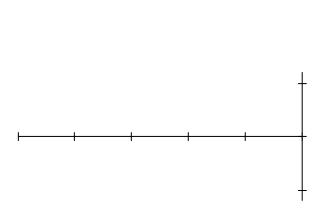
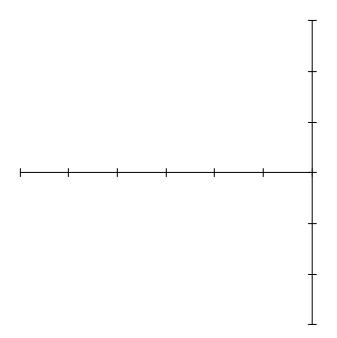
1. Problem 4.5 (p.109) in the text.

Sketch (by hand) the root-locus plot for the following open-loop transfer functions: Apply only the main rules (Section 4.6.2 in text or the first page of my notes)

a)
$$G(s) = \frac{s \cdot (s+1)}{(s+2)^2 \cdot (s+3)}$$

b)
$$G(s) = \frac{(s+3)}{s \cdot (s+9)^3}$$



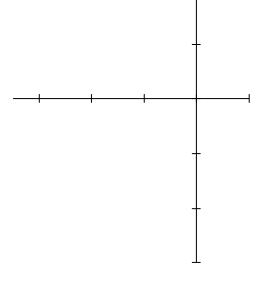


c)
$$G(s) = \frac{(s+a)}{(s+b)\cdot \left(s^2 - 2\cdot s + 2\right)}$$
 $a>0$ $b>0$ $k>0$ $a,b,\&$ k are all positive, real numbers

$$a > 0$$
 $b > 0$ $k > 0$

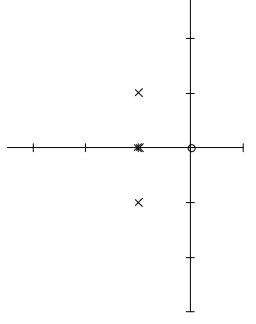
$$s^2 - 2 \cdot s + 2 = (s - 1 - j) \cdot (s - 1 + j)$$

Also give condition(s) that a and b must satisfy for the closed-loop system to be stable for sufficiently high gain (k) (note that you do not need to apply the Routh-Hurwitz criterion, nor provide the range of k for which the system is closed-loop stable).



- 2. Problem 4.12 in the text.
- ECE 3510 homework RL3 p2

Sketch the root-locus for the open-loop poles shown at right, using only the main rules. There is a zero at s=0, two poles at s=-1 and two poles at $s=-1\pm j$.

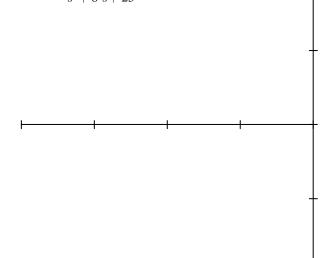


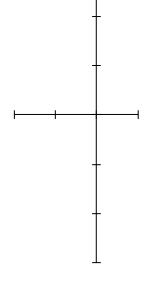
The following review questions and problems come from the Nise 3rd Ed., starting on page 471, Or 4th Ed., starting p 473. If you are using the 4th Ed., <u>clearly</u> state that on your homework.

- 3. Nise, Ch.8, review question 3, rephrased here: If $G(s_1) = 5 / 180^{\circ}$, is the point s_1 on the root locus? If yes, what gain factor would place a closed-loop pole at s_1 ?
- 4. Nise, Ch.8, review questions 4, 6, 7, 8, 9, 10.
 - 4. Do the zeros of a system change with a change in gain?
 - 6. What are two ways to find where the root locus crosses the imaginary axis?
 - (1)
 - (2)
 - 7. How can you tell from the root locus if a system is unstable?
 - 8. How can you tell from the root locus if the settling time does not change over a region of gain?
 - 9. How can you tell from the root locus that the natural frequency does not change over a region of gain?
 - 10. How would you determine whether or not the root locus plot crossed the real axis?

