXTRA CREDIT a)  $0 < K < 0.4975$       b)  $0 < K < 2.25$