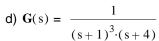
- 5. Nise, Ch.8, problem 3 Sketch the root locus for the following open-loop transfer functions:
 - a) $G(s) = \frac{(s+2)\cdot(s+6)}{s^2+8\cdot s+25}$

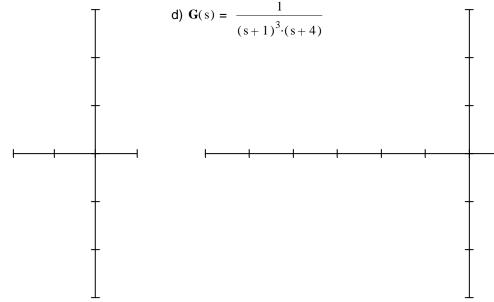
b) $G(s) = \frac{s^2 + 2^2}{s^2 + 1^2}$





c)
$$G(s) = \frac{s^2 + 1^2}{s}$$



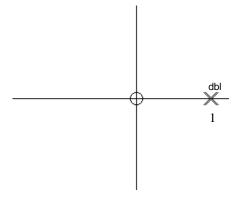


6. a) NISE Ch.8 problem 3a Find the break-in point for Nise, problem 3a, above. Note, the math here may drive you nuts, but you may simply test and prove that a point you guess is correct.

6. b) Find the break-away point for Nise, problem 3d, above.

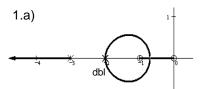
NISE Ch.8 problem 3d
$$G(s) = \frac{1}{(s+1)^3 \cdot (s+4)}$$

- 7. Problem 4.11 in the Bodson text. (Hint: do part c before b)
 - a) Sketch the root-locus for the open-loop poles shown at right. There is one zero at s=0 and two poles at s=1.
 - b) Give the range of gain k (k>0) for which the system is closed-loop stable, and give the locations of the $j\omega$ axis crossings.

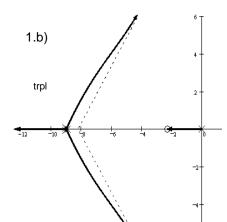


c) Give the location of the break-away point (arrival) on the real axis.

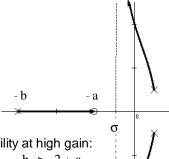
Answers

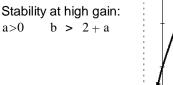


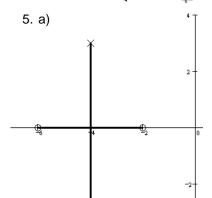
2.



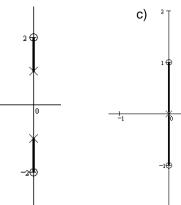
1.c)





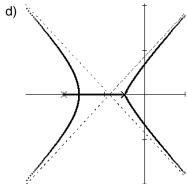


b)



dbl

5. d)



6. a) - 4



b) k>2 --> 7. c) 1, -1

ANSWERS TO REVIEW QUESTIONS

- 1. The plot of a system's closed-loop poles as a function of gain
- 2. (1) Finding the closed-loop transfer function, substituting a range of gains into the denominator, and factoring the denominator for each value of gain.
 - (2) Search on the s-plane for points that yield 180 degrees when using the open-loop poles and zeros.
- 3. Yes, K = 1/5
- 4. No
- 5. At the zeros of G(s) and the poles of H(s)
- 6. (1) Apply Routh-Hurwitz to the closed-loop transfer function's denominator. (2) Search along the imaginary axis for
- $G(s) = \pm 180^{\circ}$. (3) Use a computer with something like Matlab SISO tool to find the crossover point(s). (only need 2 ans)
- 7. If any branch of the root locus is in the rhp, the system may be unstable.
 - If the gain places one of the closed-loop poles on that part of the branch, it will be unstable.
- 8. If the branch of the root locus is vertical, the settling time remains constant for that range of gain on the vertical section.
- 9. The natural frequency is the distance of a pole from the origin. If a region of the root locus is circular and the center of the circle is at the origin, then the natural frequency would not change over that region of gain.
- 10. Determine if there are any break-in or breakaway points
- 11. (1) Poles must be at least five times further from the imaginary axis than the dominant second order pair,
 - (2) Zeros must be nearly canceled by higher order poles.
- 12. Number of branches, symmetry, starting and ending points
- 13. The zeros of the open loop system help determine the root locus. The root locus ends at the zeros. Thus, the zeros are the closed-loop poles for high gain.